

# TOPOLOGY AND CORRELATIONS IN SPIN SYSTEMS

# TALKS IN THIS SESSION

## QUANTUM MAGNETIC MATERIALS

- Yuji **Matsuda** (Kyoto University, Japan)  
"Majorana Quantization and Half-Integer Thermal Quantum Hall Effect in a Kitaev Spin Liquid"
- Joseph **Checkelsky** (Massachusetts Institute of Technology, USA)  
"Dirac Electrons in Kagome Lattice Materials"
- Lucile **Savary** (CNRS / École Normale Supérieure de Lyon, France)  
"Surprising Transport Phenomena in Magnets"

# TOPOLOGY IN SPIN SYSTEMS

- Previous talks: topology of “free” electron problems
- How do we apply topology to spin systems??
  - Find some emergent fermions 
  - Couple the spins to electrons
  - avoid fermions completely

# TOPOLOGY IN SPIN SYSTEMS

- Previous talks: topology of “free” electron problems
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• Find some emergent fermions	Matsuda	Savary
• Couple the spins to electrons	Checkelsky	Savary
• avoid fermions completely		Not today!

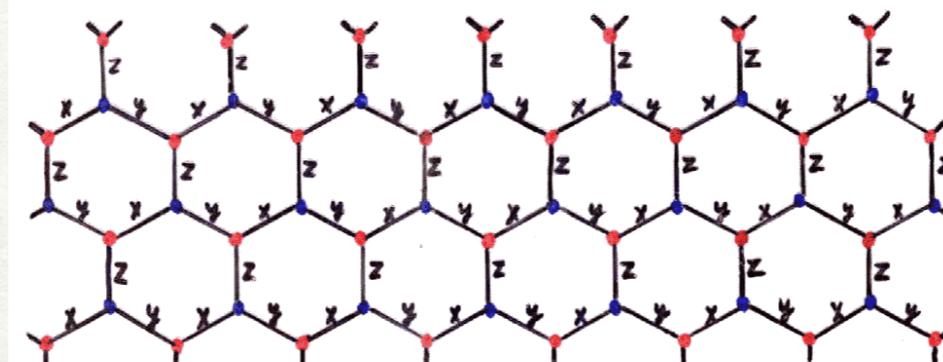
# KITAEV MODEL



Kitaev's honeycomb model

$$H = \sum_{i,\mu} K_\mu \sigma_i^\mu \sigma_{i+\mu}^\mu$$

## 1. The model



Spin  $\frac{1}{2}$  on each site.

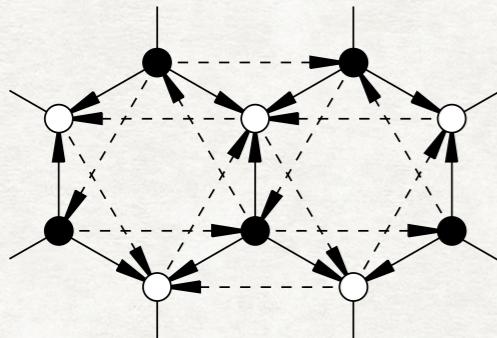
exact parton construction  $\sigma_i^\mu = i c_i c_i^\mu$   $c_i c_i^x c_i^y c_i^z = 1$

effective quadratic Hamiltonian

$$H = \sum_{i,\mu} i K_\mu c_i c_{i+\mu}$$

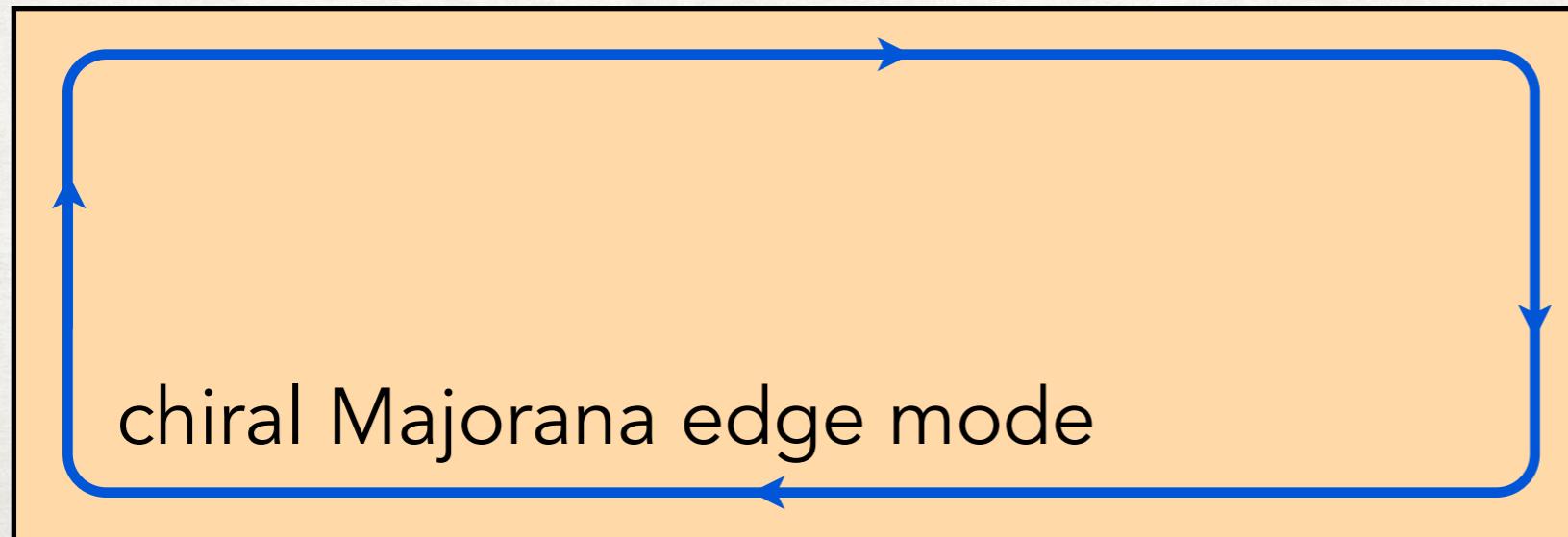
# NON-ABELIAN PHASE

- In an applied magnetic field, the Majoranas acquire a gap
  - BdG Hamiltonian for a topological superconductor



$$H_{\text{eff}} = \frac{i}{4} \sum_{j,k} A_{jk} c_j c_k,$$
$$A = 2J(\text{---}) + 2\kappa(\text{---}),$$
$$\kappa \sim \frac{h_x h_y h_z}{J^2}.$$

field induces a fermion mass, very similar to the Haldane model (except Majorana)

