



# Twisting spins and twisting layers

Leon Balents, KITP

College de France, June 10, 2022

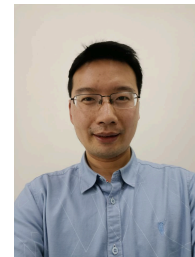


# Outline

- Twisting spins in  $\text{Mn}_3\text{Sn}$  with a magnetic field
- Multiple energy scales enable control of anomalous Hall effect



Kamran Behnia  
ESPCI

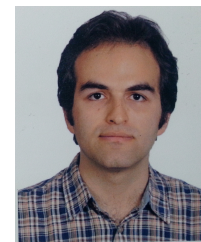


Zengwei Zhu  
Wuhan



Xiaokang Li  
Wuhan

- Twisting layers of spins in 2d materials
- Twists control new spin textures



Kasra Hejazi  
Caltech



Zhu-Xi Luo  
UCSB



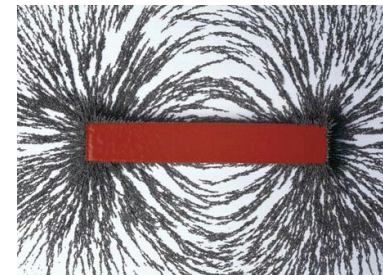
# Magnets

~500BC: Ferromagnetism  
documented in Greece,  
India, used in China



*sinan*, ~200BC

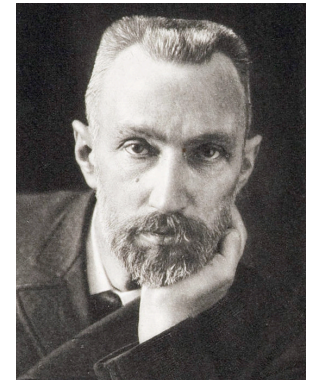
and in elementary school today





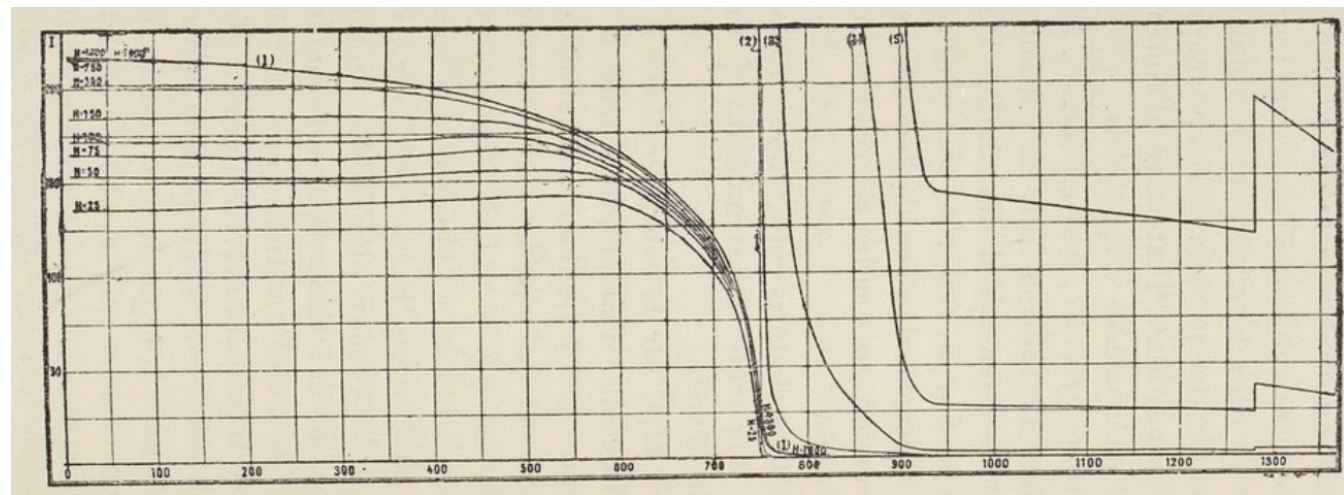
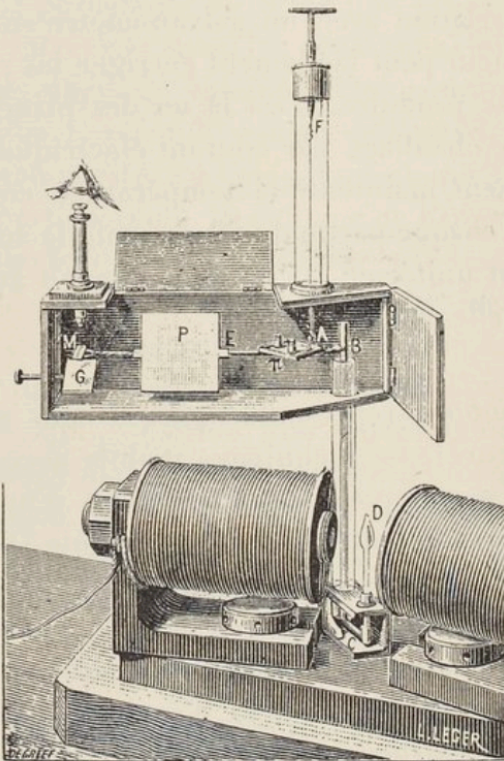
# PROPRIÉTÉS MAGNÉTIQUES DES CORPS A DIVERSES TEMPÉRATURES.

*Annales de Chimie et de Physique, 7<sup>e</sup> série, t. V, 1895, p. 289.*

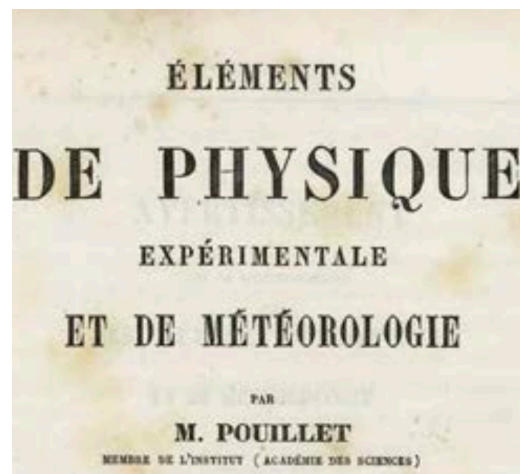


Pierre Curie

Fig. 3.







203. Influence de la chaleur sur le magnétisme. — Nous avons déjà dit qu'un aimant artificiel ou naturel, chauffé jusqu'au rouge blanc, perd complètement son magnétisme, de telle sorte qu'il n'est plus, après le refroidissement, qu'un corps inerte, sans force directrice et sans force magnétique. Cette observation est fort ancienne; elle avait été faite par Gilbert.

Quelques analogies assez remarquables entre les distances des atomes des corps et leurs propriétés magnétiques m'avaient conduit à penser que la limite magnétique des différents corps devait se trouver à des températures très-différentes, et j'ai, en effet, démontré par l'expérience :

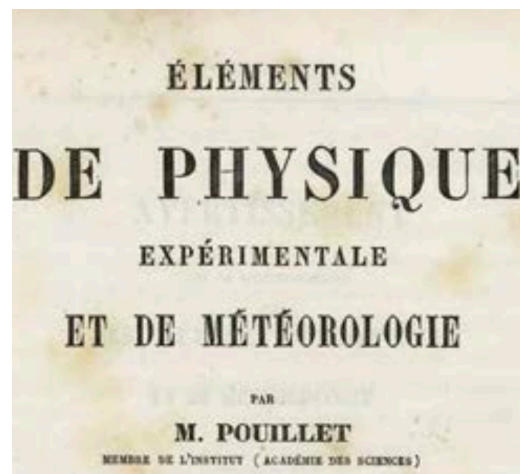
1° Que le cobalt ne cesse jamais d'être magnétique, ou plutôt que sa limite magnétique est à une température plus haute que le rouge blanc le plus éclatant ;

2° Que le chrome a sa limite magnétique un peu au-dessus de la température rouge sombre ;

3° Que le nickel a sa limite magnétique vers  $350^{\circ}$ , à peu près à la température de la fusion du zinc ;

4° Enfin, que le manganèse a sa limite magnétique à la température de  $20$  à  $25^{\circ}$  au-dessus de  $0^{\circ}$ .





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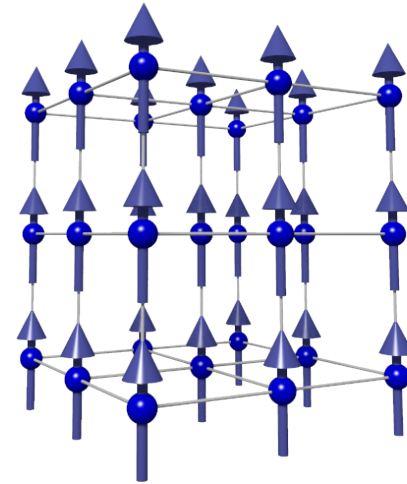




# Magnetism

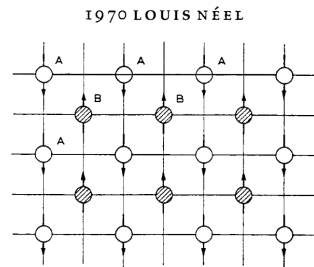
- Atomic spins interact via *exchange* to favor an ordered arrangement
- Aligned parallel: ferromagnets

$$H = -J \sum_{\langle ij \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$



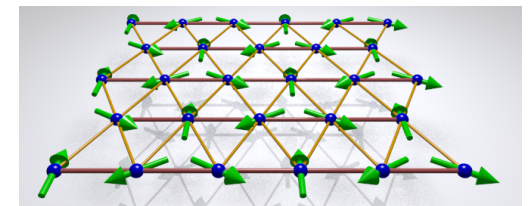
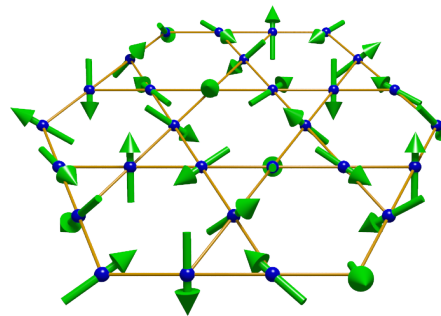
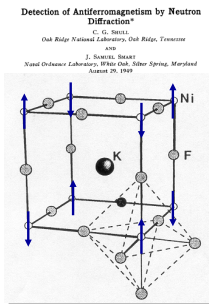
# Magnetism

- Atomic spins interact via *exchange* to favor an ordered arrangement
- More complex arrangements: antiferromagnets



Louis Néel

1949AD:  
antiferromagnetism  
proven experimentally  
  
but there are 1000s of  
them, much more  
common than FMs





# AHE

“Anomalous” Hall effect: a field-independent contribution to the Hall effect due to magnetic order

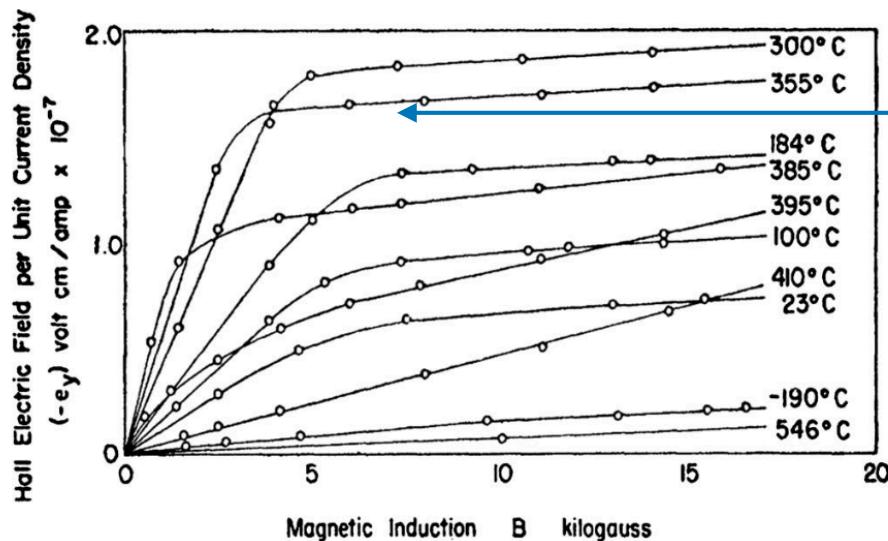


FIG. 1. The Hall effect in Ni (data from [Smith, 1910](#)). From [Pugh and Rostoker, 1953](#).

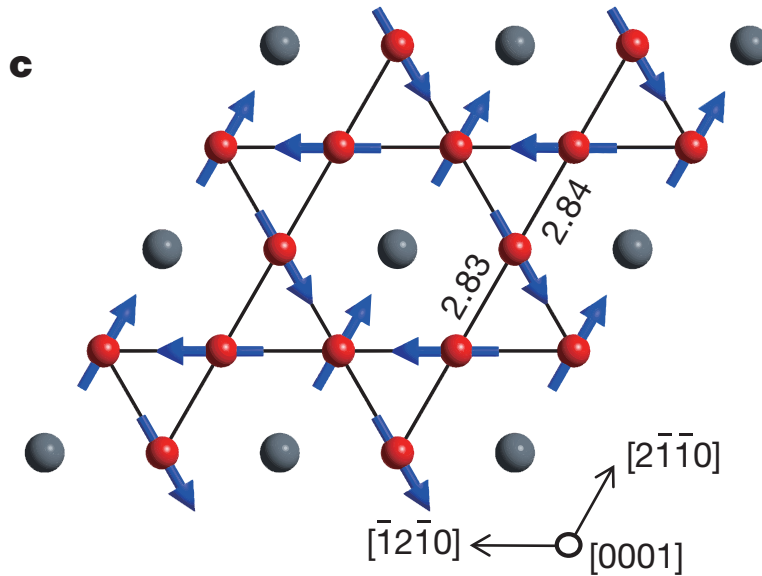
$$\rho_H = R_H B + \rho_{AH}$$

NICKEL.

La température de transformation magnétique du nickel est voisine de 340°; nous avons étudié ce corps entre 373° et 806°. Le coefficient d'aimantation est alors indépendant de l'intensité du champ. Il décroît régulièrement et très rapidement quand la température augmente. Le nickel était renfermé dans un tube de platine. Les résultats obtenus sont consignés dans le Tableau XV et figure 12.

Commonly seen in ferromagnets

# Mn<sub>3</sub>Sn



Spins arranged into  
elementary triangles -  
"kagomé"

large ordered  
*antiferromagnetic*  
moment

$$\sim 2 \mu_B / \text{Mn}$$

tiny FM moment:

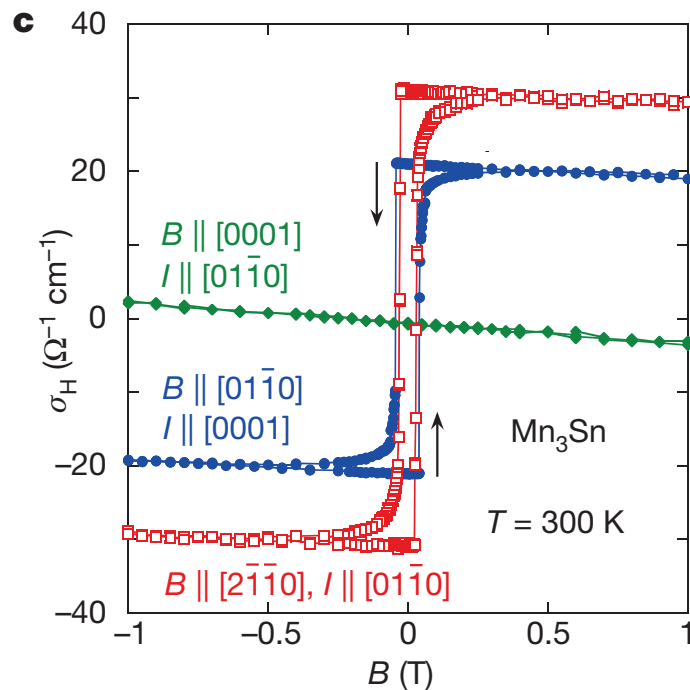
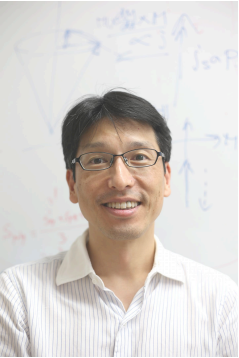
$$.002 \mu_B / \text{Mn}$$

$$T_N \sim 420\text{K}$$

Nagamiya et al, 1982



# AHE



S. Nakatsuji *et al*, 2015

$\text{Mn}_3\text{Sn}$ :

Large “anomalous” Hall conductivity

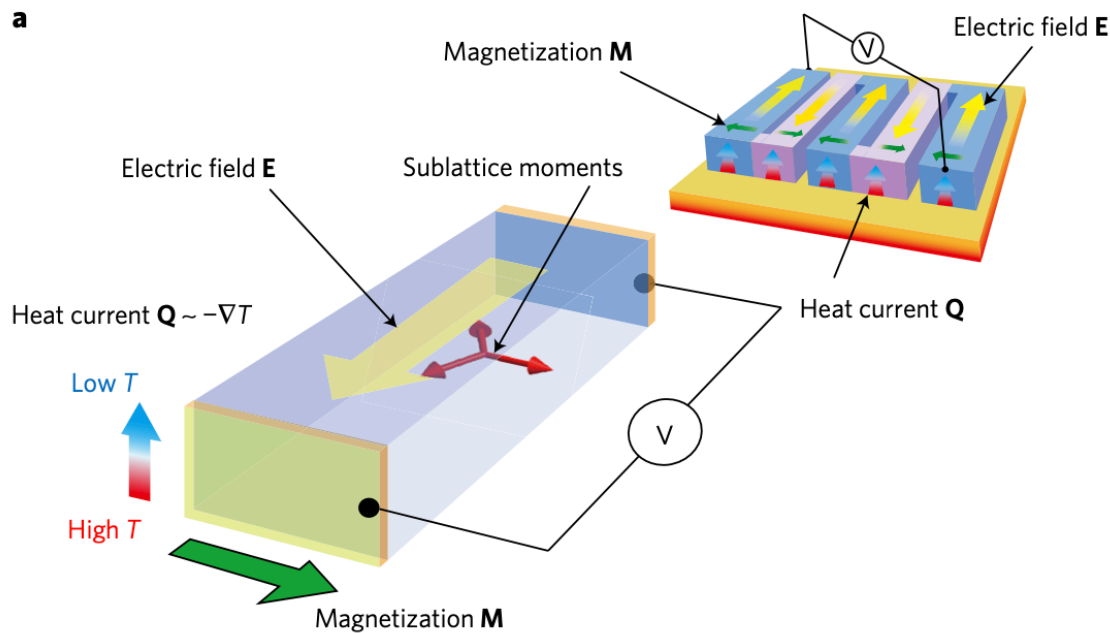
Tiny magnetization

Small coercive field

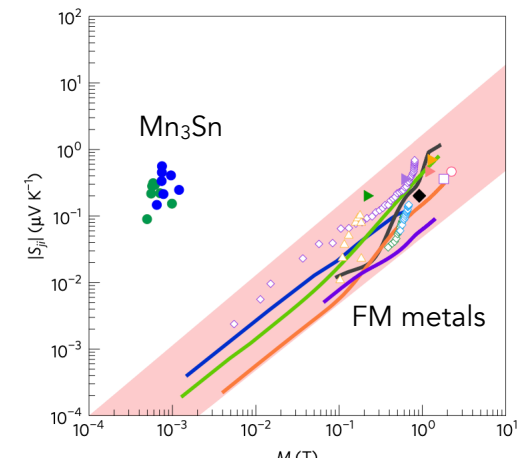
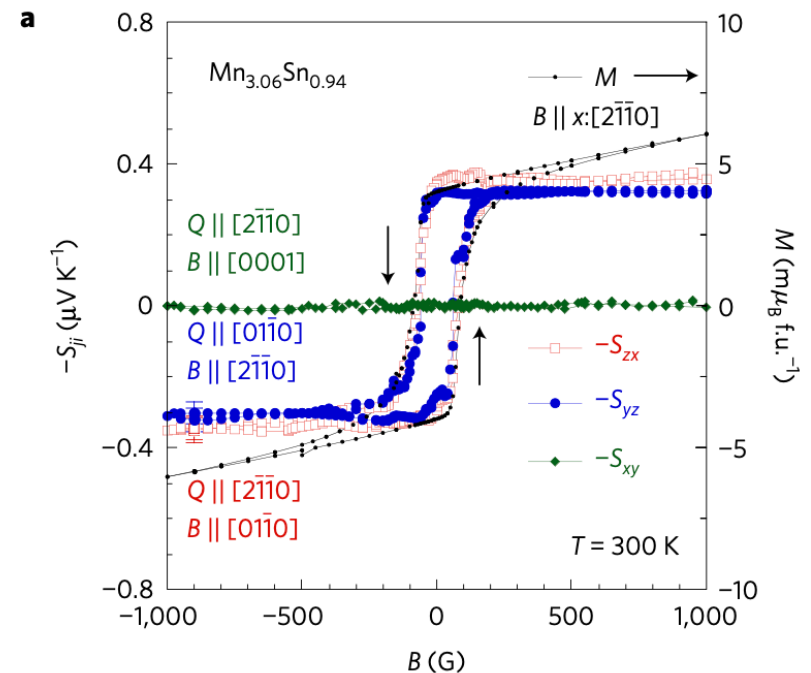
These properties are a desirable combination