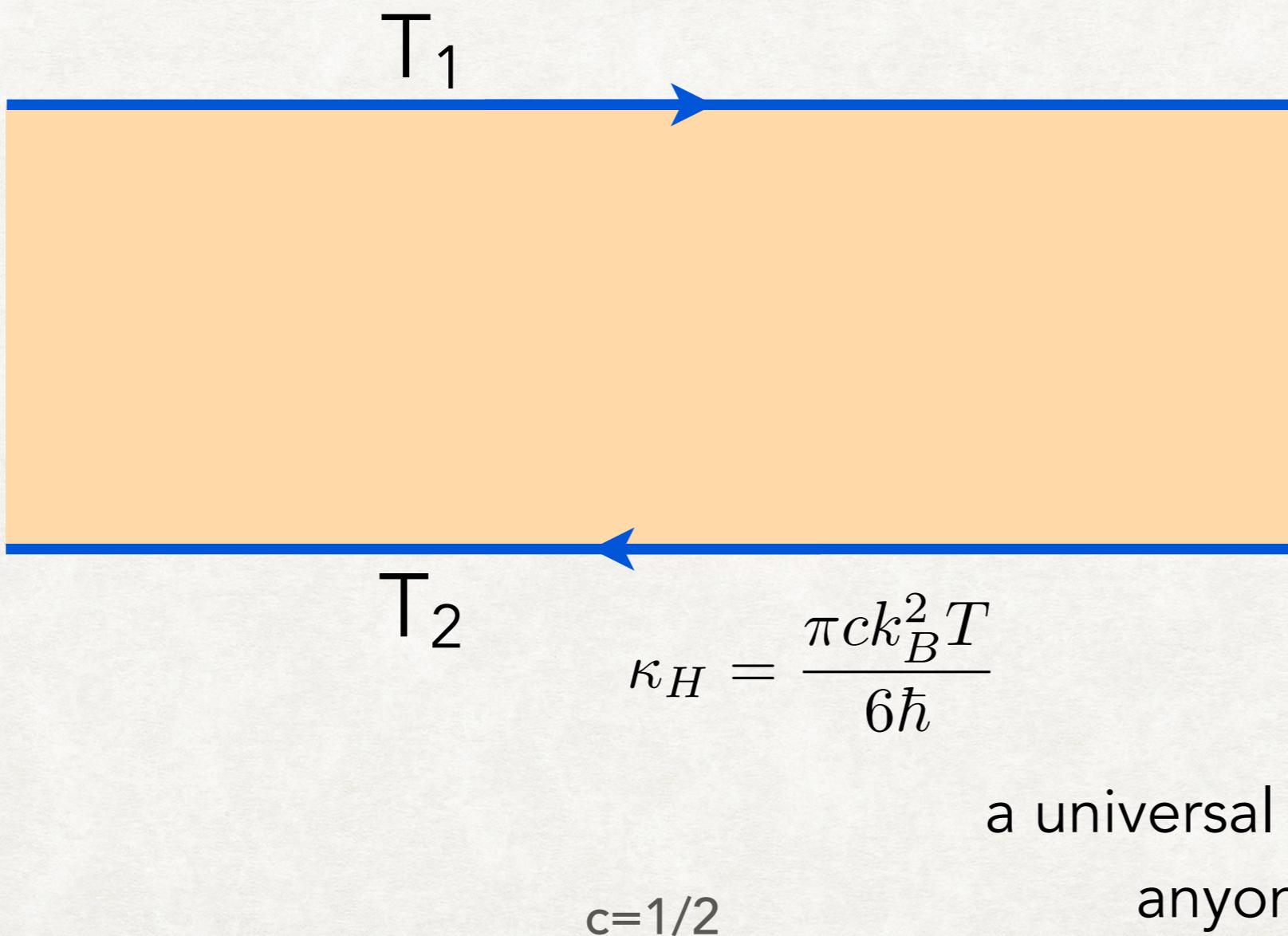


$$H_e = -\frac{iv}{4} \int dx \eta \partial_x \eta$$

Like p+ip edge state except  
the **fermions are not**  
electrons

# THERMAL QUANTUM HALL EFFECT

- Edge state picture



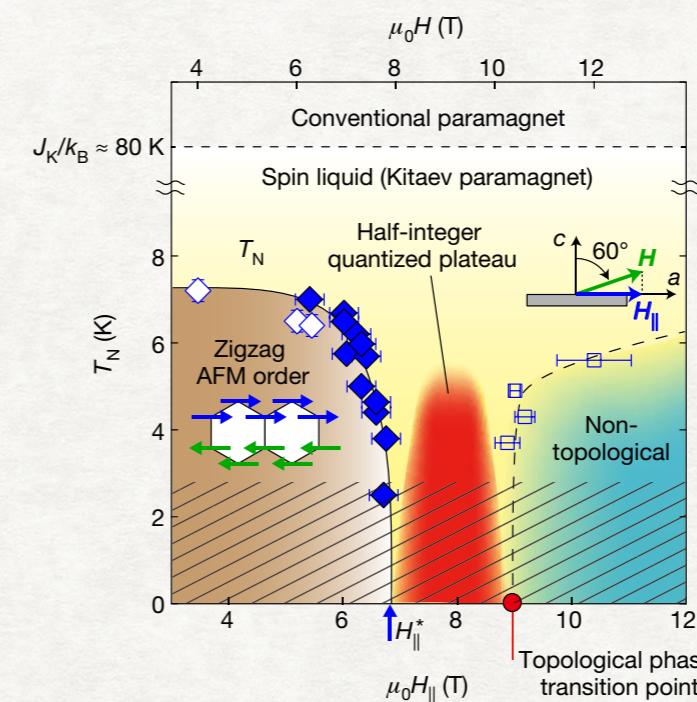
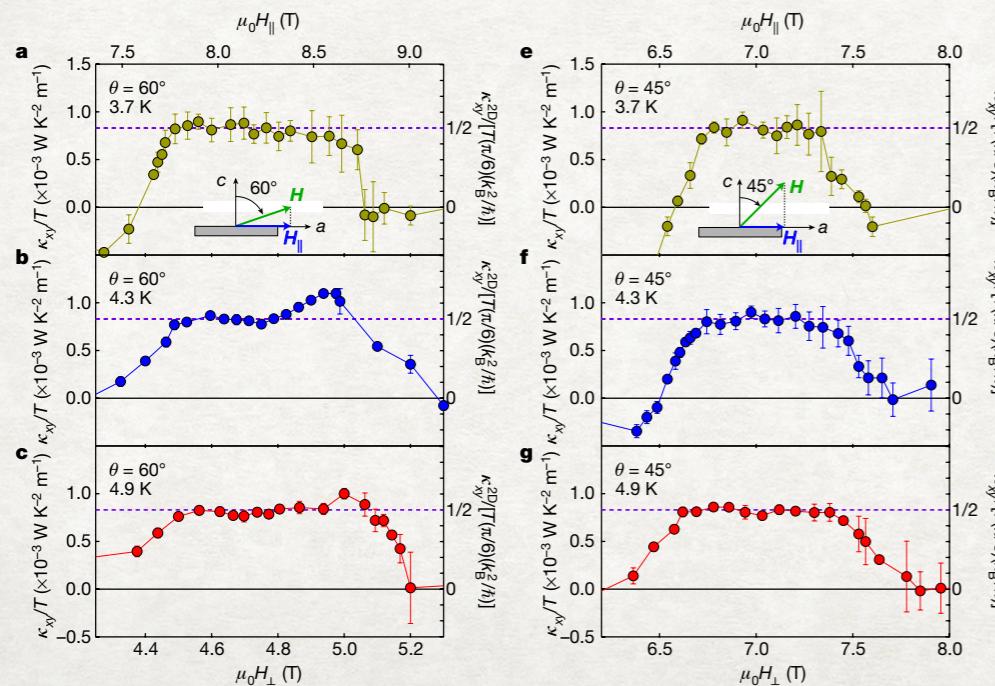
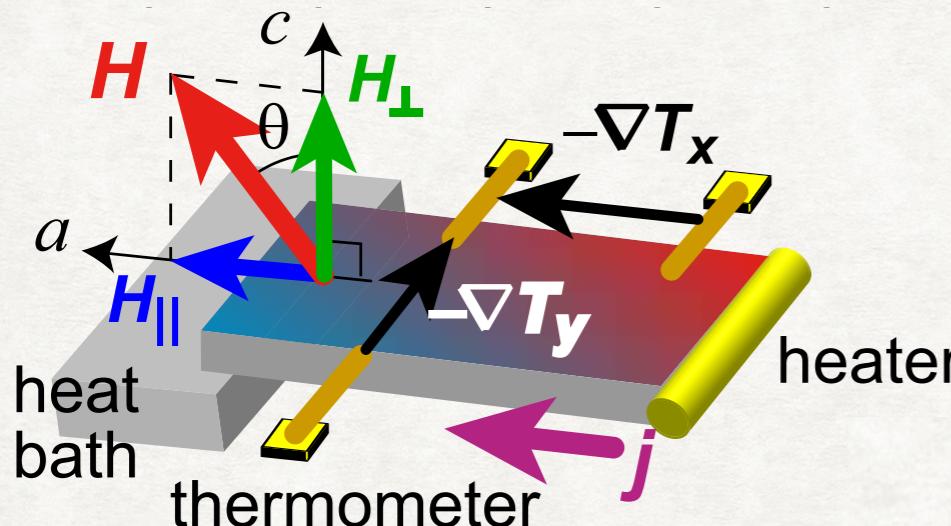
$$I_x = \kappa_H \Delta T_y$$

a universal prediction for chiral “Ising anyon” phase: agnostic to microscopic spin interactions