# Anomalous Nernst Effect

Related effect with potential thermoelectric applications

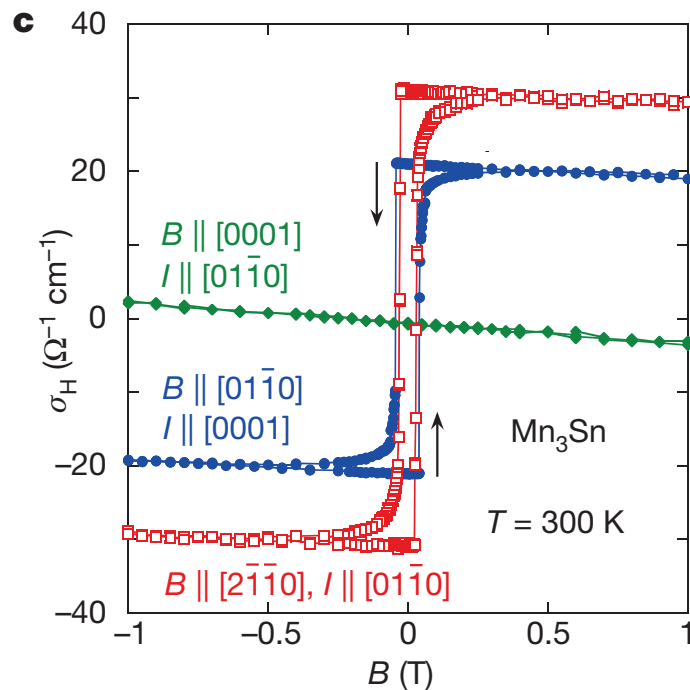
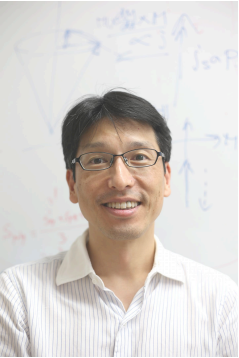


Electric field perpendicular to temperature gradient





# AHE



S. Nakatsuji *et al*, 2015

$\text{Mn}_3\text{Sn}$ :

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Small coercive field

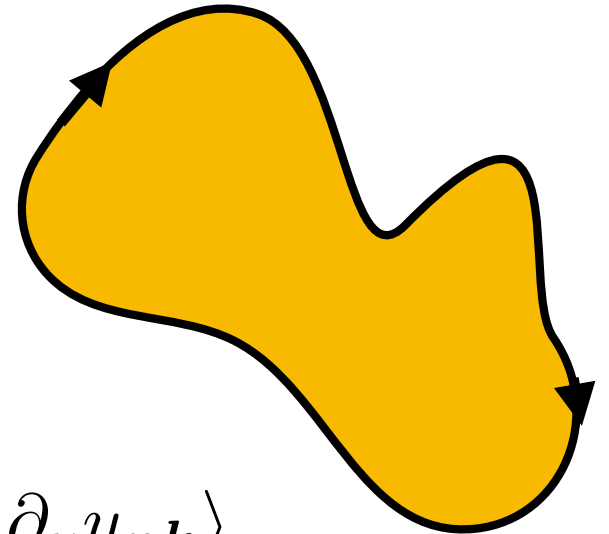
How do these properties go together???

# Twisting wave functions

Intrinsic anomalous Hall effect from  
Berry curvature:

$$\sigma_{\mu\nu}^{\text{AH}} = \frac{e^2}{\hbar} \epsilon_{\mu\nu\lambda} \Omega_{\lambda}$$

$$\Omega_{\lambda} = \epsilon_{\mu\nu\lambda} \sum_n \int \frac{d^3\mathbf{k}}{(2\pi)^3} n_F(\epsilon_{n\mathbf{k}}) \langle \partial_{\mu} u_{n\mathbf{k}} | \partial_{\nu} u_{n\mathbf{k}} \rangle$$



Karplus+Luttinger,  
1954



Physical meaning:

“Flux” of Berry curvature gives phase  
accumulated in an electron’s orbit

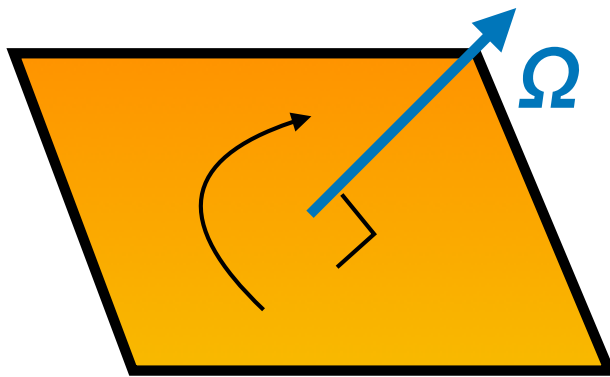


Thouless, Haldane

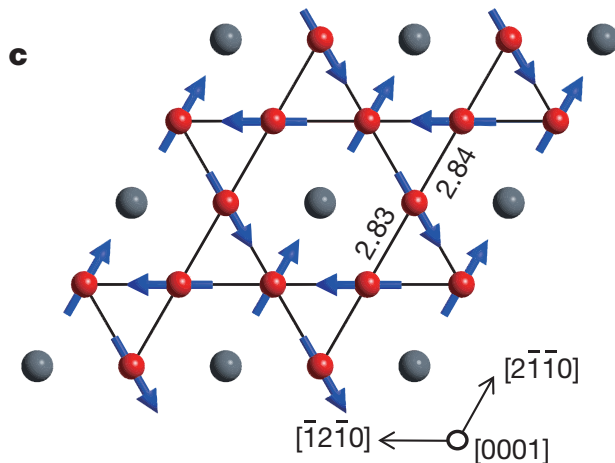


# Twisting wave functions

Hall vector  $\mathbf{\Omega}$ :  $\sigma_{\mu\nu}^{\text{AH}} = \frac{e^2}{\hbar} \epsilon_{\mu\nu\lambda} \Omega_\lambda$



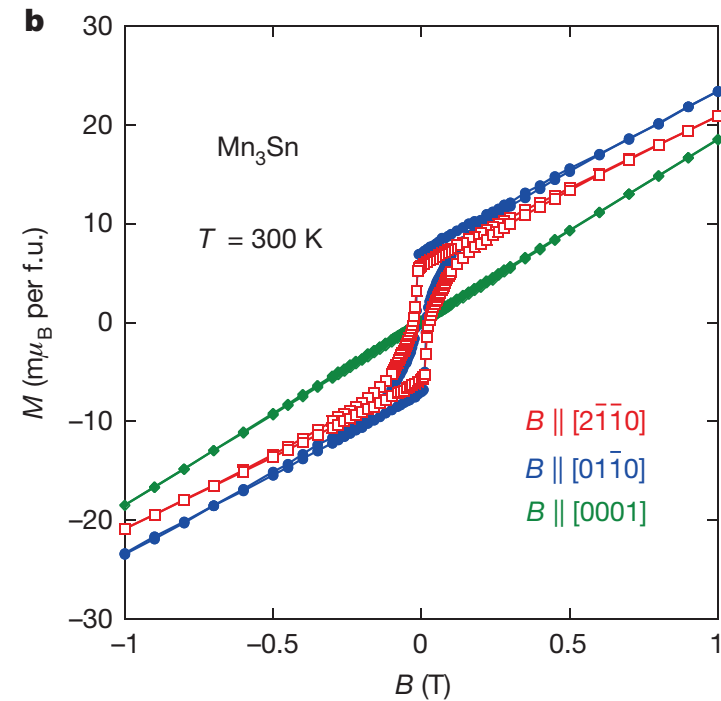
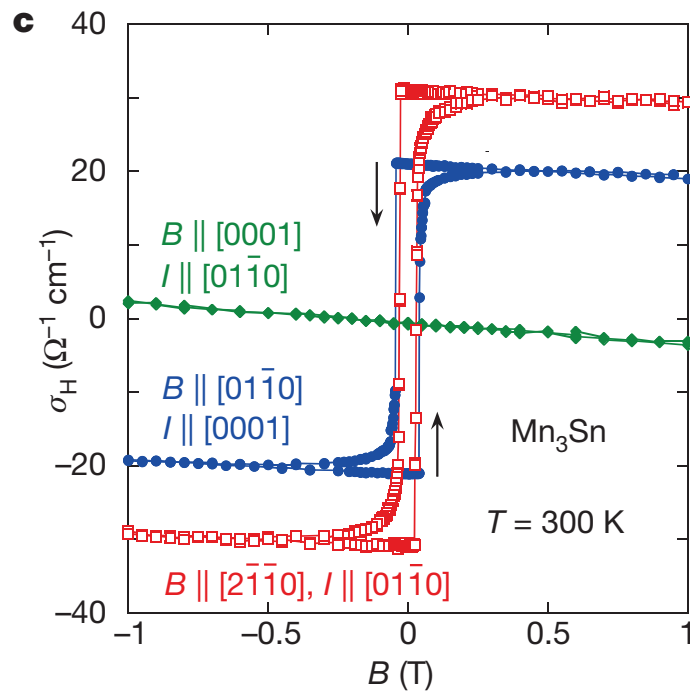
$\mathbf{\Omega}$  Determines plane of Hall effect



Spin configuration determines  $\mathbf{\Omega}$  through influence on electrons

Because *local* moments are not small, neither is  $\mathbf{\Omega}$

# AHE



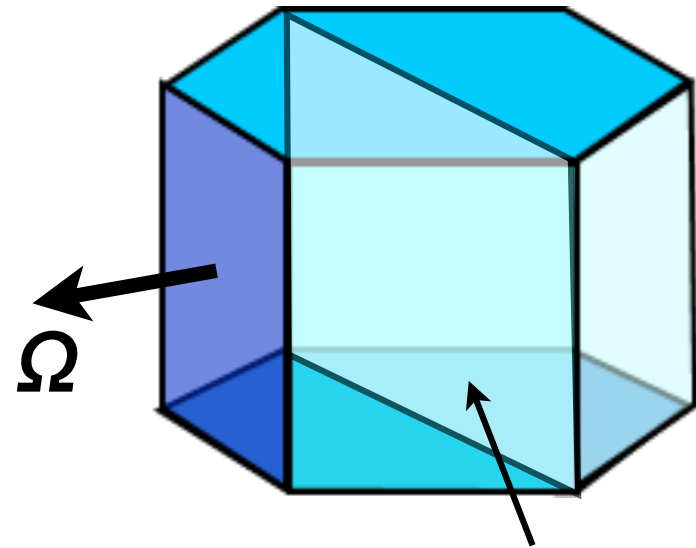
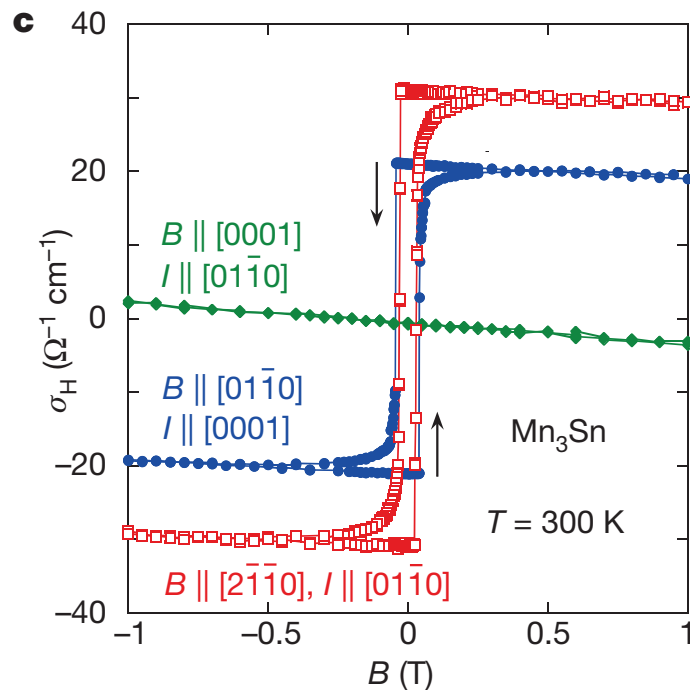
S. Nakatsuji *et al*, 2015

Why such a tiny moment?

Why such small coercive field?



# AHE

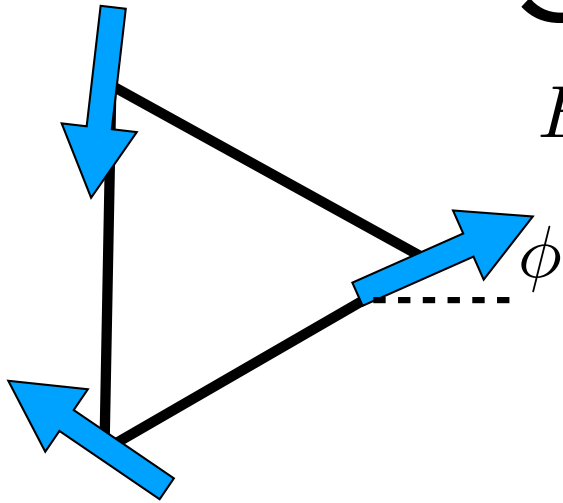


Hall effect in  
*vertical* plane

Why such a tiny moment?

For  $B > .2\text{T}$ , plane of the AHE follows the field

# Energetics: triangle



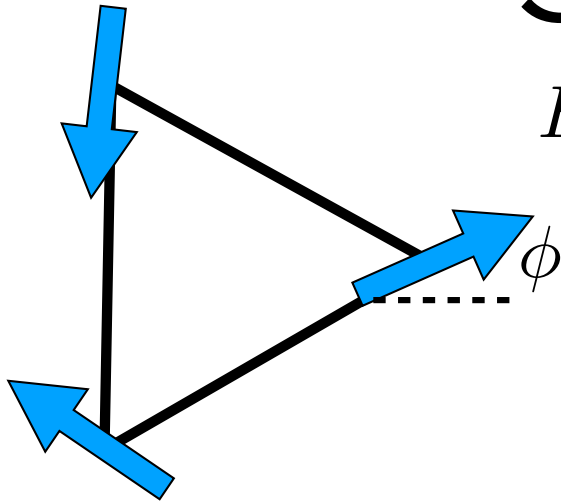
$$E = J (\mathbf{S}_1 \cdot \mathbf{S}_2 + \mathbf{S}_2 \cdot \mathbf{S}_3 + \mathbf{S}_3 \cdot \mathbf{S}_1) \\ + D \hat{\mathbf{z}} \cdot (\mathbf{S}_1 \times \mathbf{S}_2 + \mathbf{S}_2 \times \mathbf{S}_3 + \mathbf{S}_3 \times \mathbf{S}_1) \\ - K \sum_i (\hat{n}_i \cdot \mathbf{S}_i)^2$$

Jianpeng Liu + LB, 2017

$J \gg D \gg K$  **Hierarchy of interactions**

- J: spins at  $120^\circ$  angles and  $M=0$
- D: spins are “anti-chiral” in XY plane
- K: weak canting toward easy axes creates tiny moment, and even tinier preference for  $\phi$

# Energetics: triangle



$$E = J (\mathbf{S}_1 \cdot \mathbf{S}_2 + \mathbf{S}_2 \cdot \mathbf{S}_3 + \mathbf{S}_3 \cdot \mathbf{S}_1) \\ + D \hat{\mathbf{z}} \cdot (\mathbf{S}_1 \times \mathbf{S}_2 + \mathbf{S}_2 \times \mathbf{S}_3 + \mathbf{S}_3 \times \mathbf{S}_1) \\ - K \sum_i (\hat{\mathbf{n}}_i \cdot \mathbf{S}_i)^2$$

Jianpeng Liu + LB, 2017

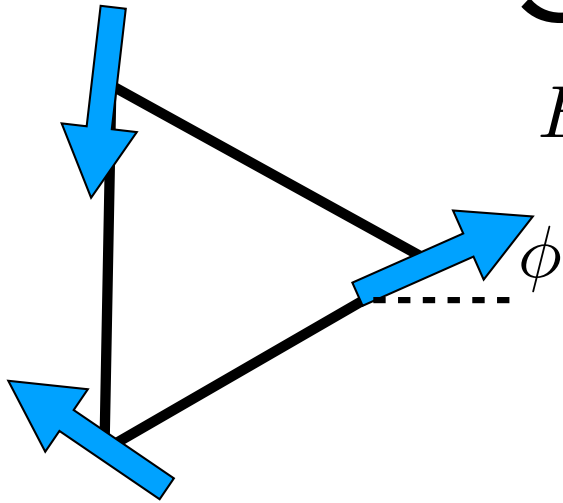
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Global symmetries:  
spin-space group

magnetic space group

# Energetics: triangle



$$E = J (\mathbf{S}_1 \cdot \mathbf{S}_2 + \mathbf{S}_2 \cdot \mathbf{S}_3 + \mathbf{S}_3 \cdot \mathbf{S}_1)$$

$$+ D \hat{\mathbf{z}} \cdot (\mathbf{S}_1 \times \mathbf{S}_2 + \mathbf{S}_2 \times \mathbf{S}_3 + \mathbf{S}_3 \times \mathbf{S}_1)$$

$$- K \sum_i (\hat{\mathbf{n}}_i \cdot \mathbf{S}_i)^2$$

Jianpeng Liu + LB, 2017

$J \gg D \gg K$  **Hierarchy of interactions**

$$m_0 = \frac{K}{J} m_s$$

Uniform moment

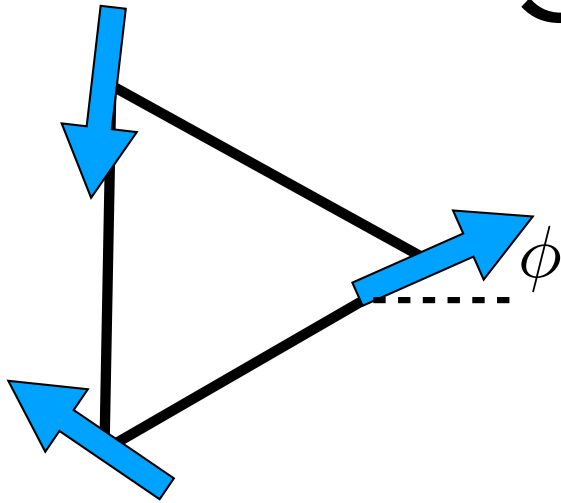
$$\lambda = \frac{K^3}{12J^2}$$

In-plane anisotropy

Low coercive field  
despite tiny Zeeman  
energy



# Energetics: triangle



$$\Omega = |\Omega| \begin{pmatrix} \cos \phi \\ -\sin \phi \\ 0 \end{pmatrix}$$

Jianpeng Liu + LB, 2017

$J \gg D \gg K$  **Hierarchy of interactions**

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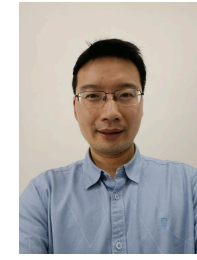
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# Torque



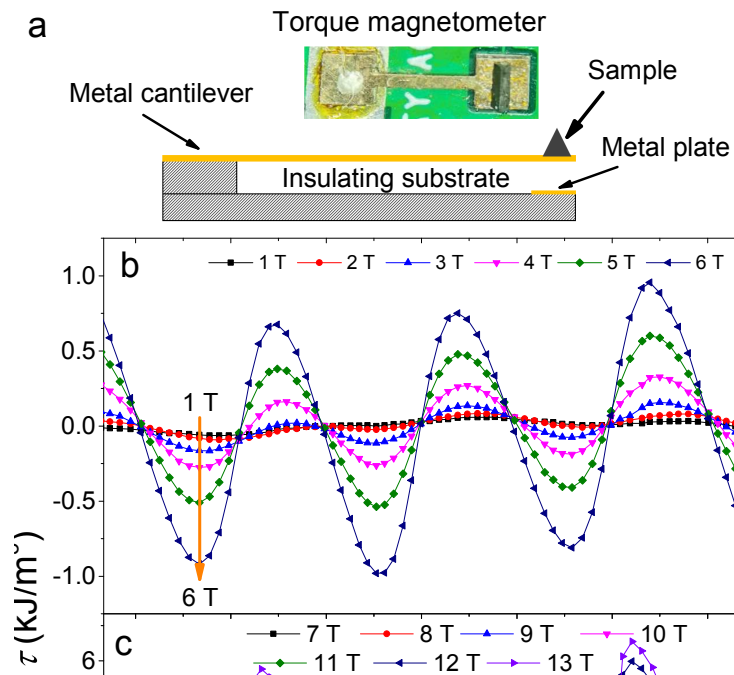
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Xiaokang Li  
Wuhan



$$\boldsymbol{\tau} = \boldsymbol{M} \times \boldsymbol{B}$$

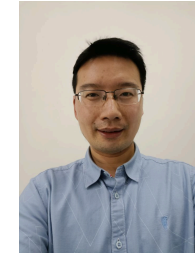
Tracks *mis*-alignment of  $\boldsymbol{M}$  with  $\boldsymbol{B}$ .

Total  $\boldsymbol{M}$  results from twists that spoil cancellation of antiferromagnetically aligned spins.

# Torque



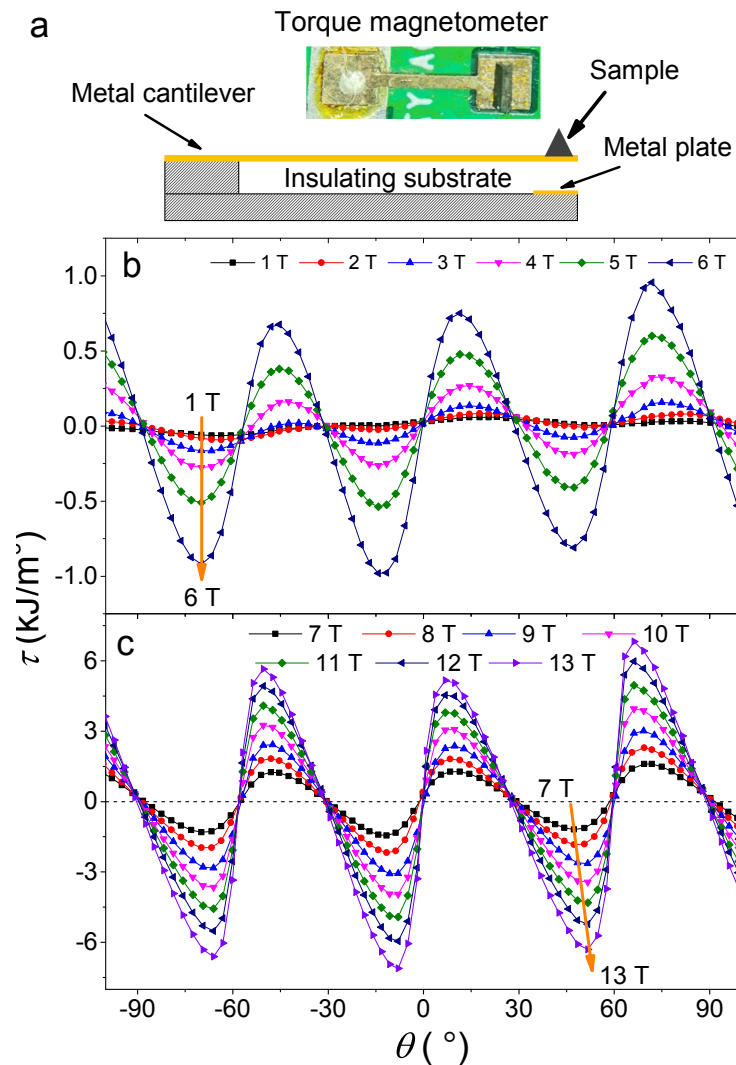
Kamran Behnia  
ESPCI



Zengwei Zhu  
Wuhan



Xiaokang Li  
Wuhan



## The free energy of twisting spins in Mn<sub>3</sub>Sn

Xiaokang Li<sup>1,\*</sup>, Shan Jiang<sup>3,1</sup>, Qingkai Meng<sup>1</sup>, Huakun Zuo<sup>1</sup>, Zengwei Zhu<sup>1,\*</sup>, Leon Balents<sup>2,4</sup> and Kamran Behnia<sup>3</sup>

(1) Wuhan National High Magnetic Field Center and School of Physics,  
Huazhong University of Science and Technology, Wuhan 430074, China

(2) Kavli Institute for Theoretical Physics, University of California, Santa Barbara, California 93106-4030, USA

(3) Laboratoire de Physique et d'Étude des Matériaux

(ESPCI - CNRS - Sorbonne Université), PSL Research University, 75005 Paris, France

(4) Canadian Institute for Advanced Research, Toronto, Ontario, Canada

(Dated: February 25, 2022)

Notice the evolution from  
sinusoidal to sawtooth

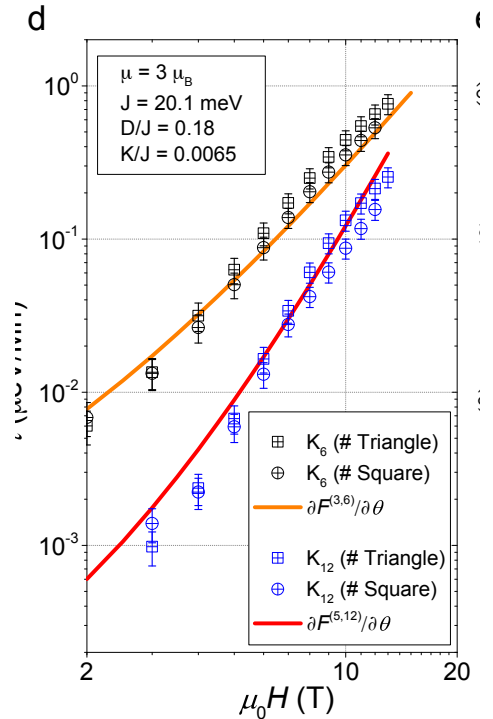
# First explanation

Extension of our expansion from 2017

$$\phi_1 = \phi + \eta_1, \quad \phi_2 = \phi - \frac{2\pi}{3} + \eta_2, \quad \phi_3 = \phi - \frac{4\pi}{3} - \eta_1 - \eta_2.$$

$$\eta_i = \sum_{n=1}^{\infty} \eta_{i,n} r^n, \quad E_{u.c.} = \sum_{n=0}^{\infty} E_{u.c.}^{(n)},$$

$$\begin{aligned} E_{u.c.}^{(0)} &= -6J - 6\sqrt{3}D, \\ E_{u.c.}^{(1)} &= -3K, \\ E_{u.c.}^{(2)} &= -\frac{(\mu H)^2 + K^2 + 2\mu H K \cos(\theta + \phi)}{2(\sqrt{3}D + J)}, \\ E_{u.c.}^{(3)} &= -\frac{1}{36(J + \sqrt{3}D)^3} \left[ (3J + 7\sqrt{3}D)K^3 \cos(6\phi) + 6(J + 3\sqrt{3}D)\mu H K^2 \cos(5\phi - \theta) \right. \\ &\quad \left. + 3(J + 5\sqrt{3}D)(\mu H)^2 K \cos(4\phi - 2\theta) + 4\sqrt{3}D(\mu H)^3 \cos(3\phi - 3\theta) \right]. \end{aligned}$$



Perturbatively solve

$$\phi(\theta)$$

$$\begin{aligned} E_{u.c.} &= -6J - 6\sqrt{3}D - 3K - \frac{(\mu H + K)^2}{2(J + \sqrt{3}D)} \left[ 1 + \frac{(3J + 7\sqrt{3}D)K + 4\sqrt{3}D\mu H}{18(J + \sqrt{3}D)^2} \cos(6\theta) \right. \\ &\quad \left. + \frac{((3J + 7\sqrt{3}D)K^2 + 2(J + 4\sqrt{3}D)\mu H K + 2\sqrt{3}D(\mu H)^2)^2}{36(J + \sqrt{3}D)^4 \mu H K} \sin^2(6\theta) \right]. \end{aligned}$$



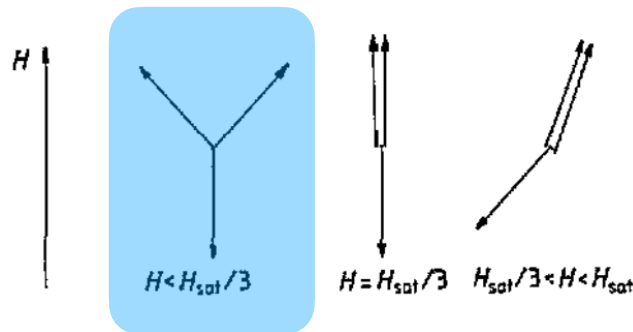
# Angular transitions

A little simpler picture

Heisenberg model

$$E_{\text{tri}} = \frac{J}{2} \left( \mathbf{S}_1 + \mathbf{S}_2 + \mathbf{S}_3 - \frac{1}{J} \mathbf{h} \right)^2$$

“Order by disorder”: thermal and quantum fluctuations favor coplanar states



**Figure 1.** Reorientation process in the magnetic field in 2D Heisenberg AFM on a triangular lattice. Zero-point fluctuations stabilize the collinear phase in the finite region  $H_1 < H < H_2$  in the vicinity of  $H_{\text{sat}}/3$ .

A. Chubukov and I. Golosov, 1991

# Experiments

PHYSICAL REVIEW B **92**, 014414 (2015)

## Magnetic phase diagram of $\text{Ba}_3\text{CoSb}_2\text{O}_9$ as determined by ultrasound velocity measurements

G. Quirion,<sup>\*</sup> M. Lapointe-Major, M. Poirier, and J. A. Quilliam

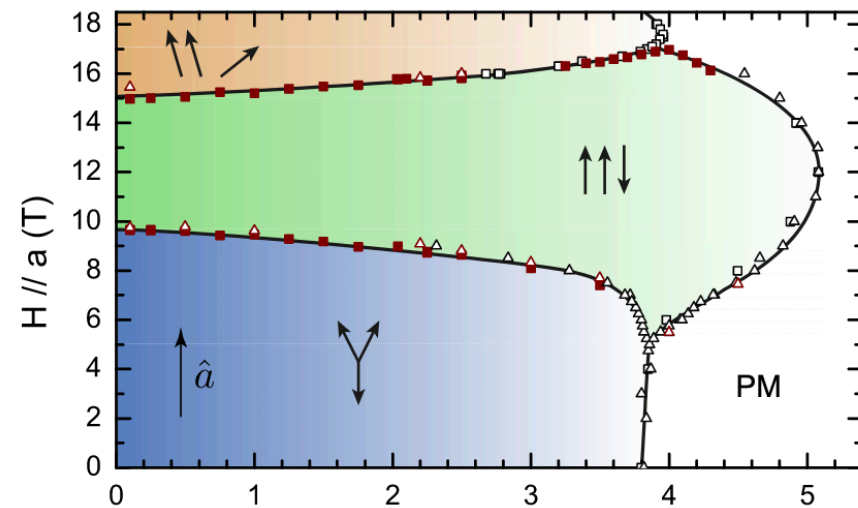
*Département de Physique, Université de Sherbrooke, Sherbrooke, Québec, Canada J1K 2R1*

Z. L. Dun and H. D. Zhou

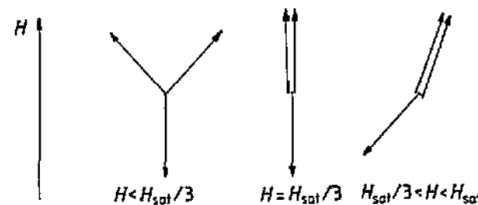
*Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee, 37996-1200, USA*

(Received 8 April 2015; revised manuscript received 26 May 2015; published 13 July 2015)

Numerous examples  
amongst insulating  
anti-ferromagnets



c.f.



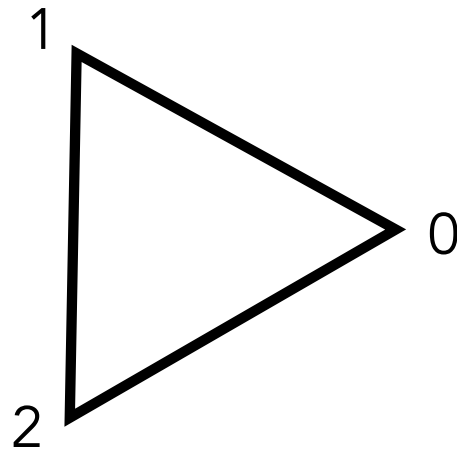
**Figure 1.** Reorientation process in the magnetic field in 2D Heisenberg AFM on a triangular lattice. Zero-point fluctuations stabilize the collinear phase in the finite region  $H_1 < H < H_2$  in the vicinity of  $H_{\text{sat}}/3$ .

# Energy and symmetries: Heisenberg limit

$$\langle S_n \rangle = \text{Re} \left[ d e^{\frac{2\pi i n}{3}} \right]$$

$$d \cdot d = 0.$$

$$d = u + iv$$



$$\text{SO}(3) \quad S_n \rightarrow OS_n$$

$$S_3 \quad S_n \rightarrow S_{P(n)}$$

$$F_h^{\text{iso}} = c_1 |\mathbf{h} \cdot \mathbf{d}|^2 + c_2 \text{Re} \left[ (\mathbf{h} \cdot \mathbf{d})^3 \right] + O(h^4)$$

Selects plane

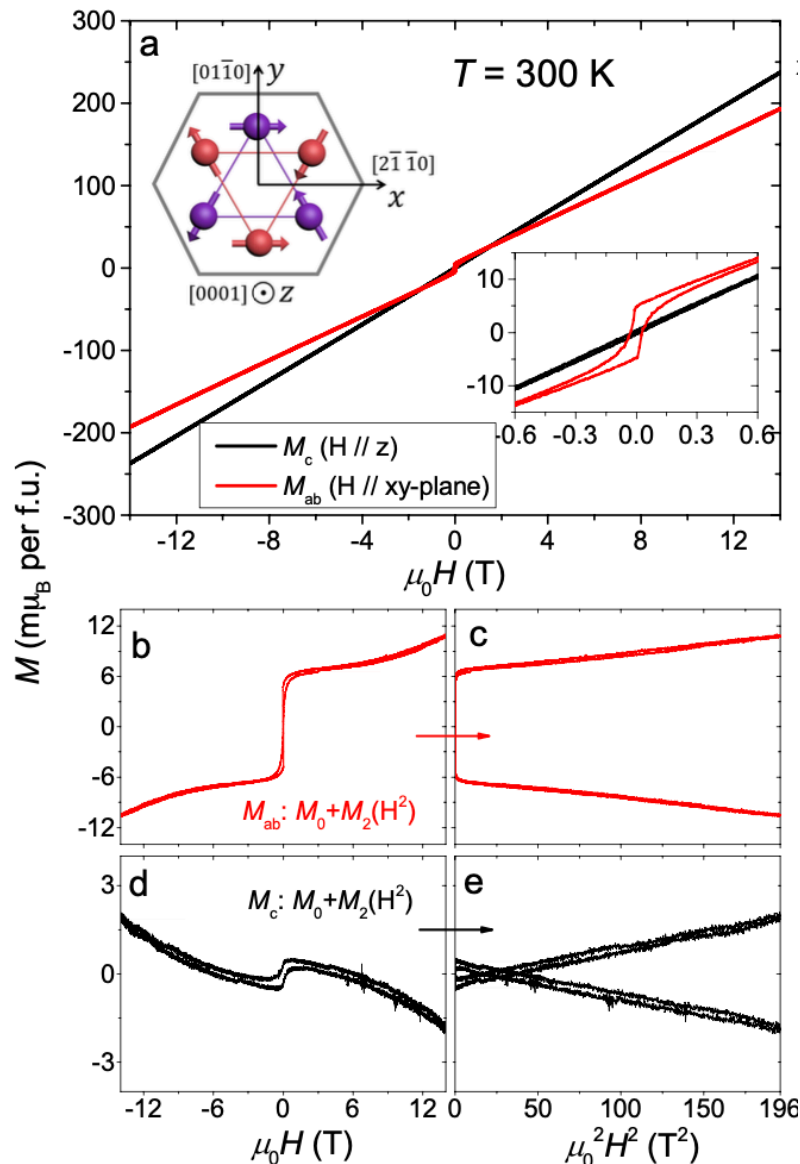
Selects angle in plane

$$c_1 < 0$$

$$c_2 > 0$$

Coefficients are "large": arise from  $J \gg D, K$

# Quadratic magnetization



Thermodynamics:

$$M = -\frac{\partial F}{\partial H}$$

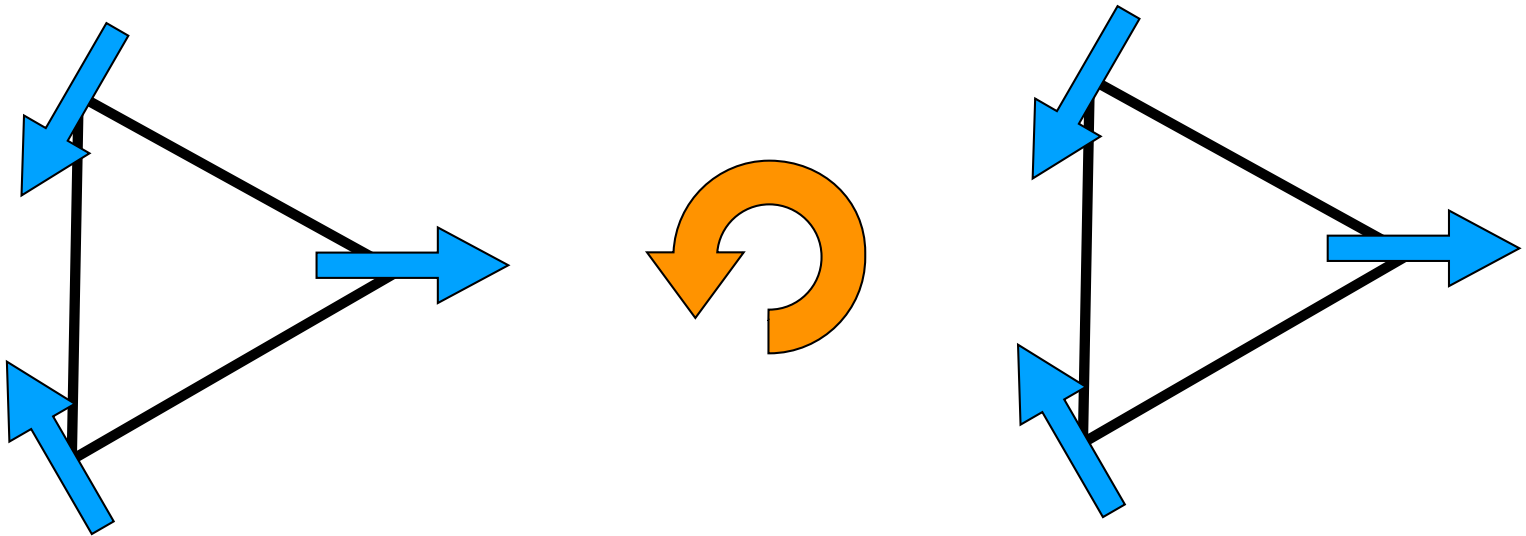
$$\sim c_1 H + c_2 H^2$$

Can directly see the energy responsible  
for order by disorder !