# KITAEV SPIN LIQUID

## MATSUDA: QUANTIZED THERMAL HALL EFFECT?

- Kasahara *et al*, 2018.  $\alpha$ -RuCl<sub>3</sub>



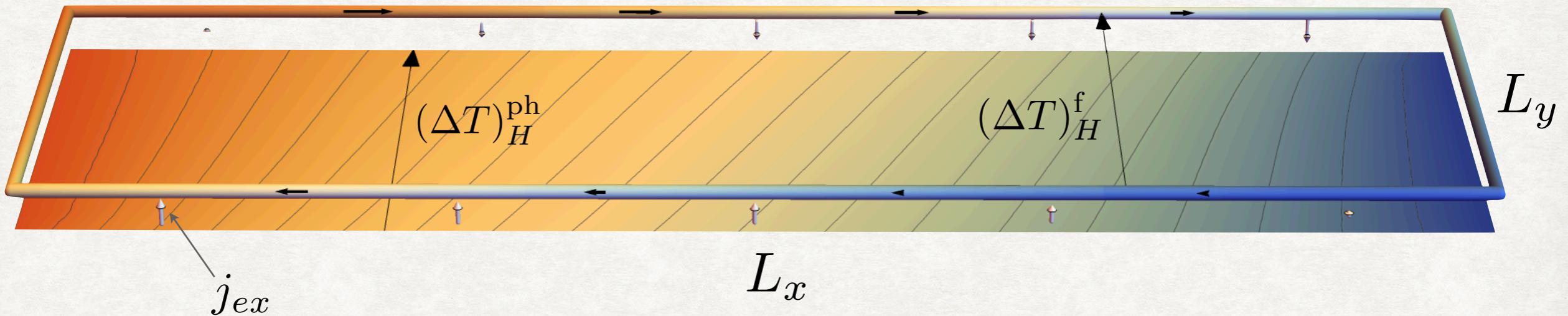
Evidence for an emergent chiral Majorana fermion edge mode?

### Questions:

- Tiny Hall angle? **Savary**
- Reproducibility?
- Why should the nonabelian QSL be stabilized?

# KITAEV SPIN LIQUID

- **Savary**: How about that small Hall angle?
  - Difference from electrical transport: phonons+spins both carry heat. May there be a phonon miracle??

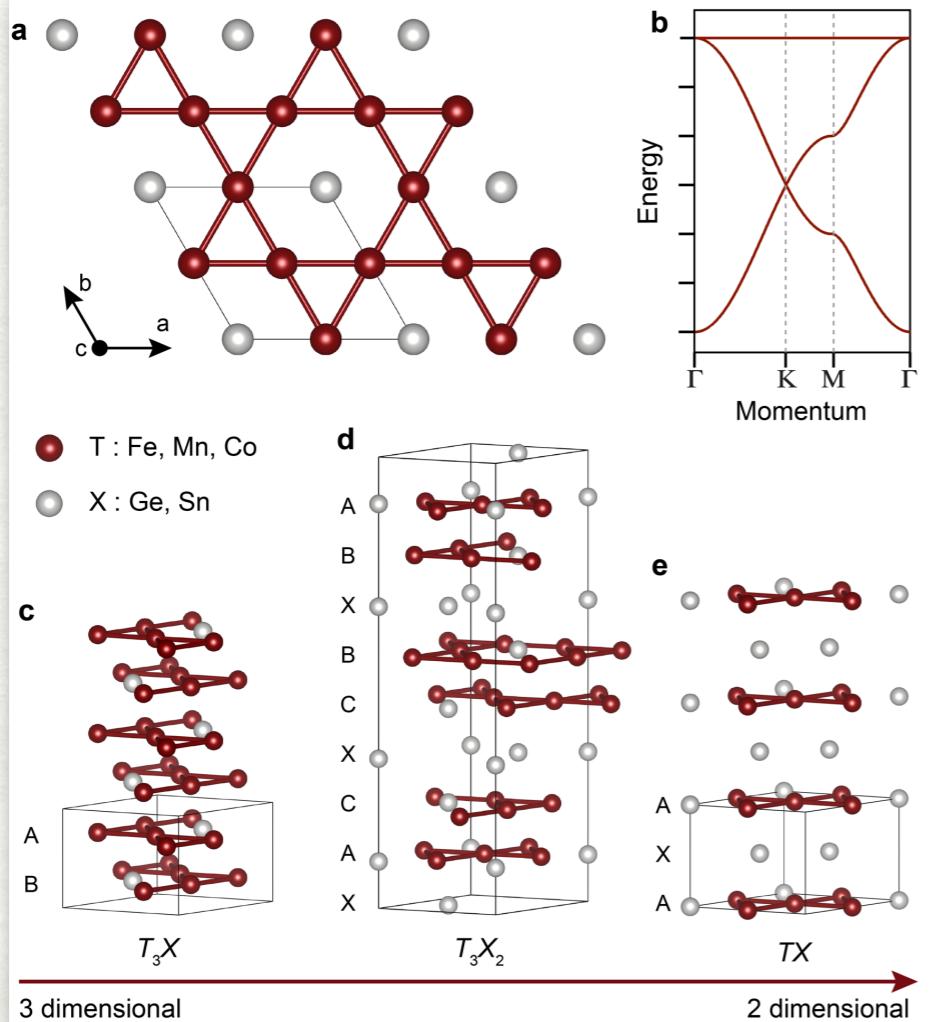


# COUPLE SPINS TO ELECTRONS

- Go to war with the fermions you have, not the fermions you might want or wish to have at a later time (Donald Rumsfeld)
- Magnetic Weyls: Pyrochlore iridates,  $\text{Mn}_3\text{Sn}$ , Heuslers, **RAIGe**,...
- Topological Kondo insulators:  $\text{SmB}_6$ ,  $\text{YbB}_{12}$ , ...
- Magnetically doped topological insulators:  $\text{Cr-Bi}_2\text{Se}_3$ ,  $\text{MnBi}_2\text{Te}_4$ ,...
- Magnetic 2d Dirac fermions? **Checkelsky**

# COUPLE SPINS TO ELECTRONS

- **Checkelsky**:  $\text{Fe}_x\text{Sn}_y$ : Dirac fermions plus spins on a kagome lattice