# Anti-chiral state

Favored by  $D > 0$      $d = d e^{i\phi} (\hat{x} + i\hat{y})$



counter-clockwise rigid rotation = clockwise spin rotation

$$d_{\pm} = d_x \pm i d_y \quad h_{\pm} = h_x \pm i h_y$$

$\text{Re}[h_+ d_+]$  is an invariant

# Full angular free energy

$$d_+ = ne^{i\phi}$$

$$d_- = d_z = 0$$

$$h_+ = he^{i\theta}$$

Zero field anisotropy  
(Negligible)

$$f_+ = -w \cos 6\phi - uh \cos(\phi + \theta) - vh^3 \cos 3(\phi - \theta)$$

Anti-chiral  
magnetization

Heisenberg  
response

$$u \sim \frac{K}{J}$$

# Full angular free energy

$$d_+ = ne^{i\phi}$$

$$d_- = d_z = 0$$

$$h_+ = he^{i\theta}$$

$$f_+ = -uh \cos(\phi + \theta) - vh^3 \cos 3(\phi - \theta)$$

Anti-chiral  
magnetization

Heisenberg  
response

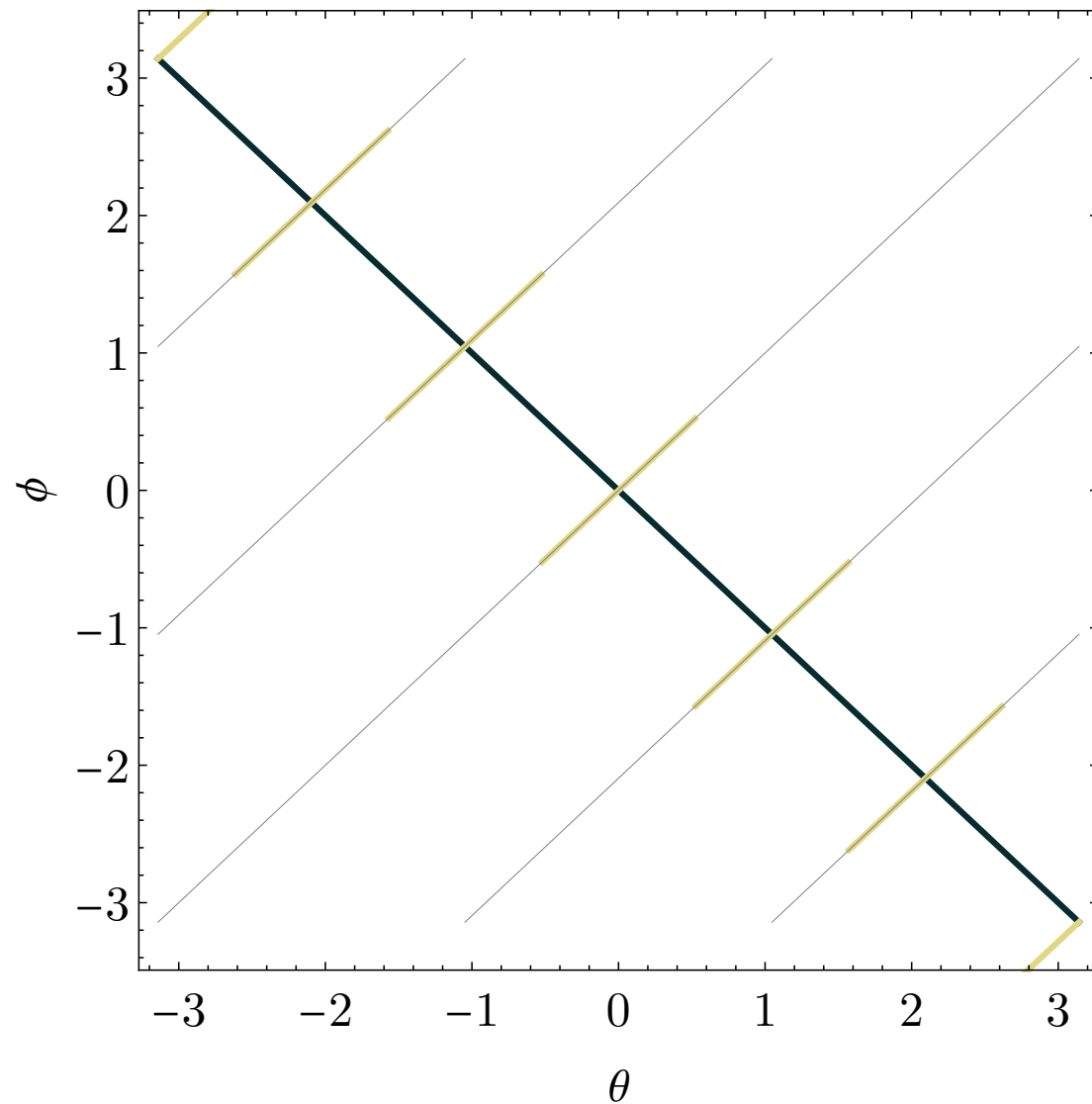
small  $h$ :

$$\phi \approx -\theta$$

large  $h$ :

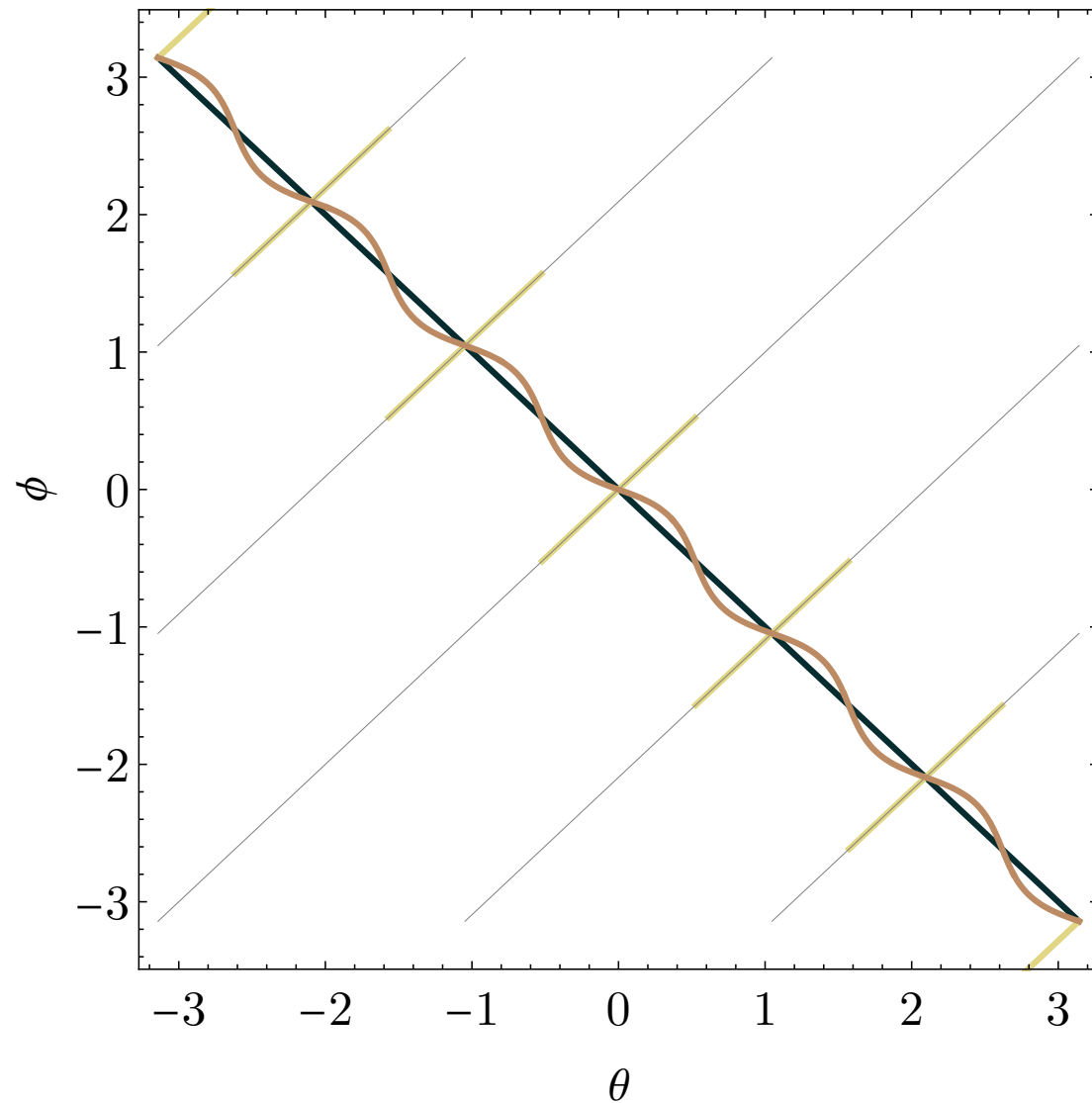
$$\phi \approx \theta + \frac{2\pi k}{3}$$

# Angular evolution

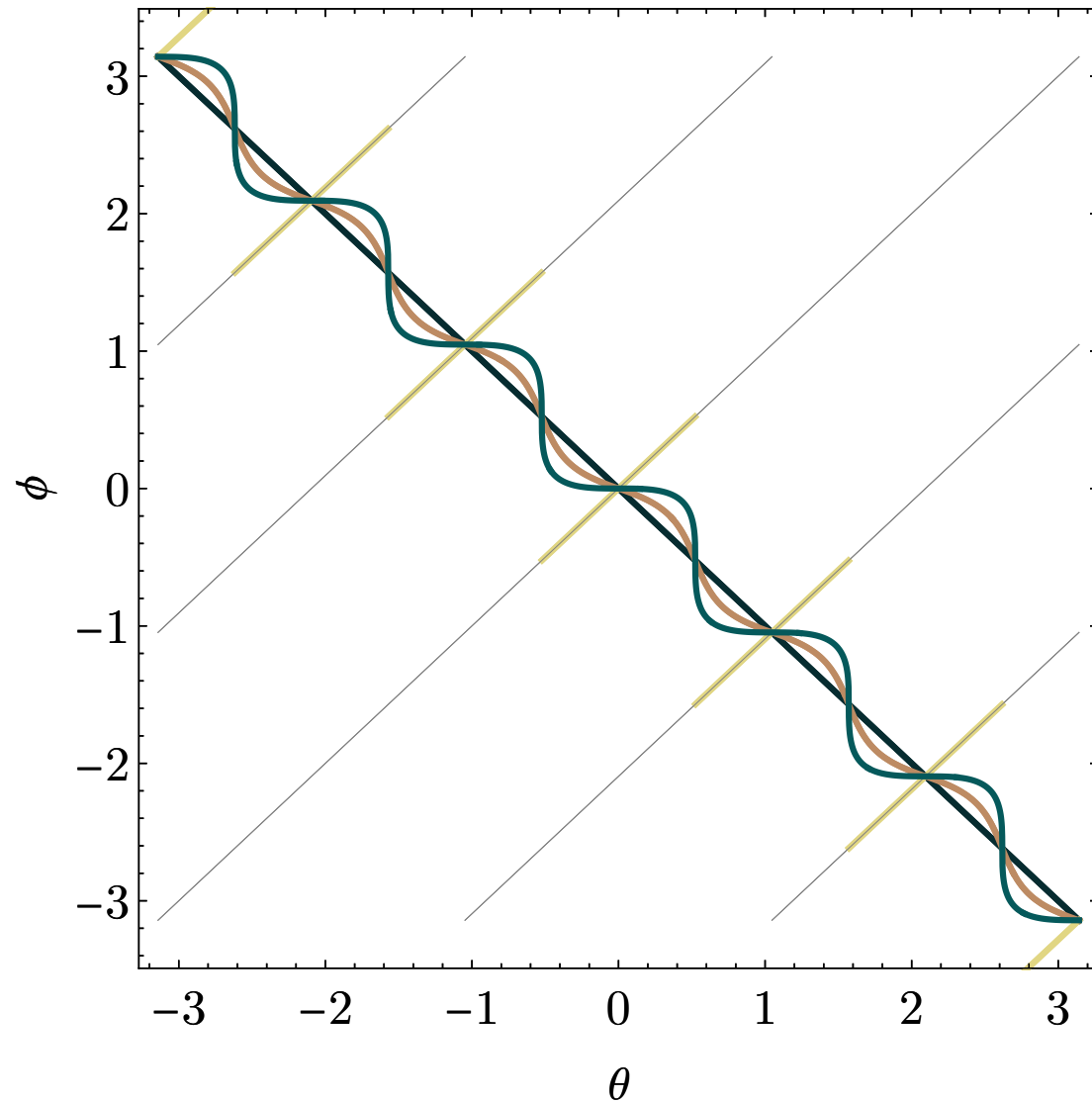




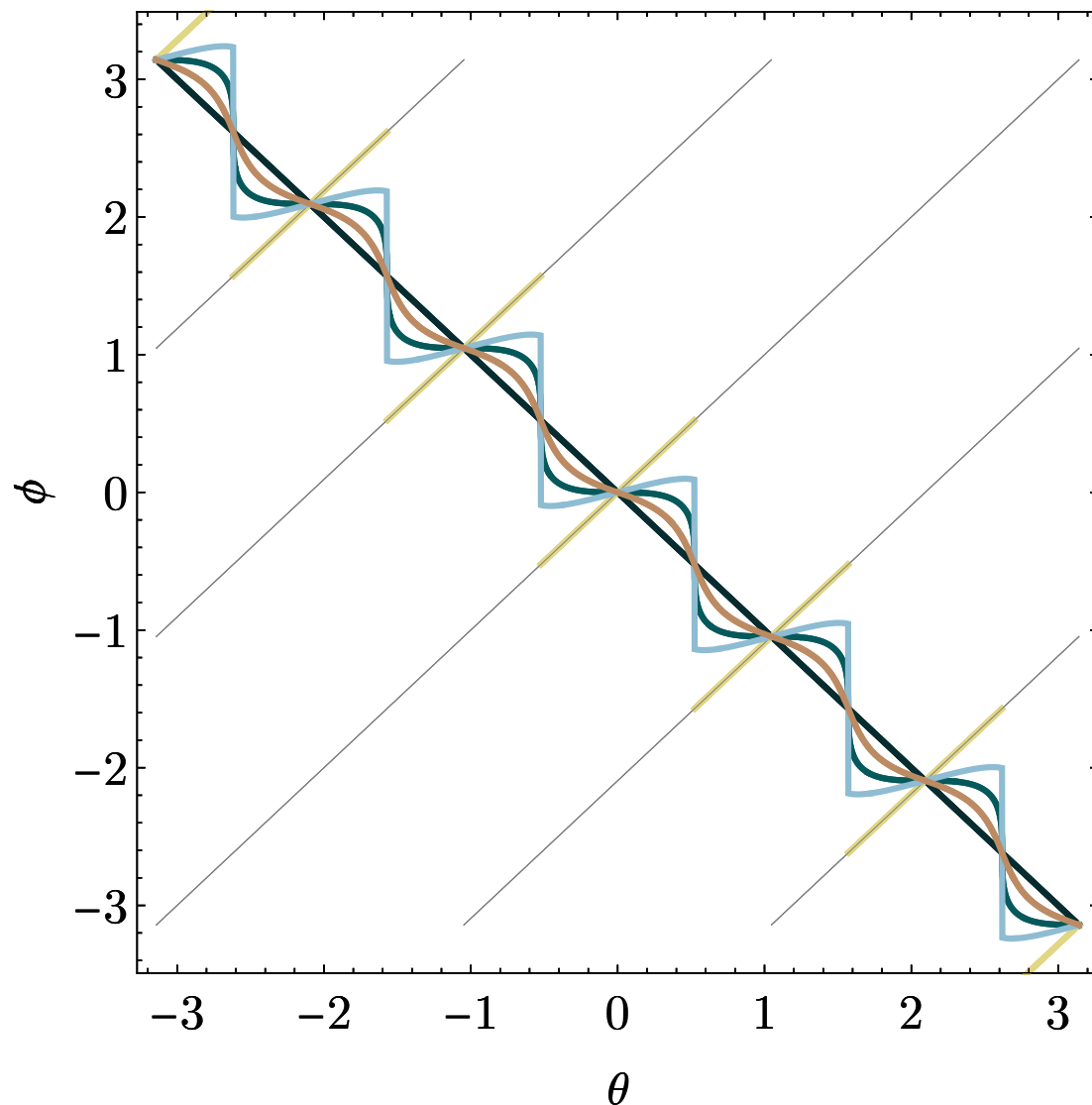
# Angular evolution



# Angular evolution



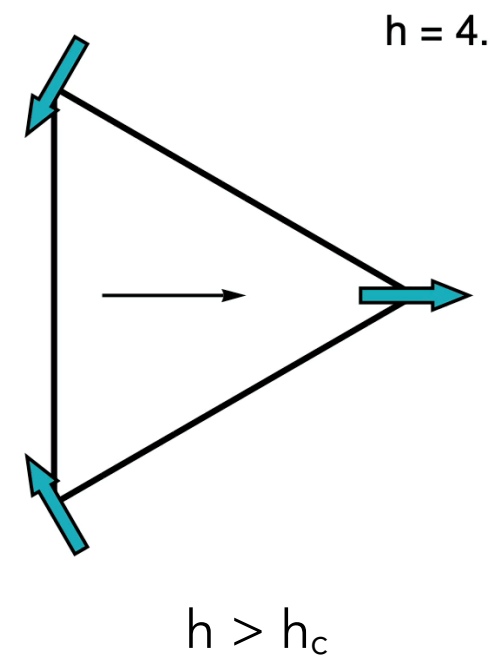
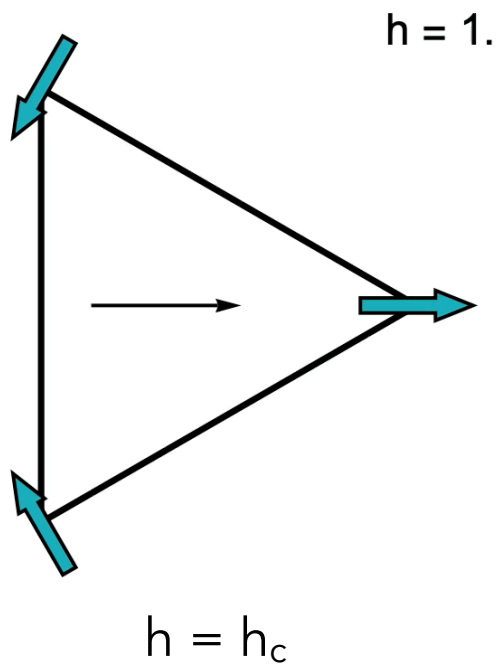
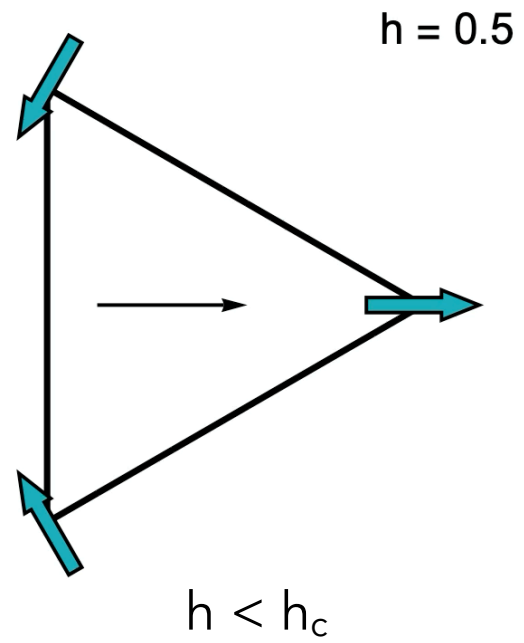
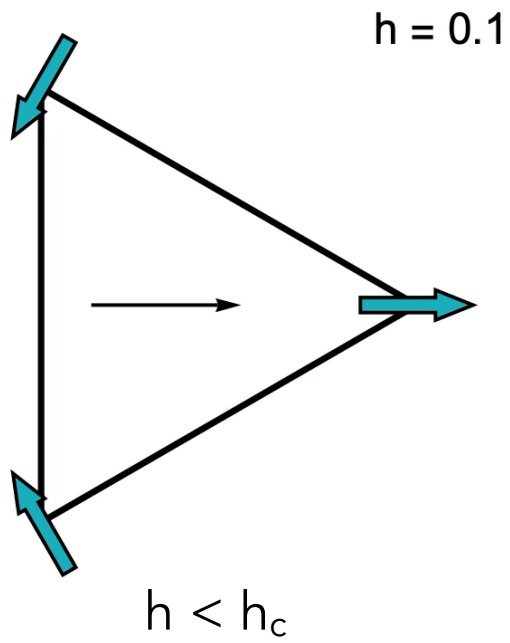
# Angular evolution



$$\theta = \frac{\pi}{6} + \frac{\pi m}{3}$$

$h > h_{\text{crit}}$   
 Jumps at  

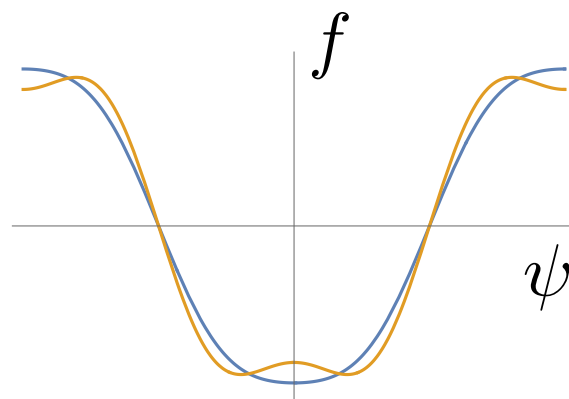
$$\theta = \frac{\pi}{6} + \frac{\pi m}{3}$$



# How do the jumps onset?

$$\psi = \phi + \theta, \quad \theta = \pi/6 + \delta \quad x = \sqrt{v/uh^2}$$

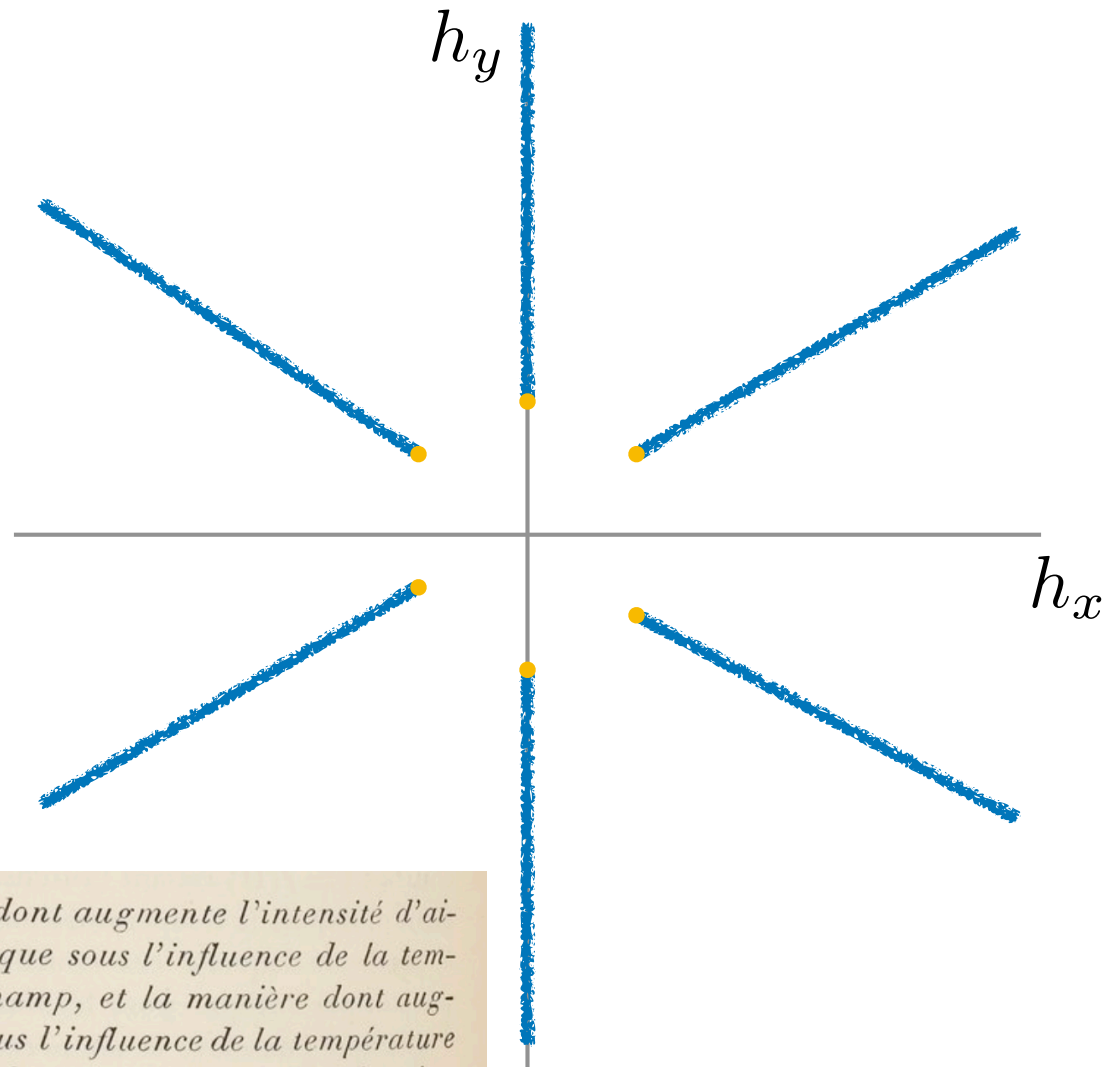
$$\begin{aligned} \frac{f}{uh} &= -\cos \psi + x \cos 6\delta \cos 3\psi + x \sin 6\delta \sin 3\psi \\ &= -\cos \psi + x \cos 3\psi \quad (\delta = 0) \end{aligned}$$