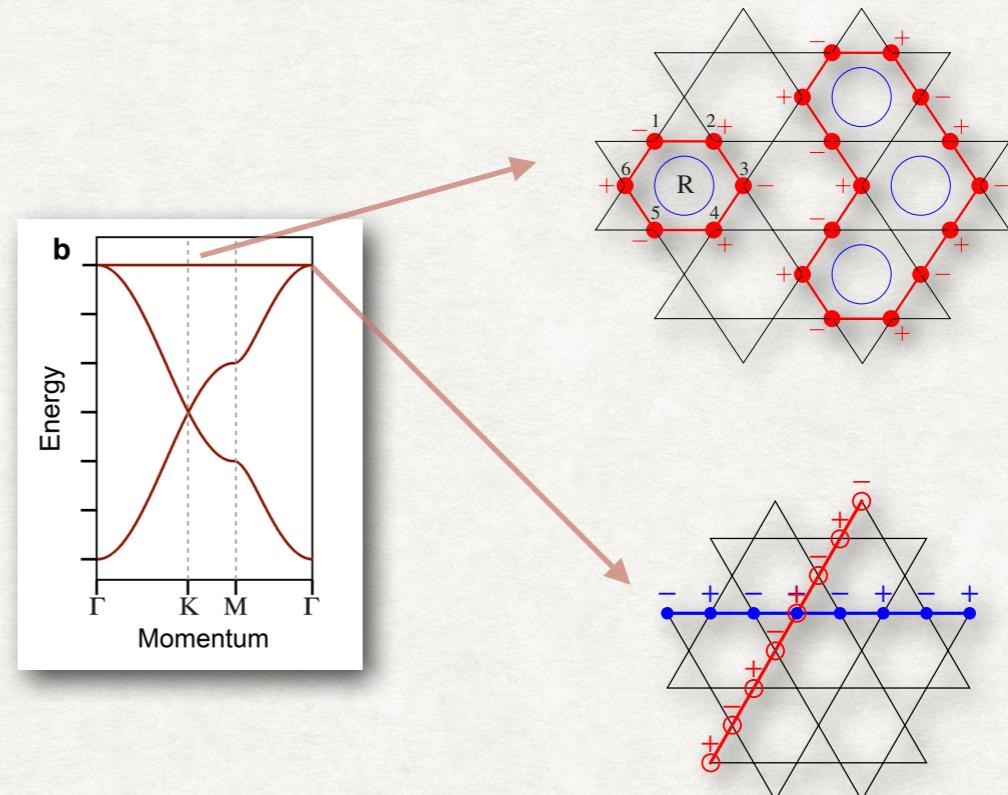


## Old times

PHYSICAL REVIEW B **78**, 125104 (2008)

### Band touching from real-space topology in frustrated hopping models

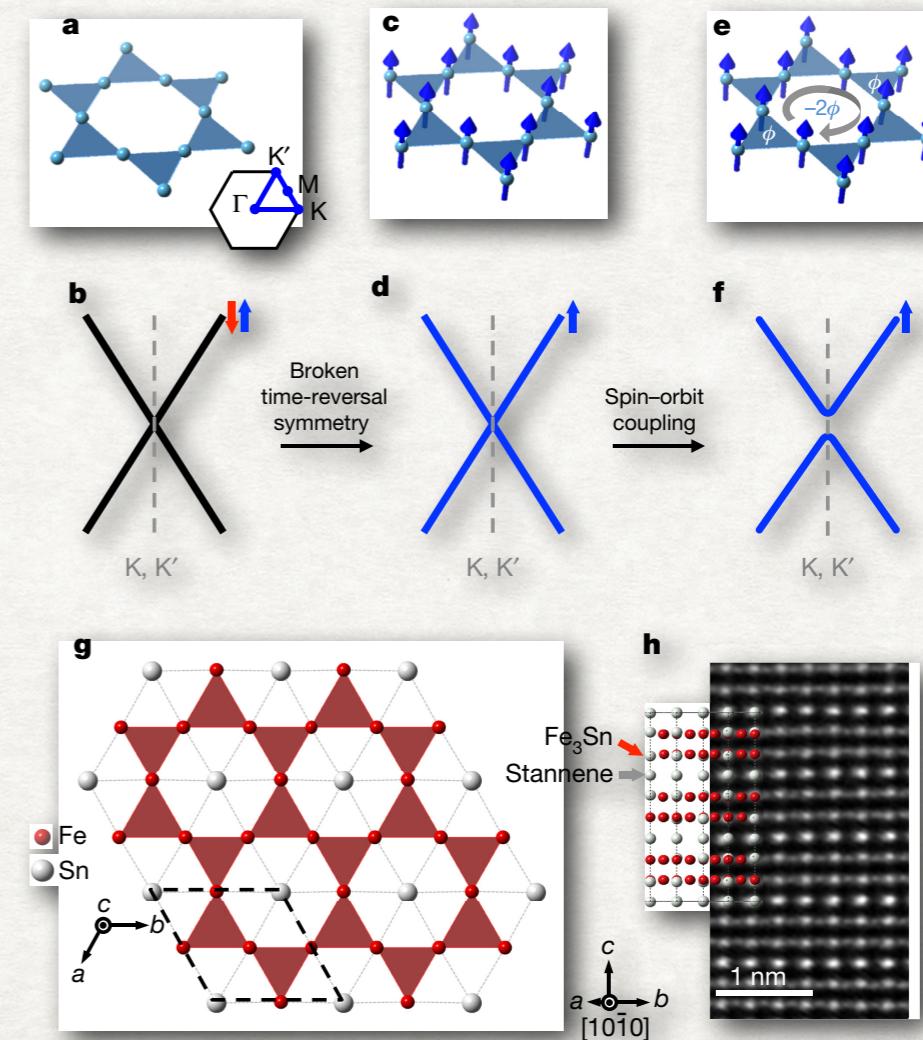
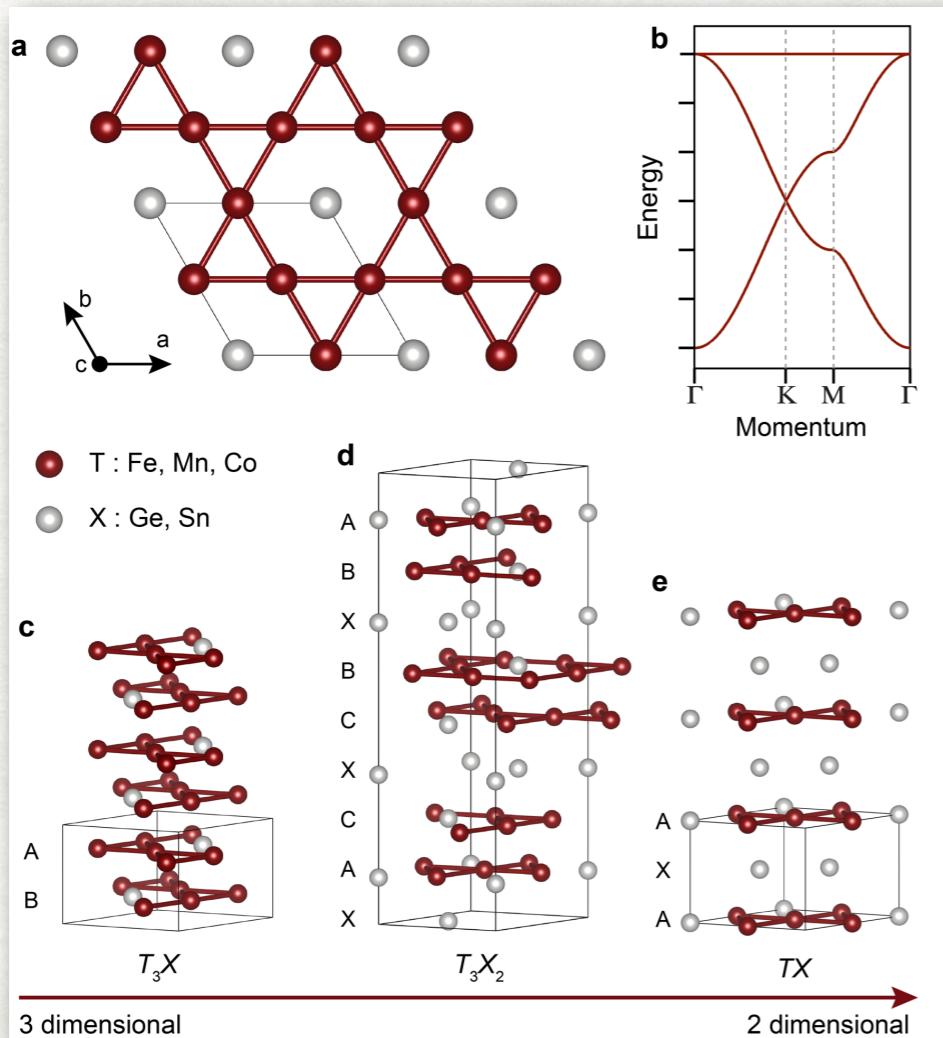
Doron L. Bergman,<sup>1</sup> Congjun Wu,<sup>2</sup> and Leon Balents<sup>3</sup>



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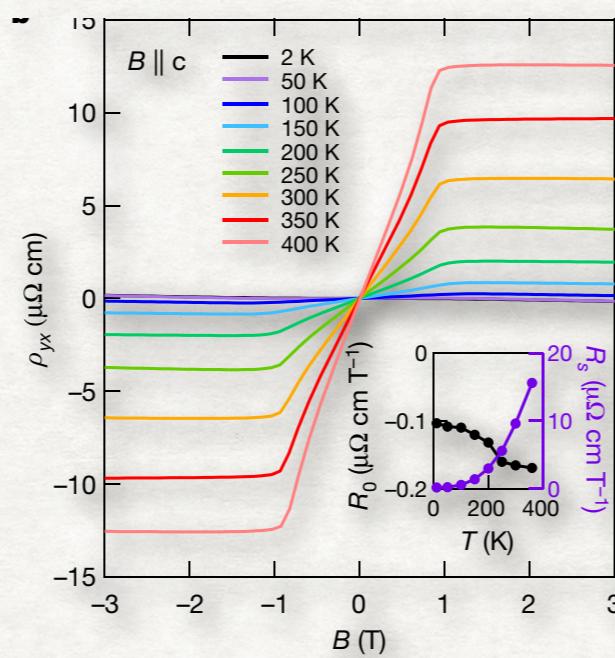
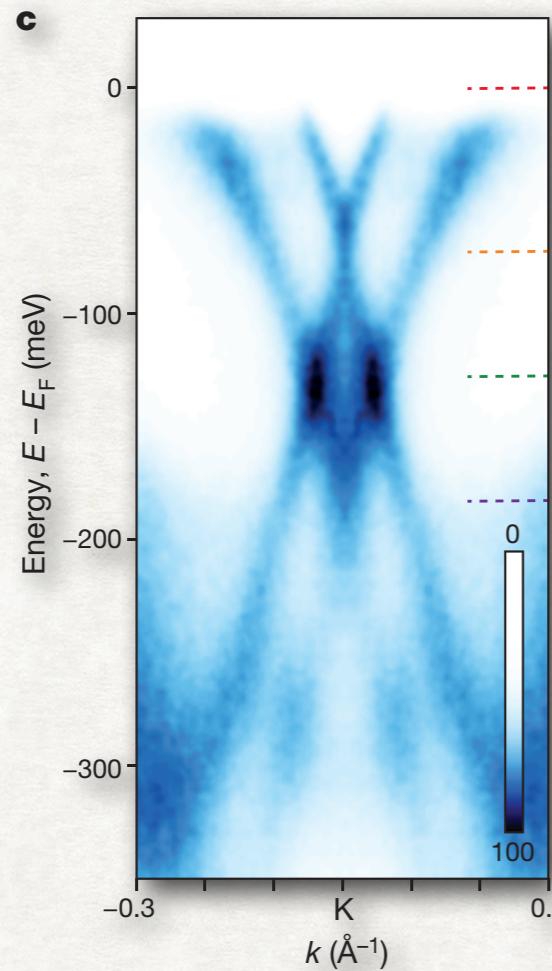
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Q: What orbitals? Why is "s"-orbital TB model relevant?