Ising transition  
at  $x=1/9$

$\delta$  acts as symmetry breaking field

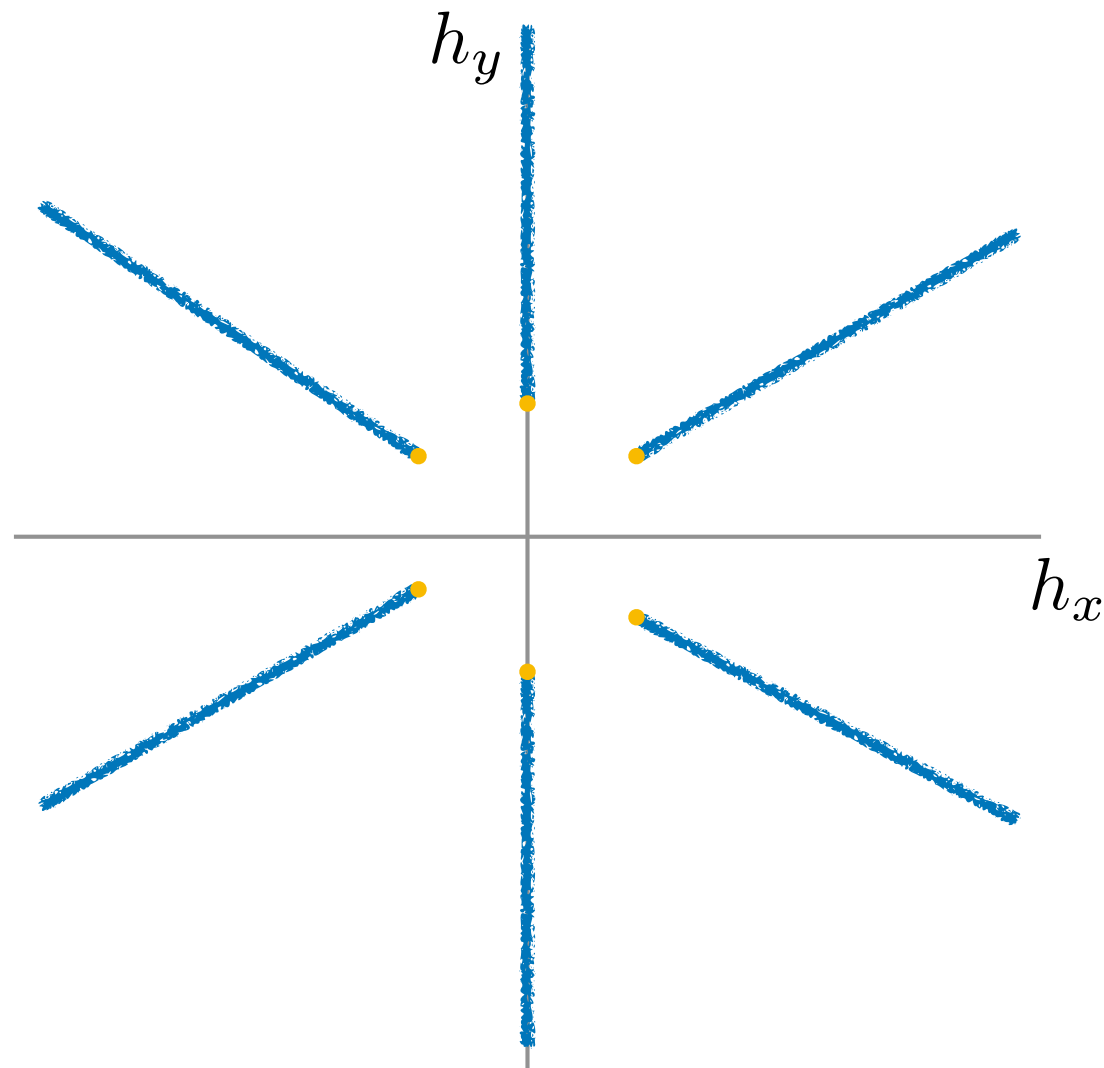
# Phase diagram



*Analogie entre la manière dont augmente l'intensité d'aimantation d'un corps magnétique sous l'influence de la température et de l'intensité du champ, et la manière dont augmente la densité d'un fluide sous l'influence de la température et de la pression. — Il y a des analogies entre la fonction  $f(I, H, T)=0$  relative à un corps magnétique et la fonction  $f(D, p, T)=0$  relative à un fluide. L'intensité d'aimantation  $I$*

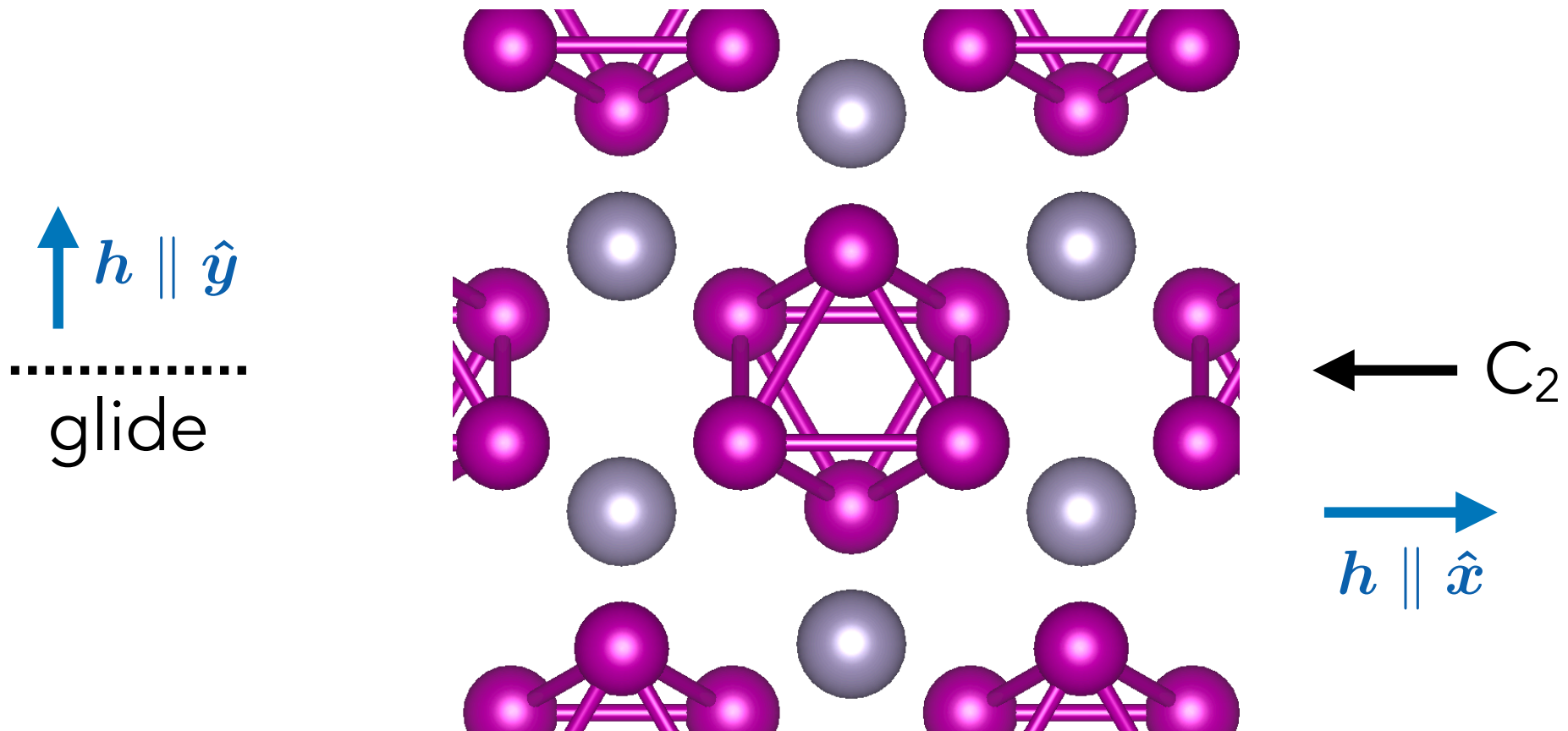


# Phase diagram

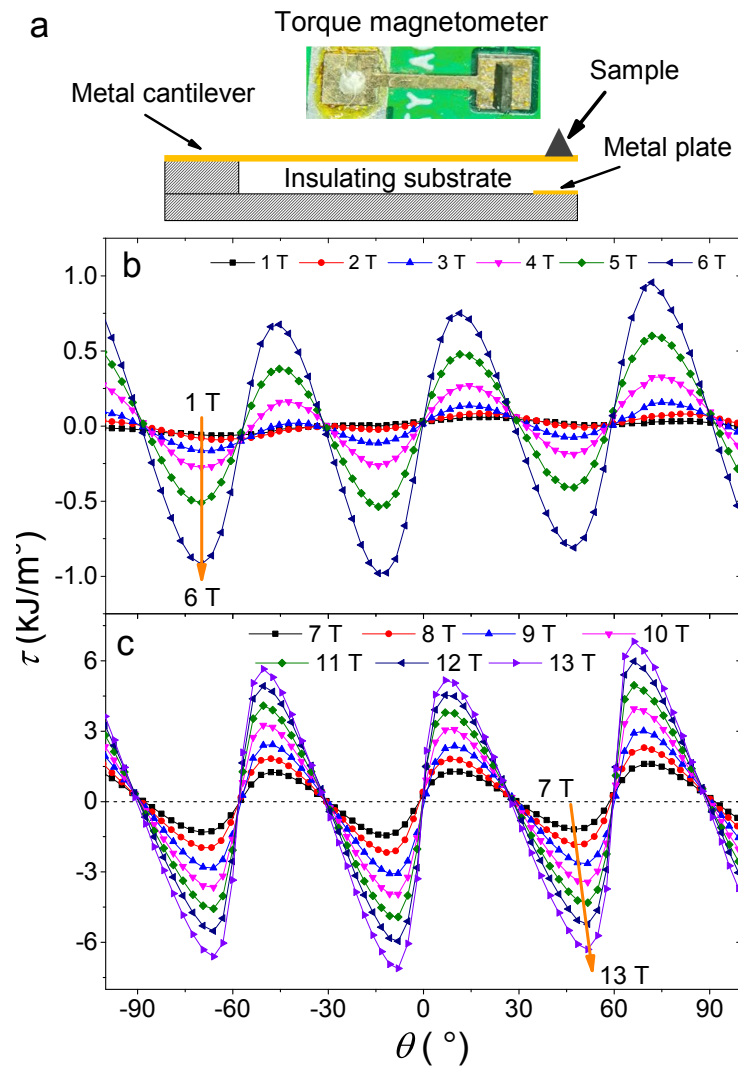


What symmetry is broken along the lines?

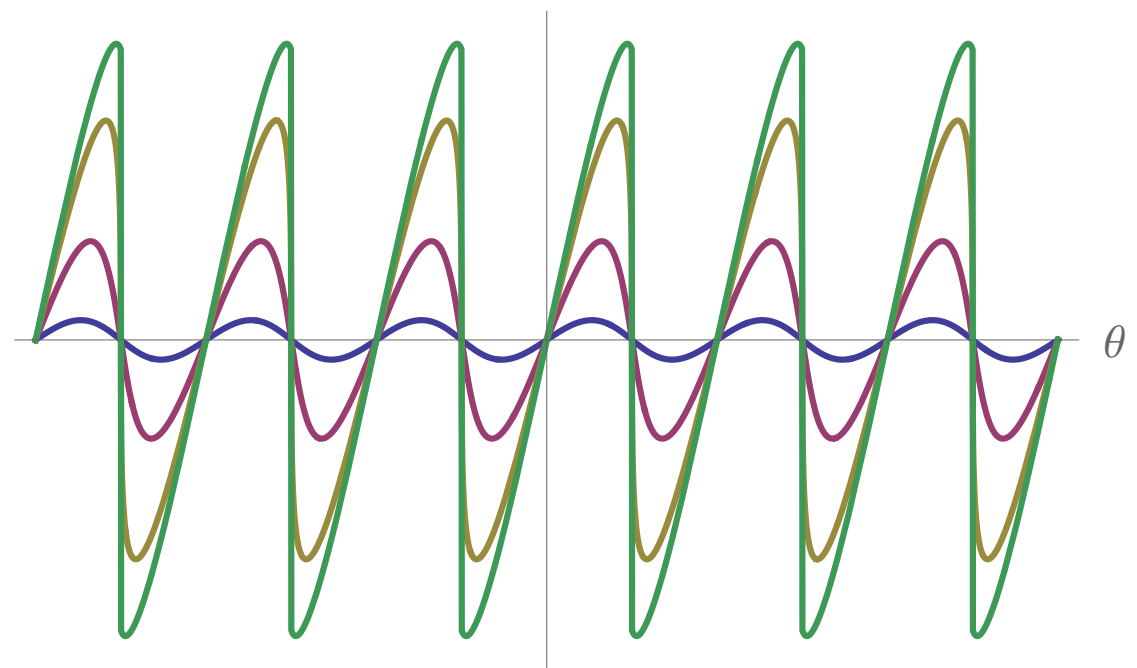
# Mn<sub>3</sub>Sn structure



# Torque

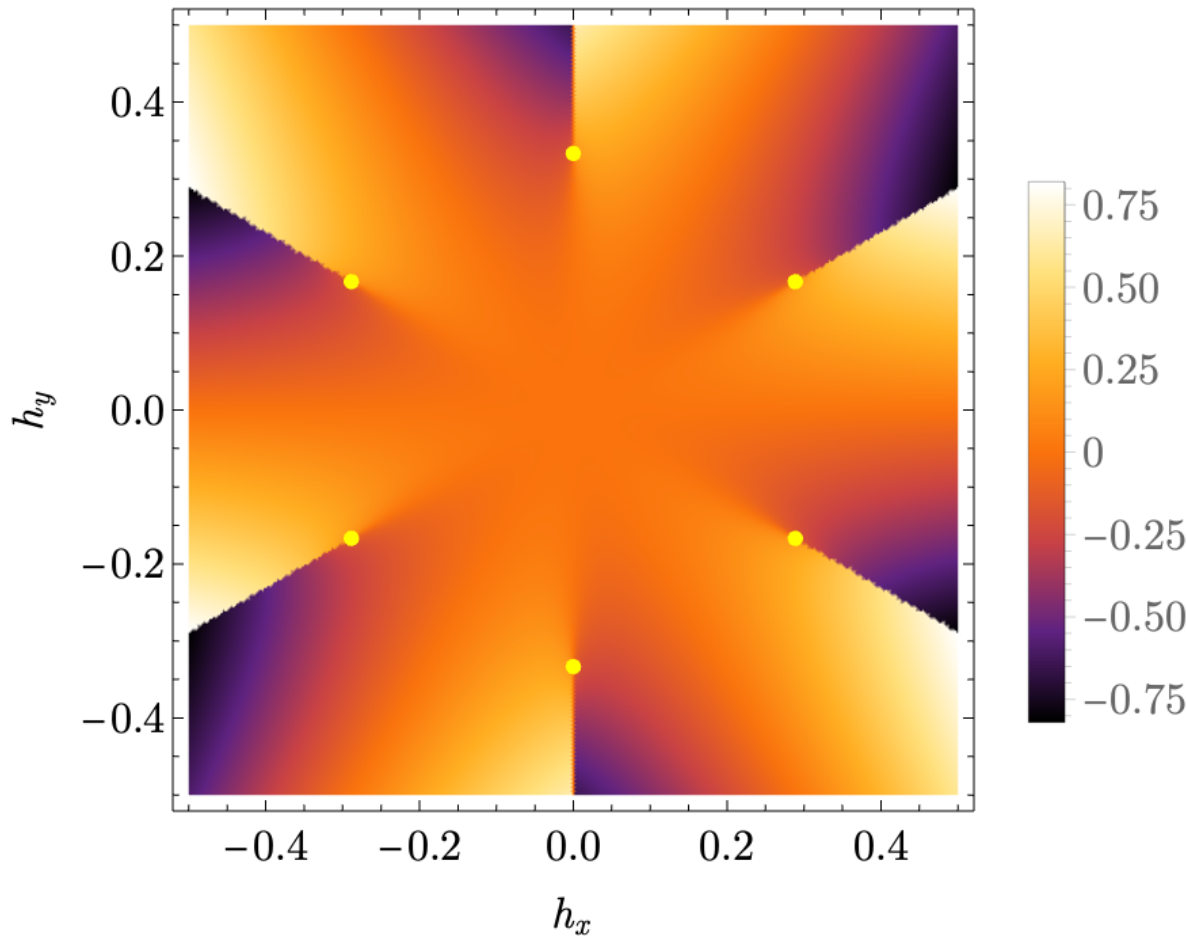


$$\tau = \frac{df}{d\theta}$$



Discontinuities for  $h > h_c$

# Estimate

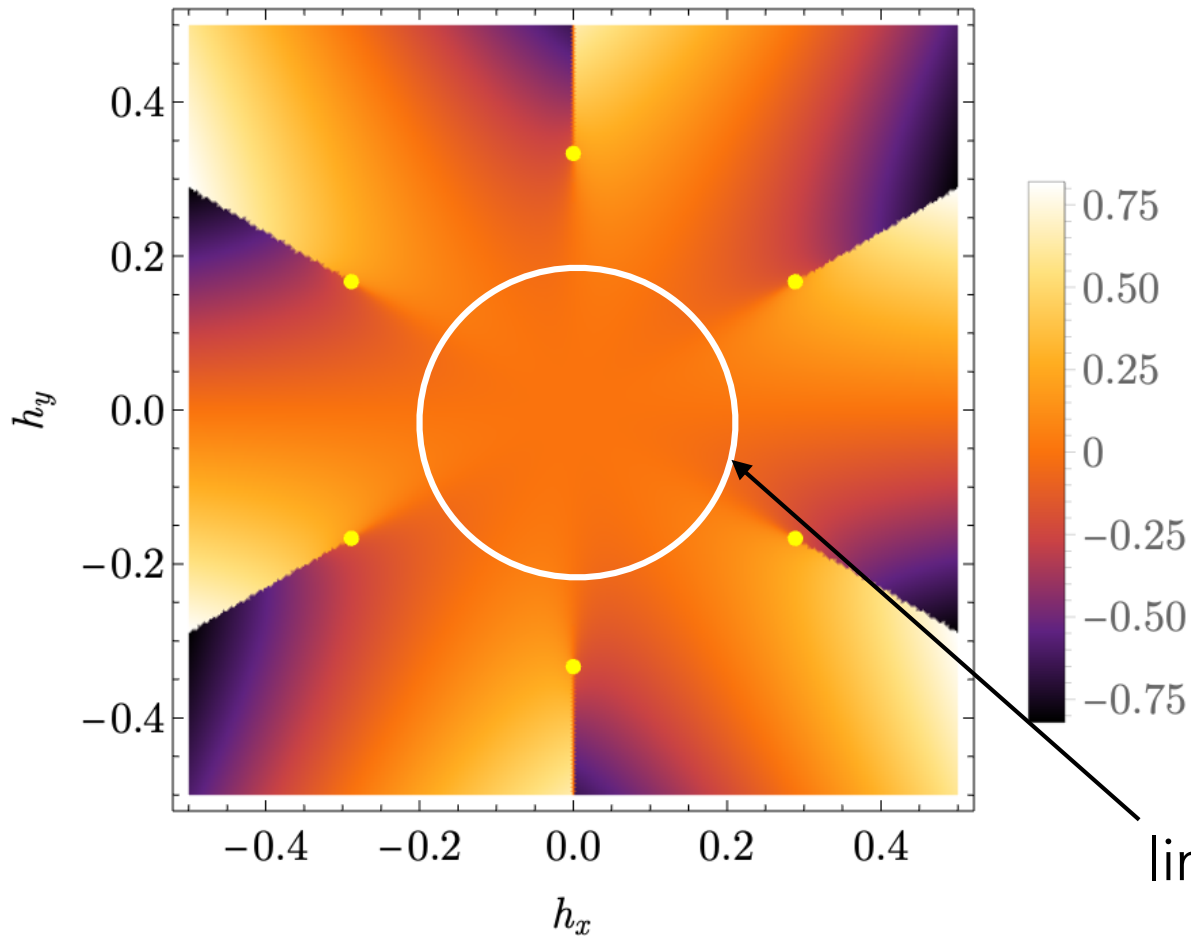


Classical,  $T=0$

$$H_c = \frac{J + \sqrt{3}D}{g\mu_B} \sqrt{\frac{K}{D}}$$

$$\approx 20T$$

# Estimate



Classical,  $T=0$

$$H_c = \frac{J + \sqrt{3}D}{g\mu_B} \sqrt{\frac{K}{D}}$$

$$\approx 20T$$

limit of current experiments

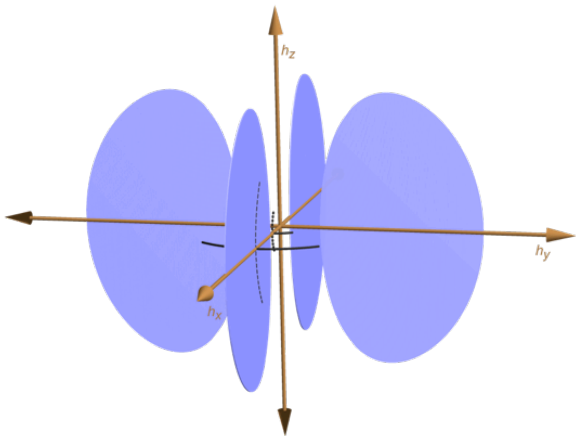
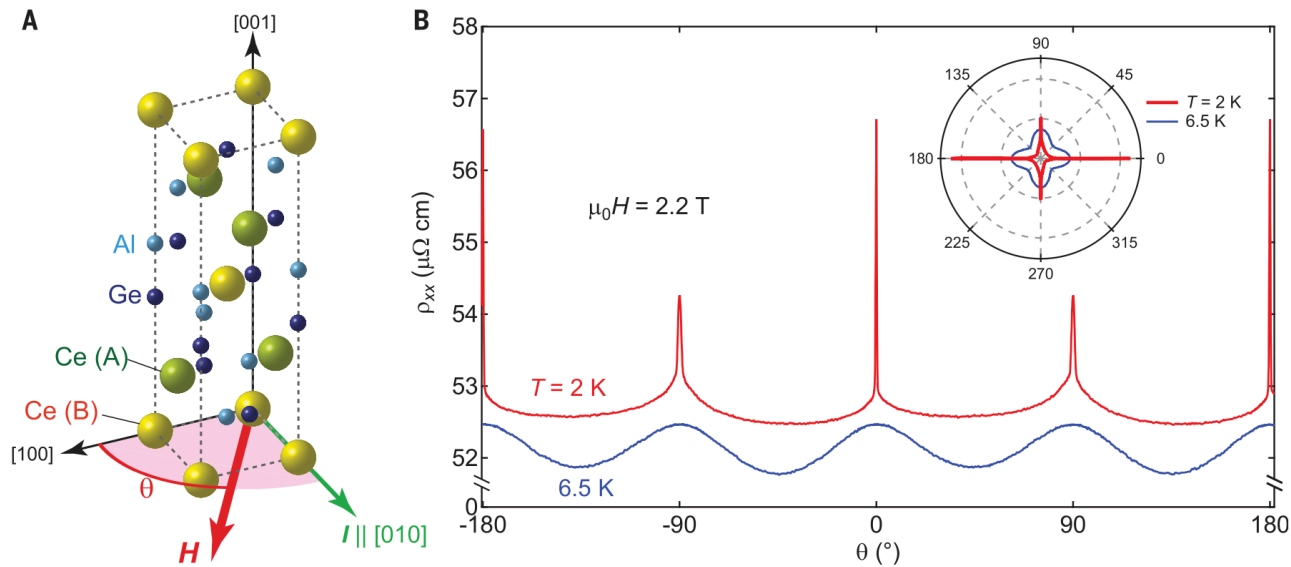
Hope to observe these transitions in future experiments

## MAGNETISM

c.f.

# Singular angular magnetoresistance in a magnetic nodal semimetal

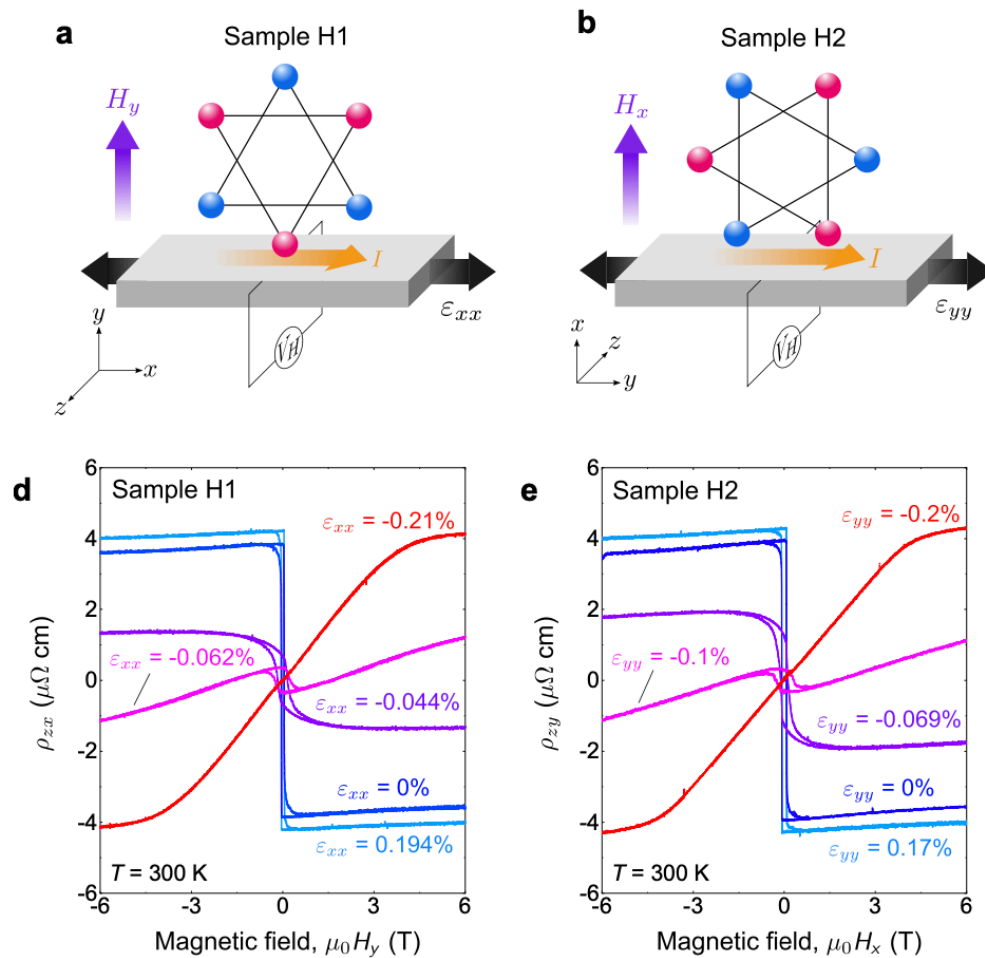
T. Suzuki<sup>1</sup>, L. Savary<sup>1,2,3</sup>, J.-P. Liu<sup>2,4</sup>, J. W. Lynn<sup>5</sup>, L. Balents<sup>2</sup>, J. G. Checkelsky<sup>1\*</sup>



Would be interesting to search for transport signatures in  $\text{Mn}_3\text{Sn}$



# Strain control



Strain also twists spins,  
allowing separate control  
of magnetization and Berry  
curvature

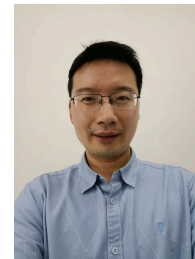
Ikhlas et al, arXiv:2206.00793 (2022)

# Outline

- Twisting spins in  $\text{Mn}_3\text{Sn}$  with a magnetic field
- Multiple energy scales enable control of anomalous Hall effect



Kamran Behnia  
ESPCI

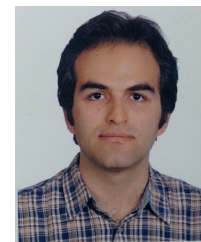


Zengwei Zhu  
Wuhan



Xiaokang Li  
Wuhan

- Twisting layers of spins in 2d materials
- Twists control new spin textures

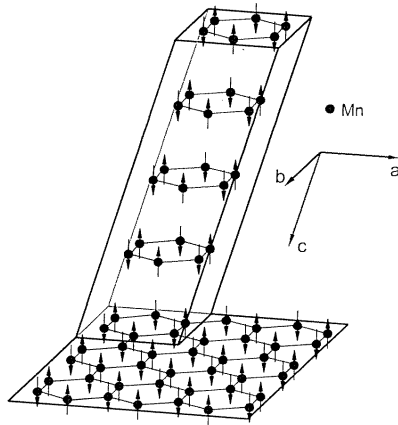


Kasra Hejazi  
Caltech



Zhu-Xi Luo  
UCSB

# 2d VdW magnets

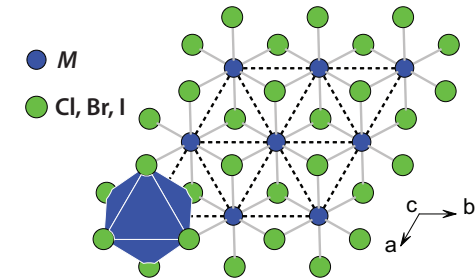


MnPS<sub>3</sub>, FePS<sub>3</sub>, NiPS<sub>3</sub>, CoPS<sub>3</sub>, CrSiTe<sub>3</sub>...

**MCl<sub>2</sub>**

Ti	V	Cr	Mn	Fe	Co	Ni
Zr	Nb	Mo	Tc	Ru	Rh	Pd
Hf	Ta	W	Re	Os	Ir	Pt

**MBr<sub>2</sub>**

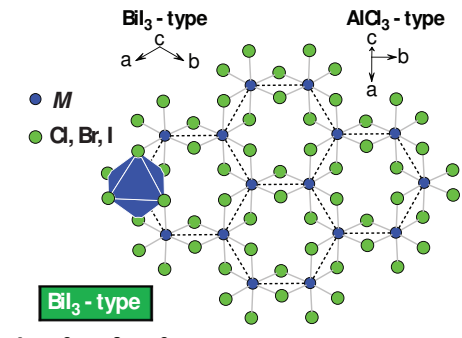


**MCl<sub>3</sub>**

Ti	V	Cr	Mn	Fe	Co	Ni
Zr	Nb	Mo	Tc	Ru	Rh	Pd
Hf	Ta	W	Re	Os	Ir	Pt

**MBr<sub>3</sub>**

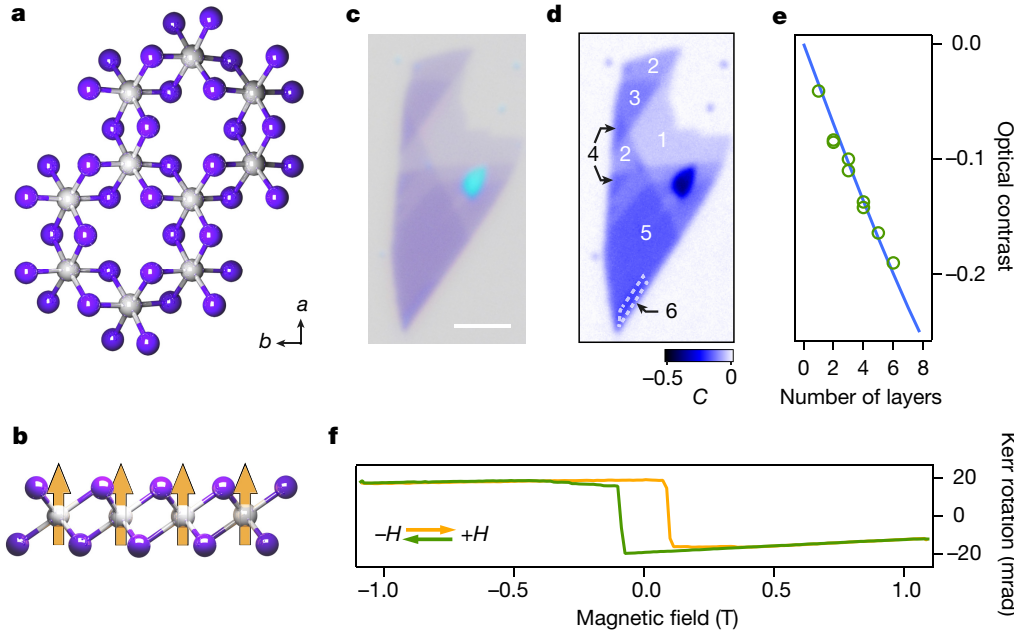
Ti	V	Cr	Mn	Fe	Co	Ni
----	---	----	----	----	----	----



CrI<sub>3</sub>, RuCl<sub>3</sub>, ...

# CrI<sub>3</sub>

B. Huang *et al*, 2017



Ferromagnetic 2d  
honeycomb layers

Optical measurement  
of magnetization

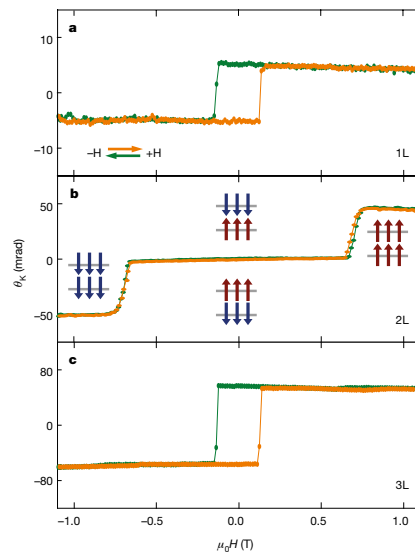
1L

Still ferromagnetic in single layer

2L

Surprise: bilayer is anti-ferromagnetic

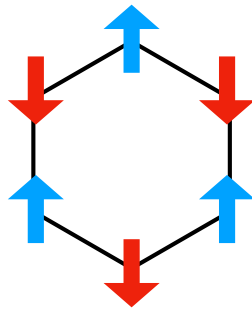
3L



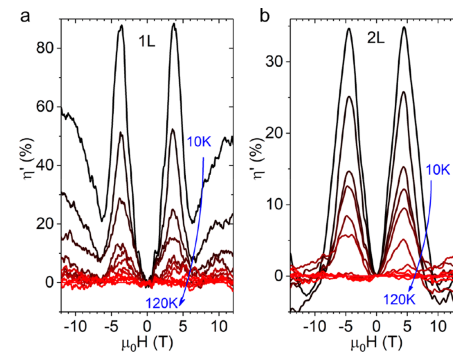
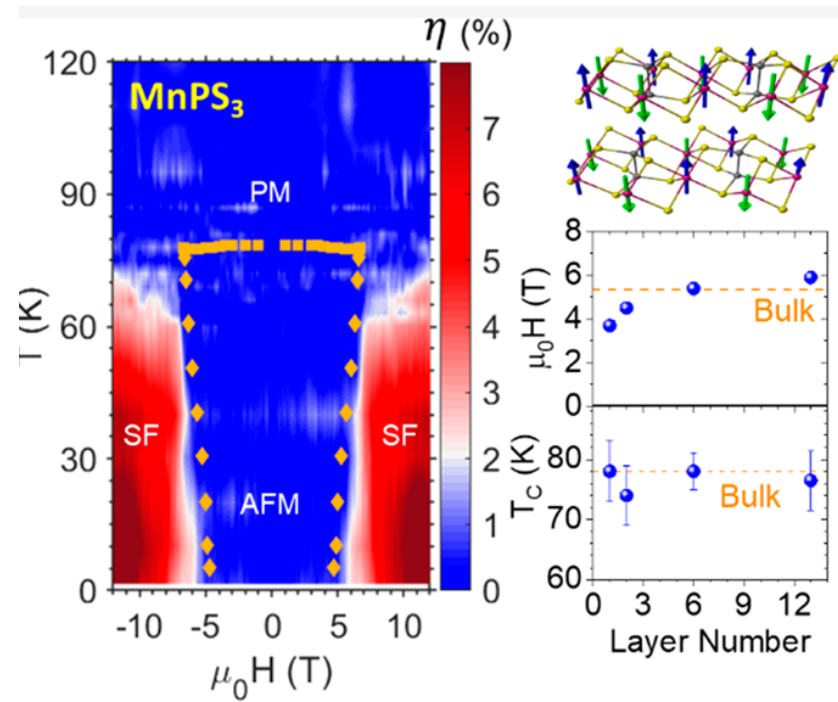
# MnPS<sub>3</sub>

G. Long et al, 2020

antiferromagnetic  
honeycomb



order persists to single layer



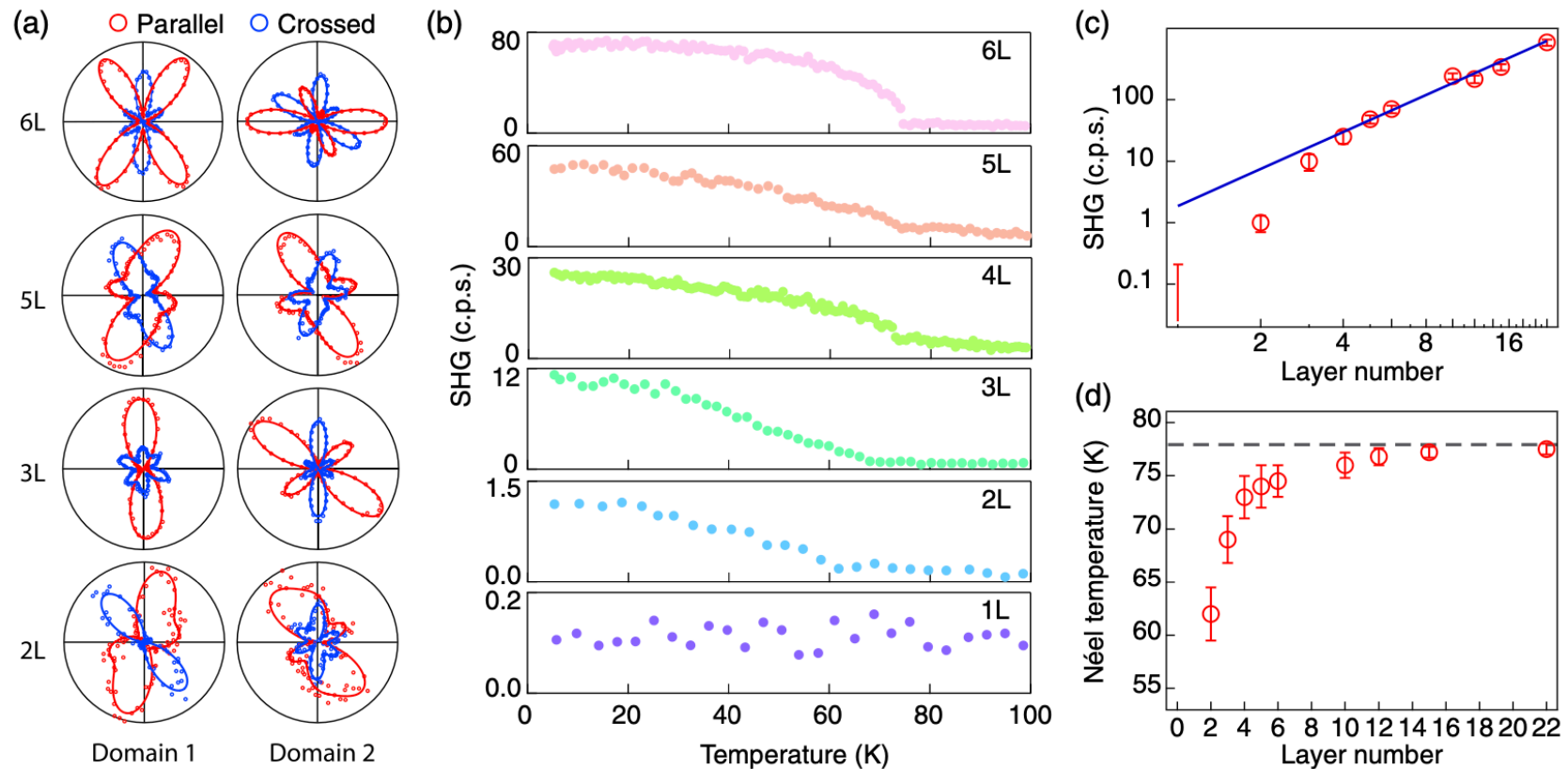
tunneling MR

# MnPS<sub>3</sub>

## Direct Imaging of Antiferromagnetic Domains and Anomalous Layer-Dependent Mirror Symmetry Breaking in Atomically Thin MnPS<sub>3</sub>