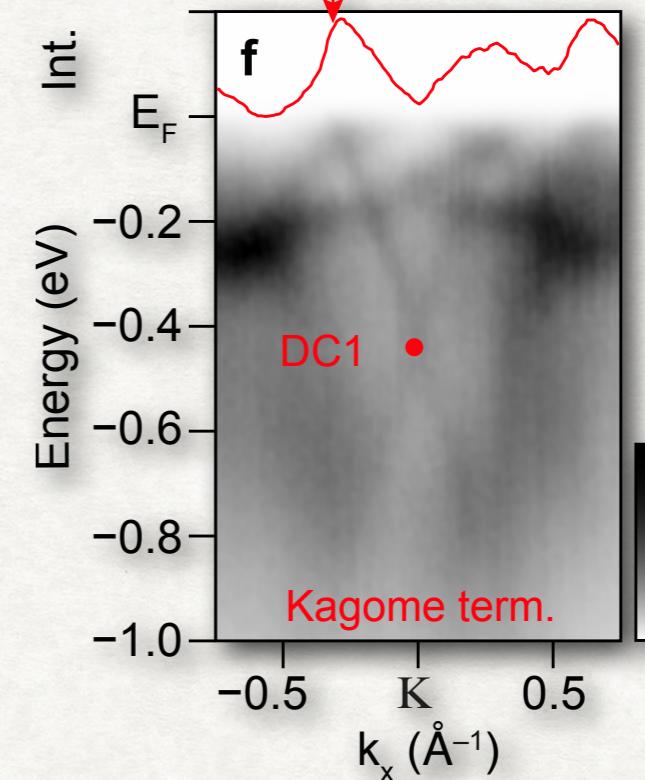
# KAGOME DIRAC FERMIONS?

- $\text{Fe}_3\text{Sn}_2$  (bilayer)



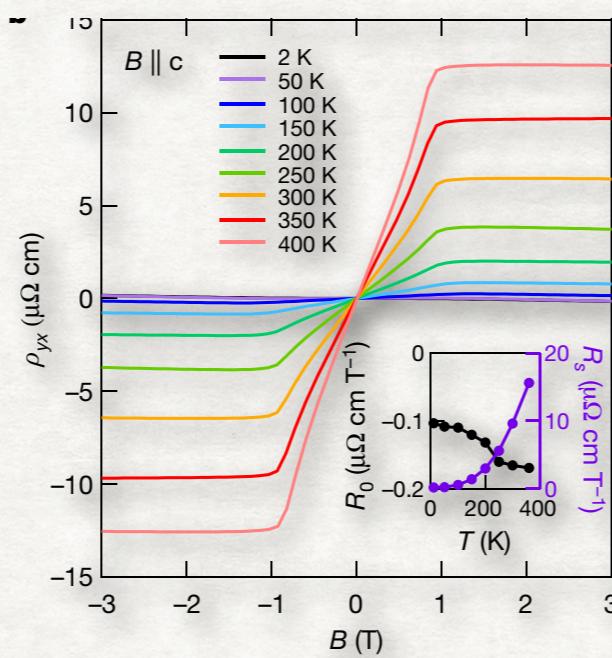
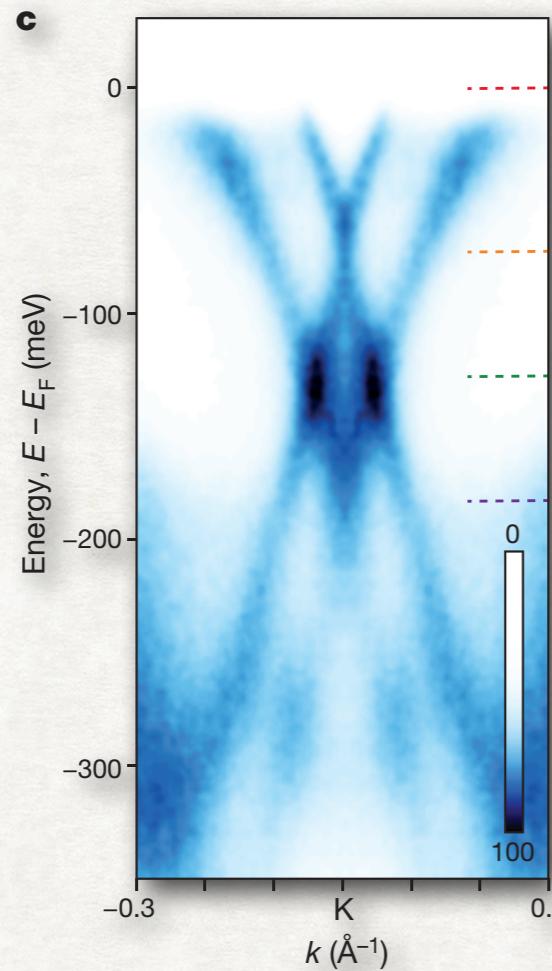
Q: AHE strongly decreases with lower temperature?