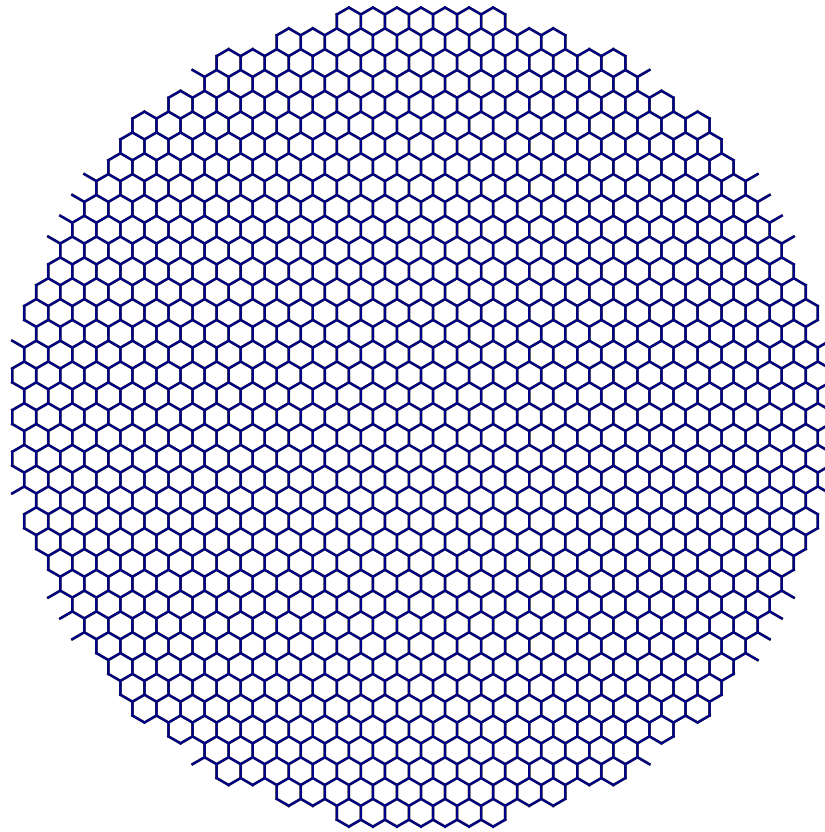
Zhuoliang Ni<sup>1</sup>, Huiqin Zhang,<sup>2</sup> David A. Hopper,<sup>2,1</sup> Amanda V. Haglund,<sup>3</sup> Nan Huang,<sup>3</sup> Deep Jariwala,<sup>2</sup> Lee C. Bassett,<sup>2</sup> David G. Mandrus,<sup>3,4</sup> Eugene J. Mele,<sup>1</sup> Charles L. Kane,<sup>1</sup> and Liang Wu<sup>1,\*</sup>

PHYSICAL REVIEW LETTERS **127**, 187201 (2021)





# Twisting and moiré



# Moiré



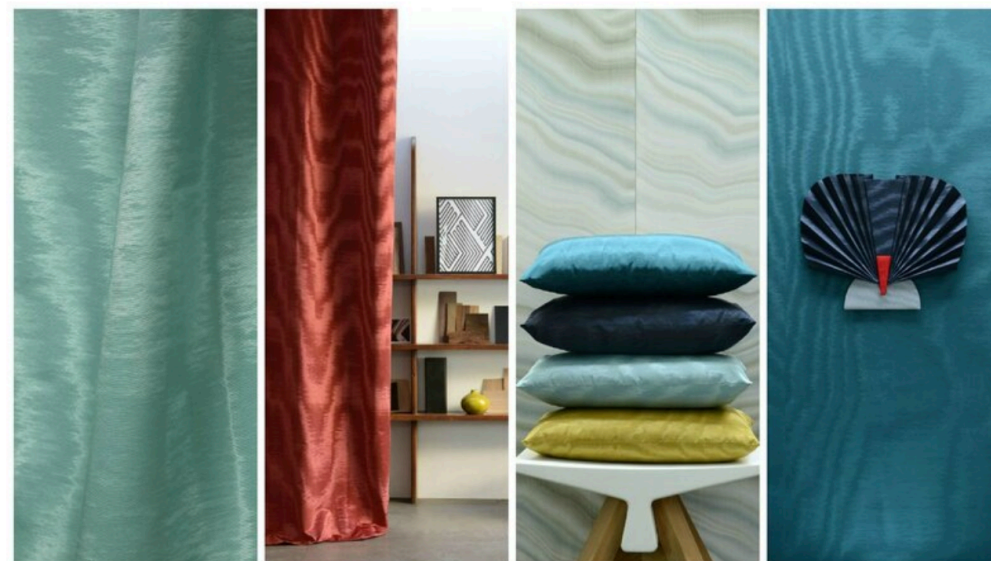
mohair

# Le retour de la moire



Le grand retour de la moire chez vous

La moire : Un tissu d'exception pour des murs, des rideaux et des meubles originaux



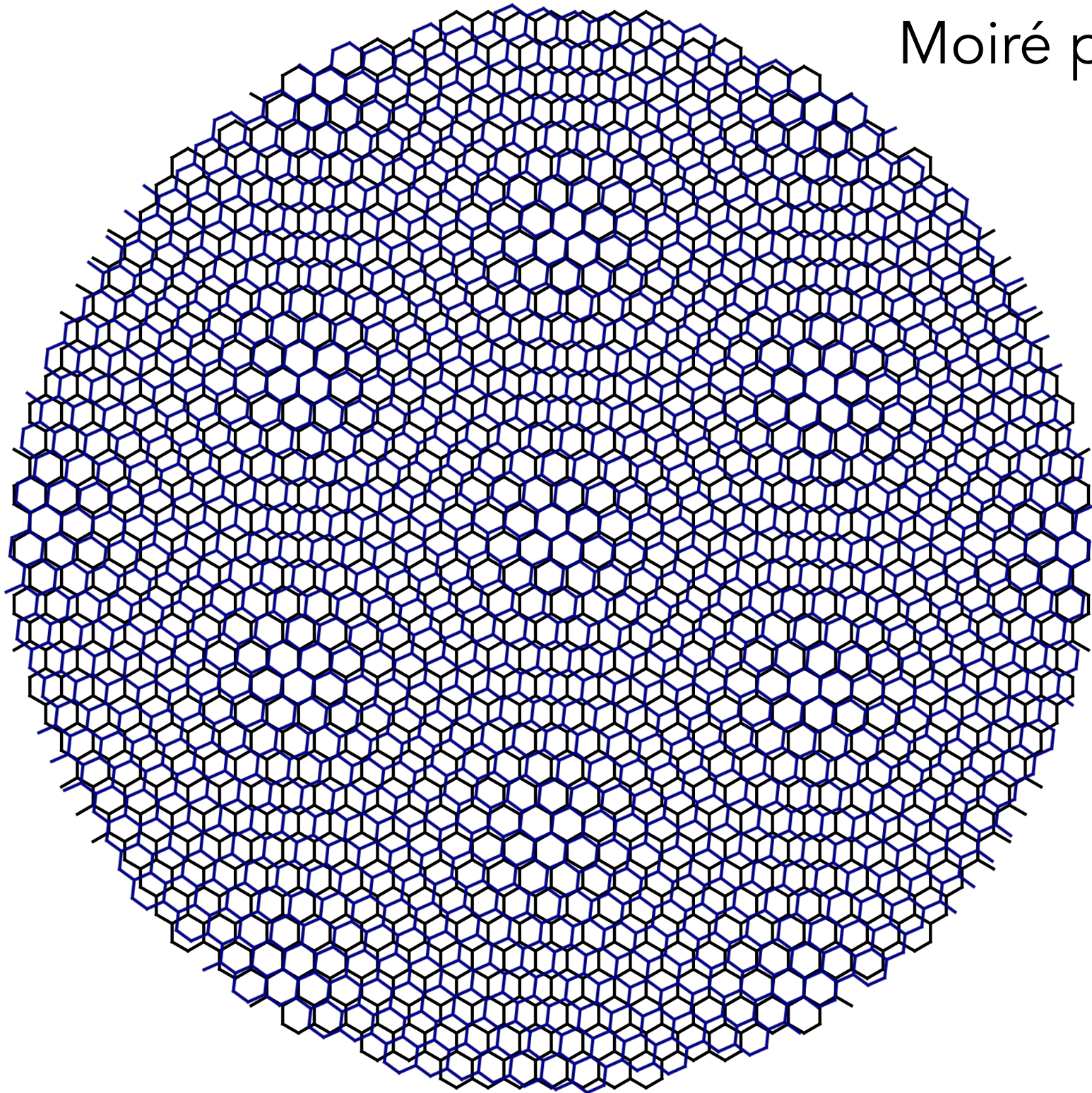






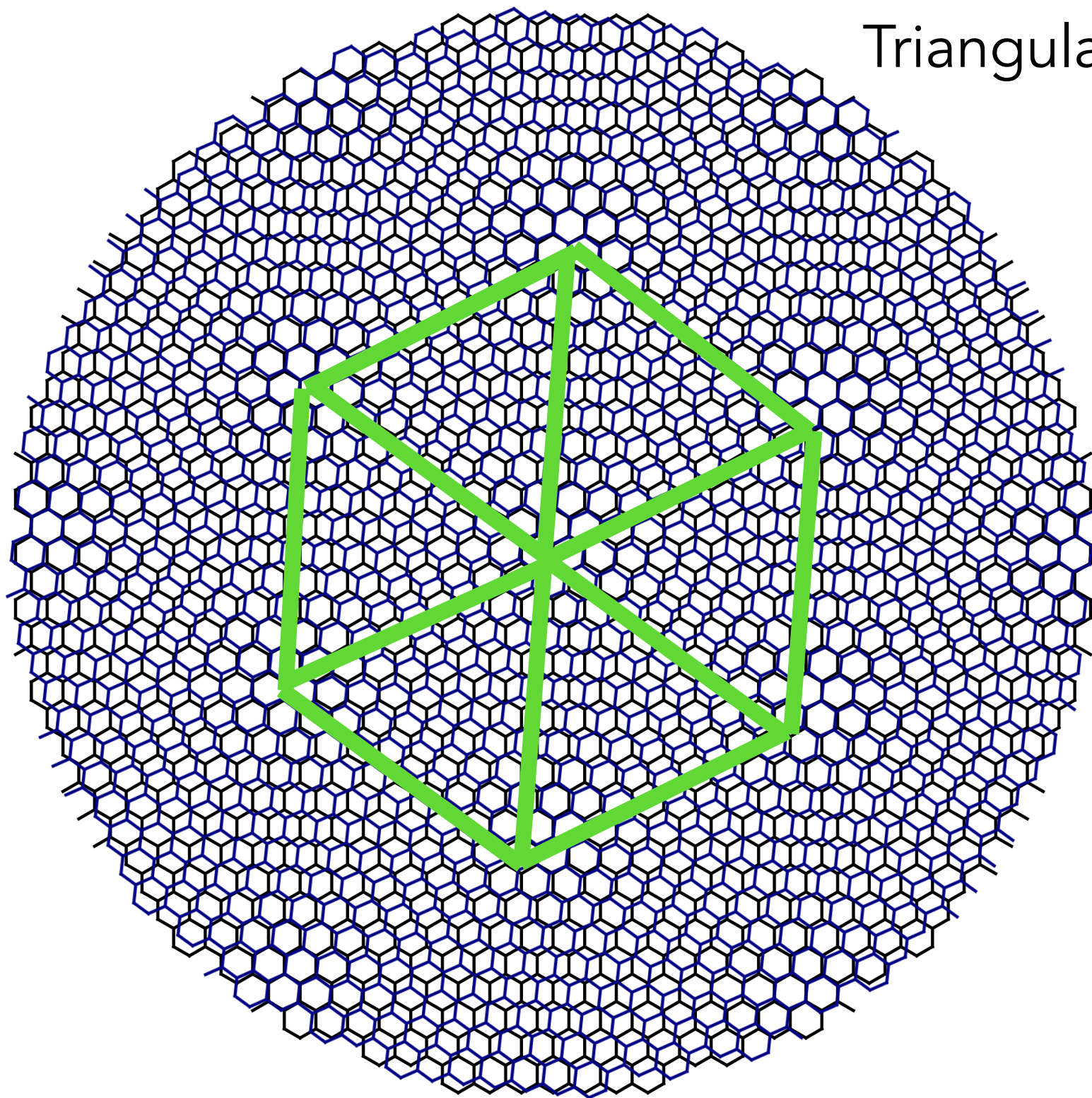
Moiré pattern

$6^\circ$



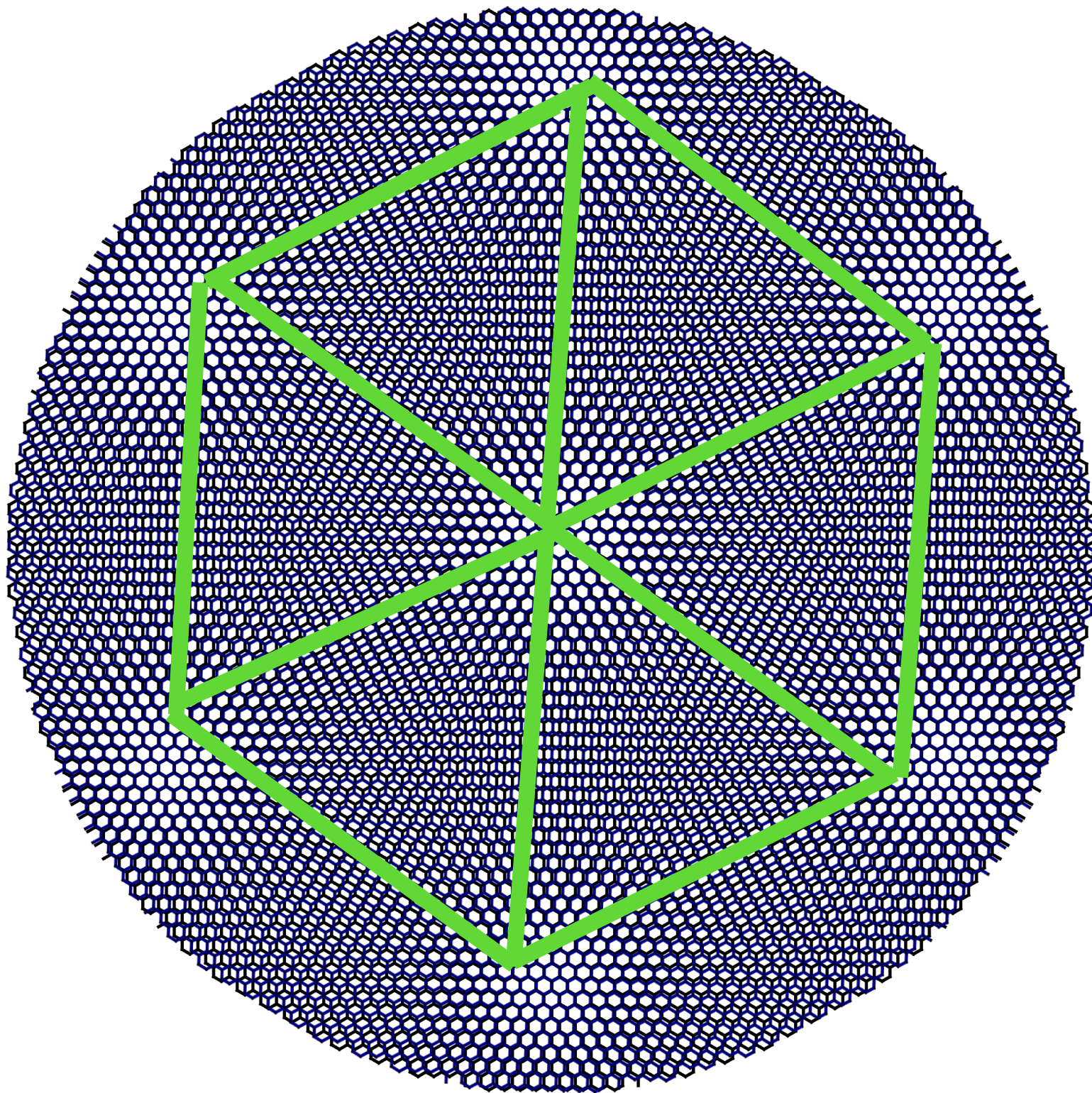
$6^\circ$

Triangular lattice



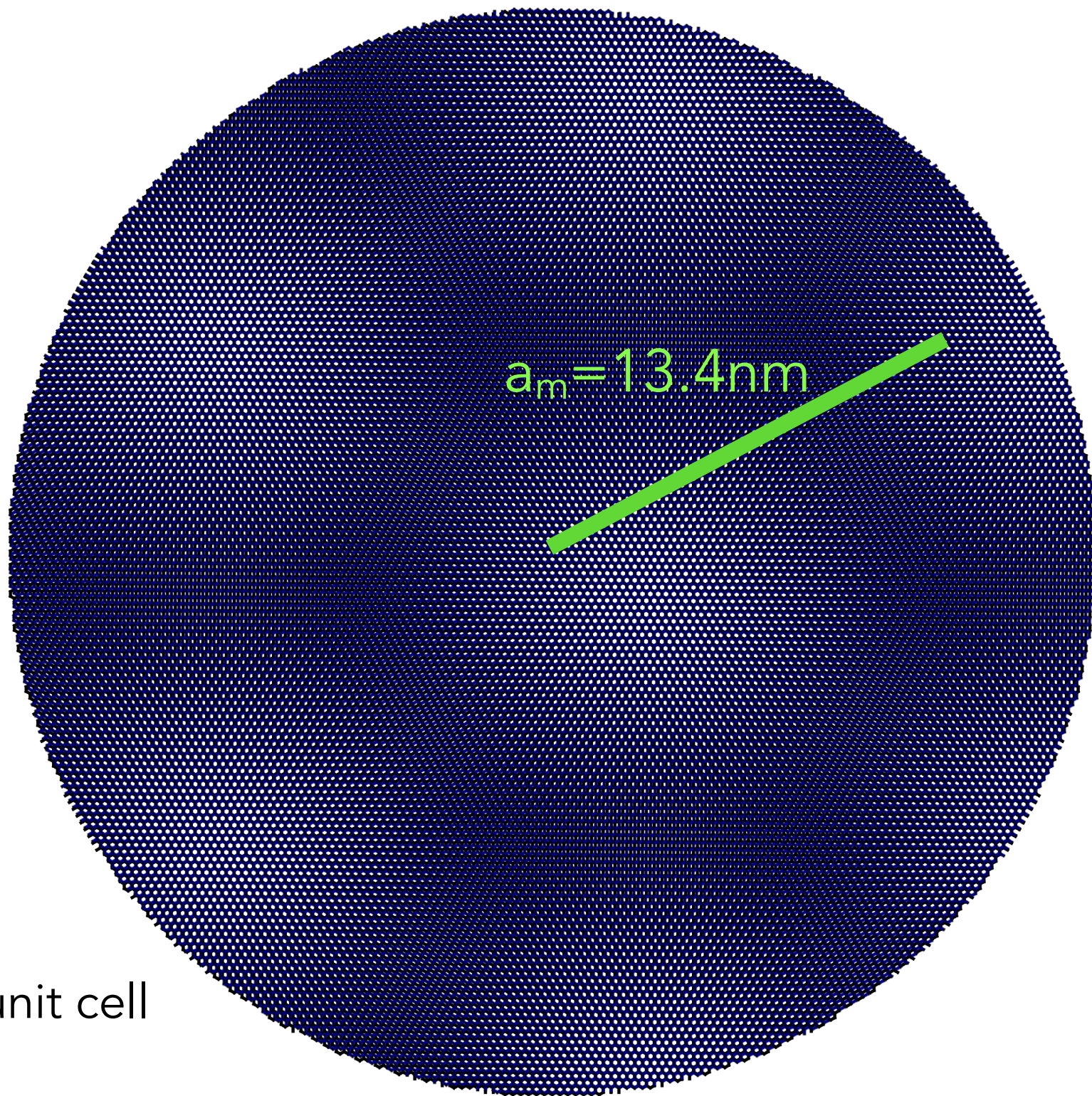


2°





1°



huge unit cell

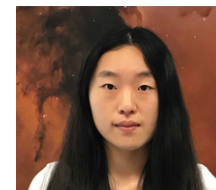


6°

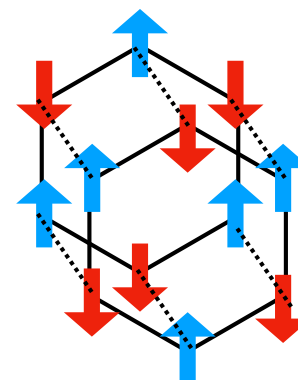
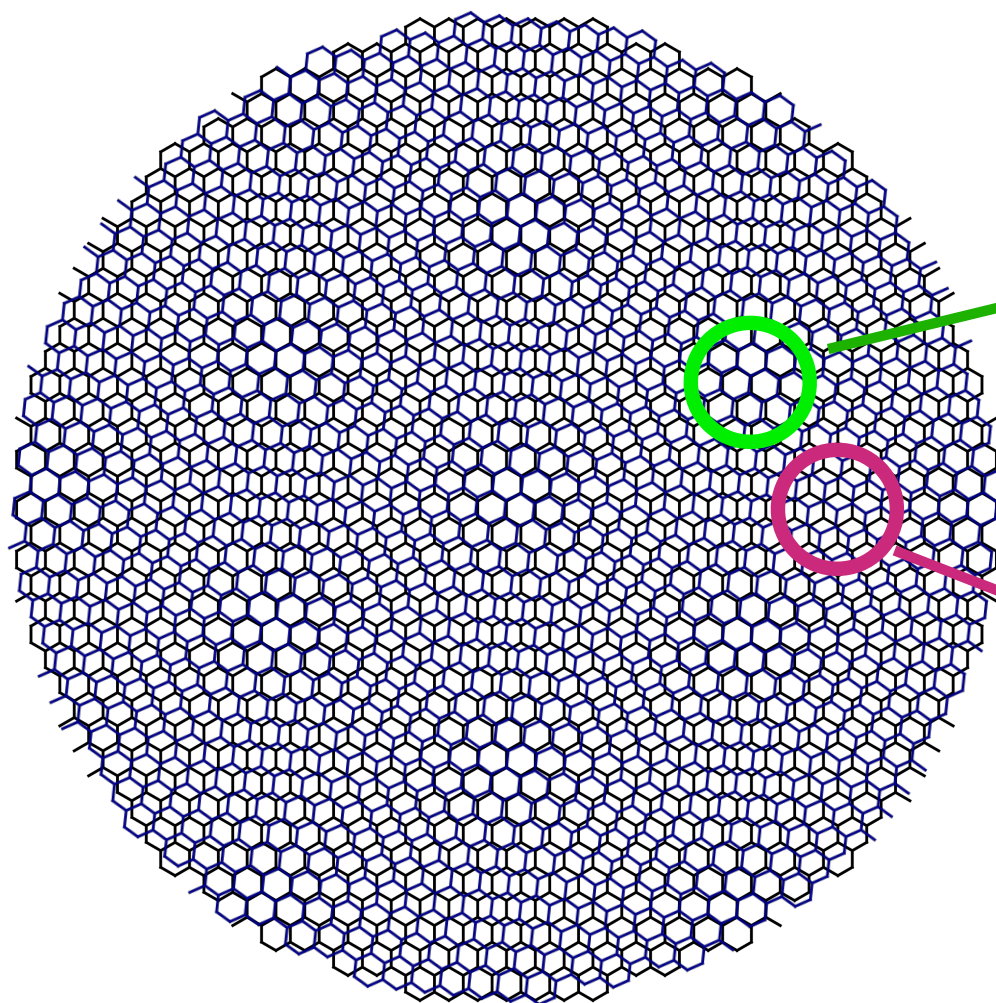
# Twisted AF



Kasra Hejazi

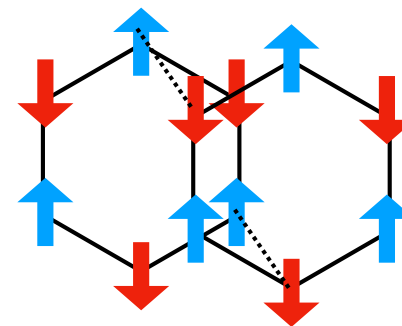


Zhu-Xi Luo



AA

$$N_1 = -N_2$$



AB

$$N_1 = N_2$$

Frustration: Néel vectors must rotate

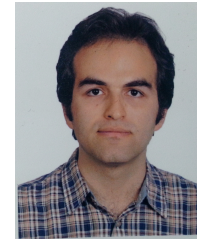
# Continuum model(s)

- Basic assumptions:

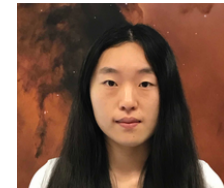
- Inter-layer coupling weak  $J' \ll J$

- Rotation angle is small (can also treat general strains)

- Example:  $\text{MnPS}_3$ : excellent Heisenberg AF



Kasra Hejazi



Zhu-Xi Luo

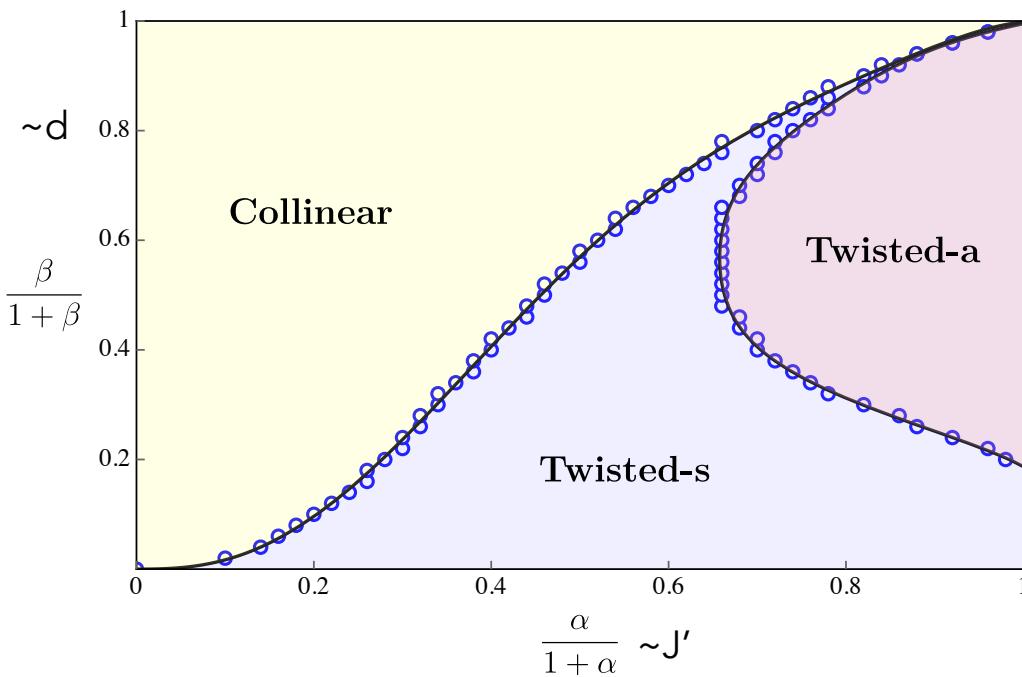
$$\mathcal{L} = \sum_l \frac{\rho}{2v^2} (\partial_t \mathbf{N}_l)^2 - \mathcal{H}_{\text{cl}} \quad \mathcal{H}_{\text{cl}} = \sum_l \left[ \frac{\rho}{2} (\nabla \mathbf{N}_l)^2 - d (N_l^z)^2 \right] - J' \Phi(\mathbf{x}) \mathbf{N}_1 \cdot \mathbf{N}_2$$
$$\Phi(\mathbf{x}) = \sum_{a=1}^3 \cos(\mathbf{q}_a \cdot \mathbf{x})$$

Can predict spin textures, magnon subbands, etc.

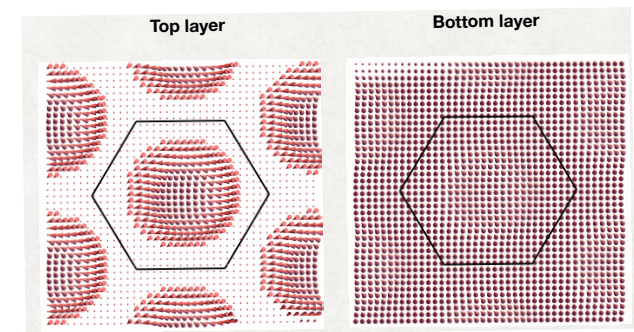
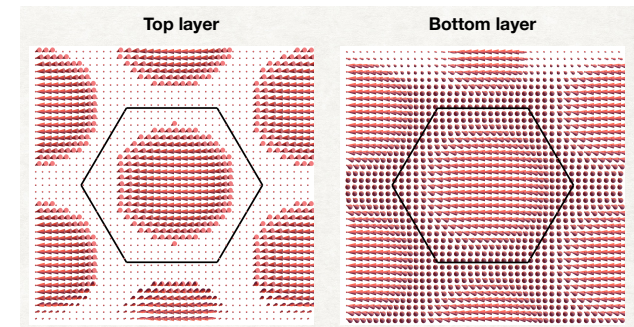
# Twisted AF

$$\mathcal{H}_{\text{cl}} = \sum_l \left[ \frac{\rho}{2} (\nabla \mathbf{N}_l)^2 - d (N_l^z)^2 \right] - J' \Phi(\mathbf{x}) \mathbf{N}_1 \cdot \mathbf{N}_2$$

Dimensionless parameter  $\alpha = \frac{2J'}{\rho q_m^2} \sim \frac{J'}{J\theta^2}$

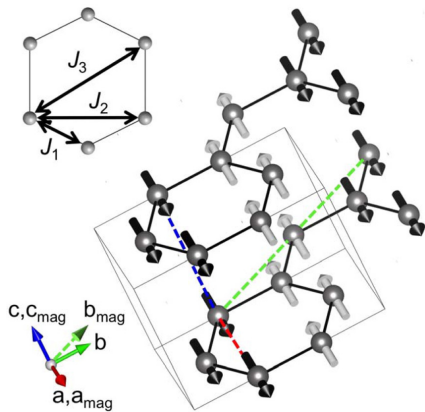


Coplanar spin textures



Transitions should be tunable by applied field

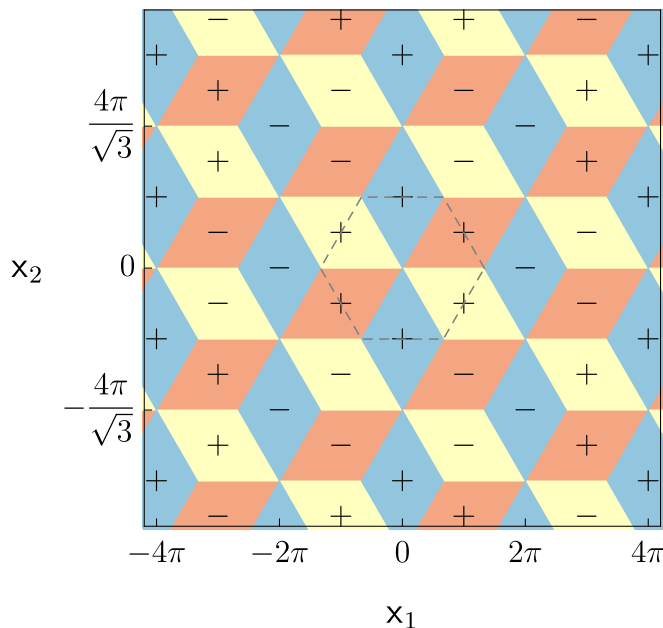
# Zig-Zag antiferromagnets



$$\mathcal{H}_{cl} = \sum_{a,l} \frac{\rho}{2} (\nabla N_{a,l})^2 - \frac{J'}{2} \sum_a N_{a,1} \cdot N_{a,2} \cos \left( \frac{\mathbf{q}_a \cdot \mathbf{x}}{2} \right)$$

3 distinct  $\mathbf{q}_a$  domains

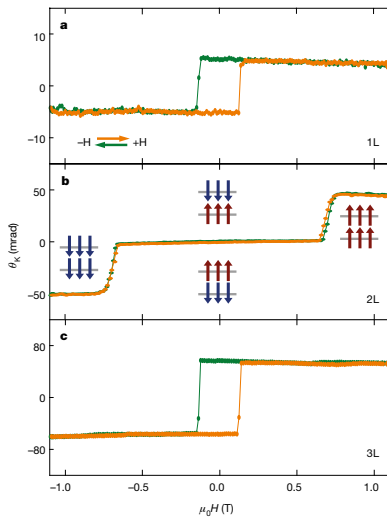
NiPS<sub>3</sub>, FePS<sub>3</sub>, CoPS<sub>3</sub>, RuCl<sub>3</sub>...



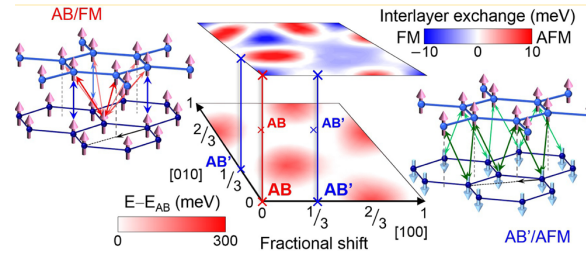
Strong-coupling  
domains have structure  
of "dice lattice"

# CrI<sub>3</sub>

Might not expect much from a *ferro*-magnet, but...



B. Huang *et al*, 2017



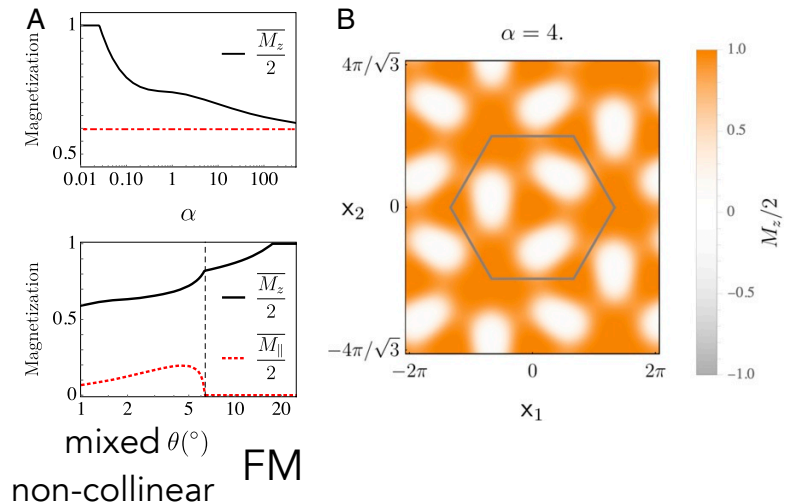
Sivadas *et al*, 2018

Sign-changing stacking-dependent interactions

$$\mathcal{H}_{\text{cl}} = \sum_l \left[ \frac{\rho}{2} (\nabla \mathbf{M}_l)^2 - d (M_l^z)^2 \right] - J' \tilde{\Phi}(\mathbf{x}) \mathbf{M}_1 \cdot \mathbf{M}_2$$



from DFT theory



# CrI<sub>3</sub>

nature  
nanotechnology

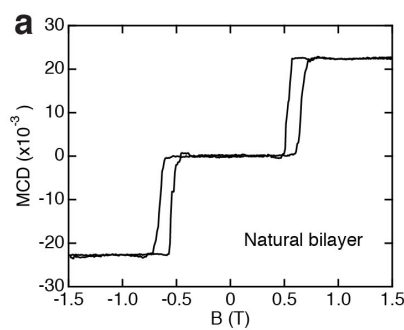
LETTERS

<https://doi.org/10.1038/s41565-021-01014-y>

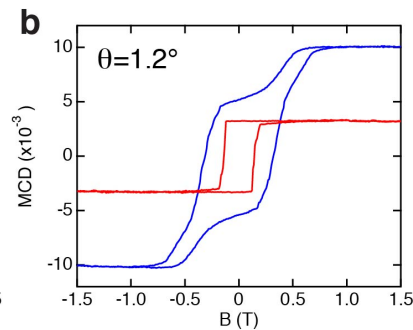
Check for updates

## Coexisting ferromagnetic-antiferromagnetic state in twisted bilayer CrI<sub>3</sub>

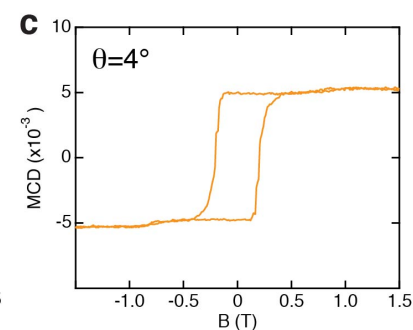
Yang Xu<sup>1,2</sup>, Ariana Ray<sup>3</sup>, Yu-Tsun Shao<sup>1</sup>, Shengwei Jiang<sup>3</sup>, Kihong Lee<sup>3</sup>, Daniel Weber<sup>4</sup>, Joshua E. Goldberger<sup>4</sup>, Kenji Watanabe<sup>5</sup>, Takashi Taniguchi<sup>6</sup>, David A. Muller<sup>1,7</sup>, Kin Fai Mak<sup>1,3,7</sup> and Jie Shan<sup>1,3,7</sup>✉



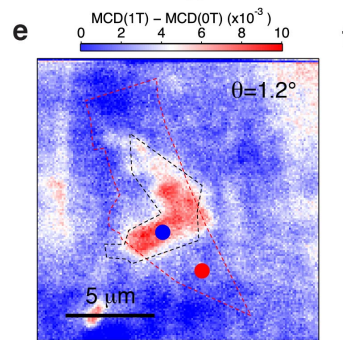
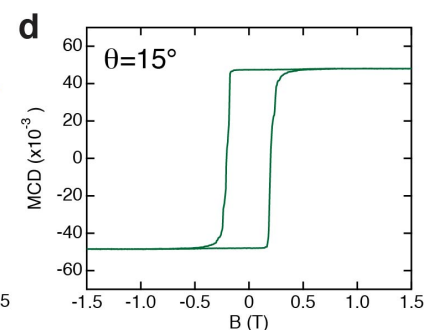
bilayer: AF



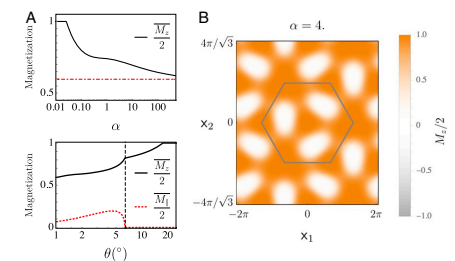
small twist: mixed



large twist: FM



c.f.





# CrI<sub>3</sub>

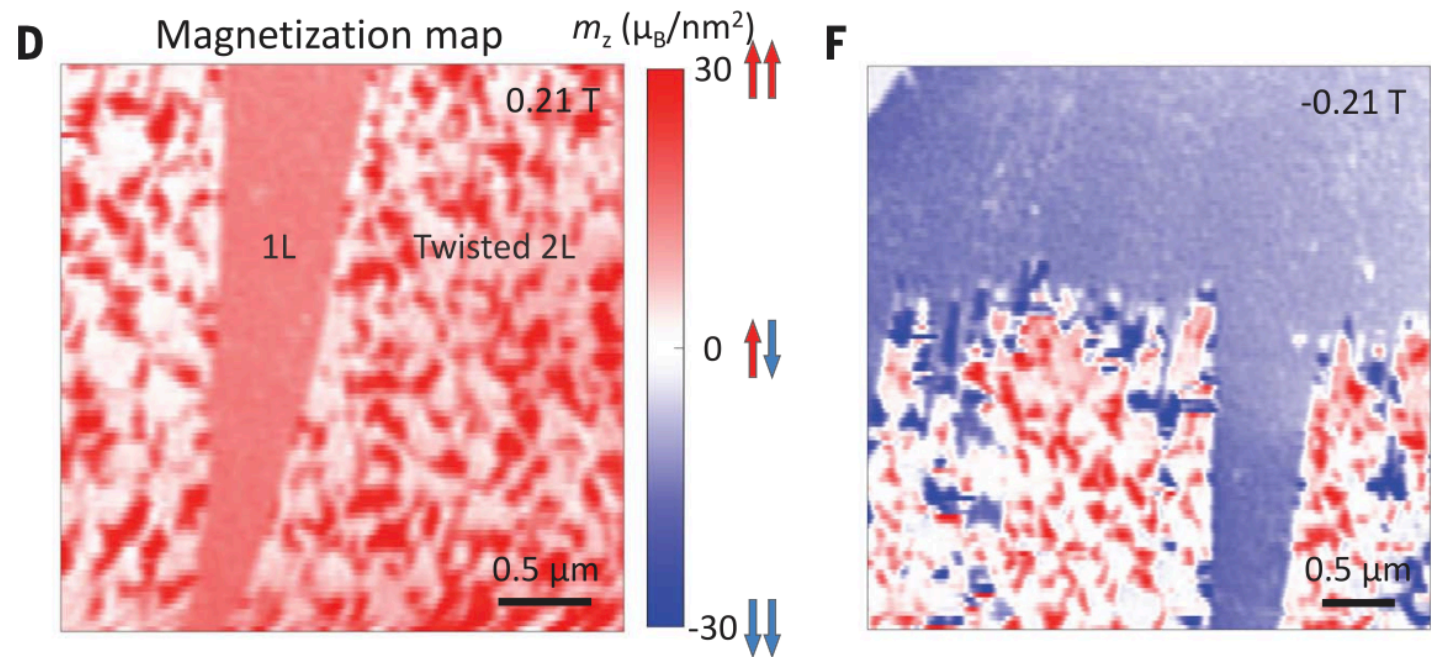
## REPORT

### MAGNETISM

## Direct visualization of magnetic domains and moiré magnetism in twisted 2D magnets

Tiancheng Song<sup>1,†</sup>, Qi-Chao Sun<sup>2,†</sup>, Eric Anderson<sup>1,†</sup>, Chong Wang<sup>3</sup>, Jimin Qian<sup>4</sup>, Takashi Taniguchi<sup>5</sup>, Kenji Watanabe<sup>6</sup>, Michael A. McGuire<sup>7</sup>, Rainer Stöhr<sup>2,8</sup>, Di Xiao<sup>3</sup>, Ting Cao<sup>4</sup>, Jörg Wrachtrup<sup>2,9,\*</sup>, Xiaodong Xu<sup>1,4,\*</sup>

## Scanning NV magnetometry



(twist disorder is evident)

# Merci