- $\text{FeSn}$  (single layer)

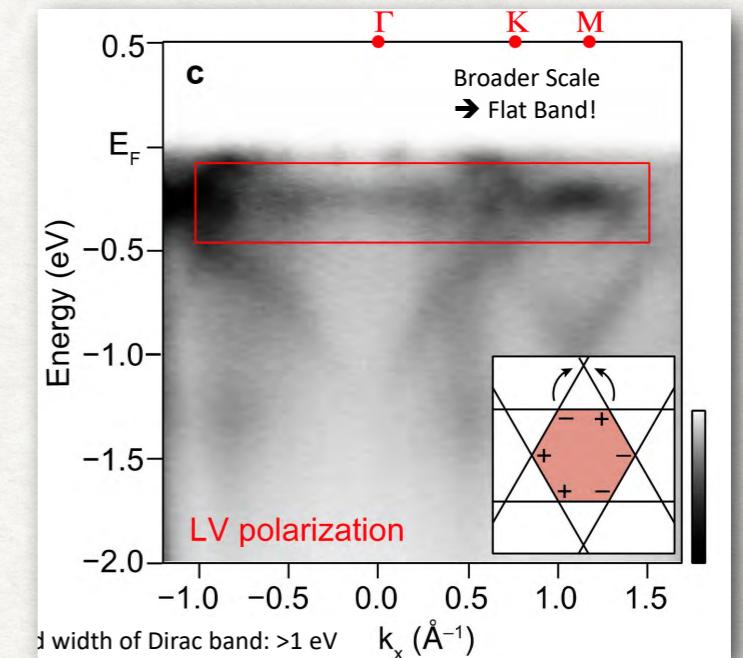


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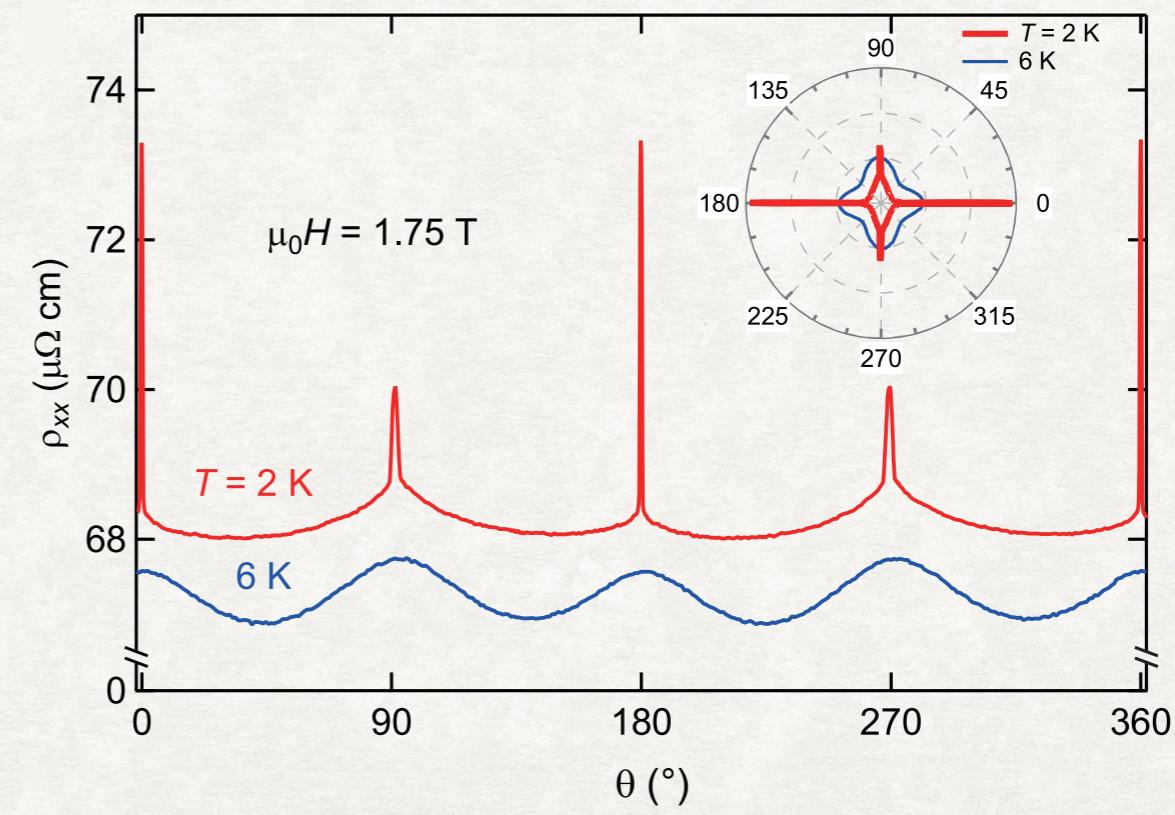
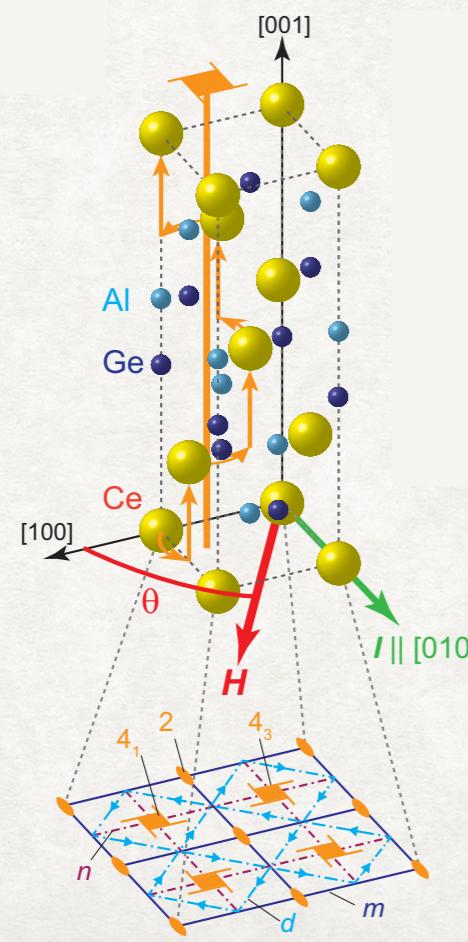


Flat band??!??!

Q: Correlation effects?

# SINGULAR ANGULAR MAGNETORESISTANCE

- **Savary**: surprising transport phenomena in CeAlGe - an antiferromagnetic topological semimetal
- Let me spoil the surprise



Lucile will explain this!

# LET'S GO!!

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