


TOPOLOGY AND CORRELATIONS IN SPIN SYSTEMS

TALKS IN THIS SESSION

QUANTUM MAGNETIC MATERIALS

- Yuji **Matsuda** (Kyoto University, Japan)
"Majorana Quantization and Half-Integer Thermal Quantum Hall Effect in a Kitaev Spin Liquid"
- Joseph **Checkelsky** (Massachusetts Institute of Technology, USA)
"Dirac Electrons in Kagome Lattice Materials"
- Lucile **Savary** (CNRS / École Normale Supérieure de Lyon, France)
"Surprising Transport Phenomena in Magnets"

TOPOLOGY IN SPIN SYSTEMS

- Previous talks: topology of “free” electron problems
- How do we apply topology to spin systems??
 - Find some emergent fermions 
 - Couple the spins to electrons
 - avoid fermions completely

TOPOLOGY IN SPIN SYSTEMS

- Previous talks: topology of “free” electron problems
- How do we apply topology to spin systems??
 - Find some emergent fermions Matsuda Savary
 - Couple the spins to electrons Checkelsky Savary
 - avoid fermions completely Not today!

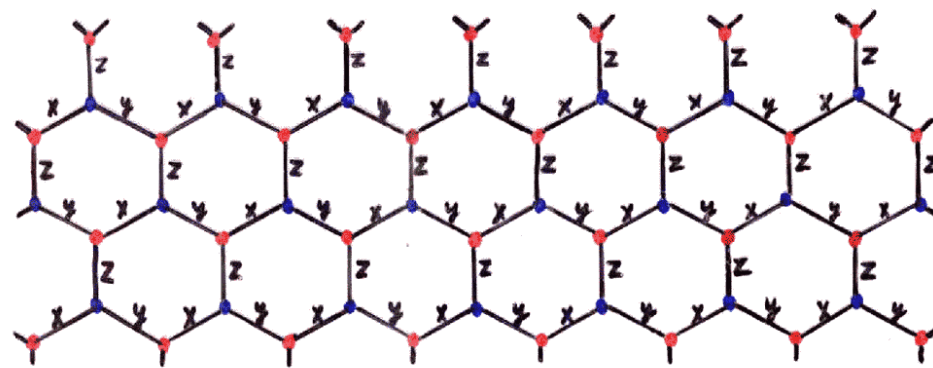
KITAEV MODEL



Kitaev's honeycomb model

$$H = \sum_{i,\mu} K_{\mu} \sigma_i^{\mu} \sigma_{i+\mu}^{\mu}$$

1. The model



Spin $\frac{1}{2}$ on each site.

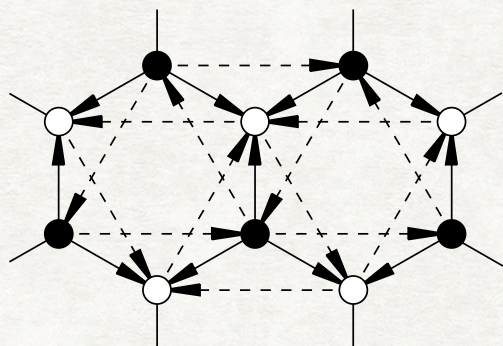
exact parton construction $\sigma_i^{\mu} = i c_i c_i^{\mu}$ $c_i c_i^x c_i^y c_i^z = 1$

effective quadratic Hamiltonian

$$H = \sum_{i,\mu} i K_{\mu} c_i c_{i+\mu}$$

NON-ABELIAN PHASE

- In an applied magnetic field, the Majoranas acquire a gap
- BdG Hamiltonian for a topological superconductor

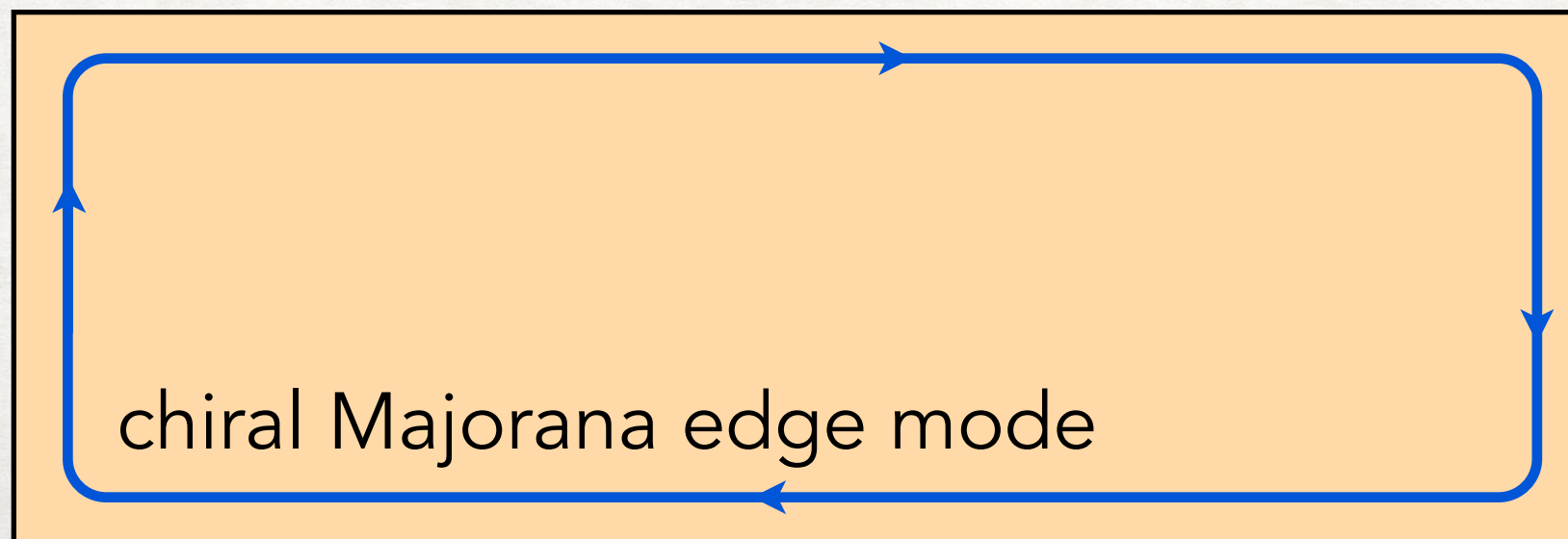


$$H_{\text{eff}} = \frac{i}{4} \sum_{j,k} A_{jk} c_j c_k,$$

$$A = 2J (\text{solid arrow}) + 2\kappa (\text{dashed arrow}),$$

$$\kappa \sim \frac{h_x h_y h_z}{J^2}.$$

field induces a fermion mass,
very similar to the Haldane
model (except Majorana)

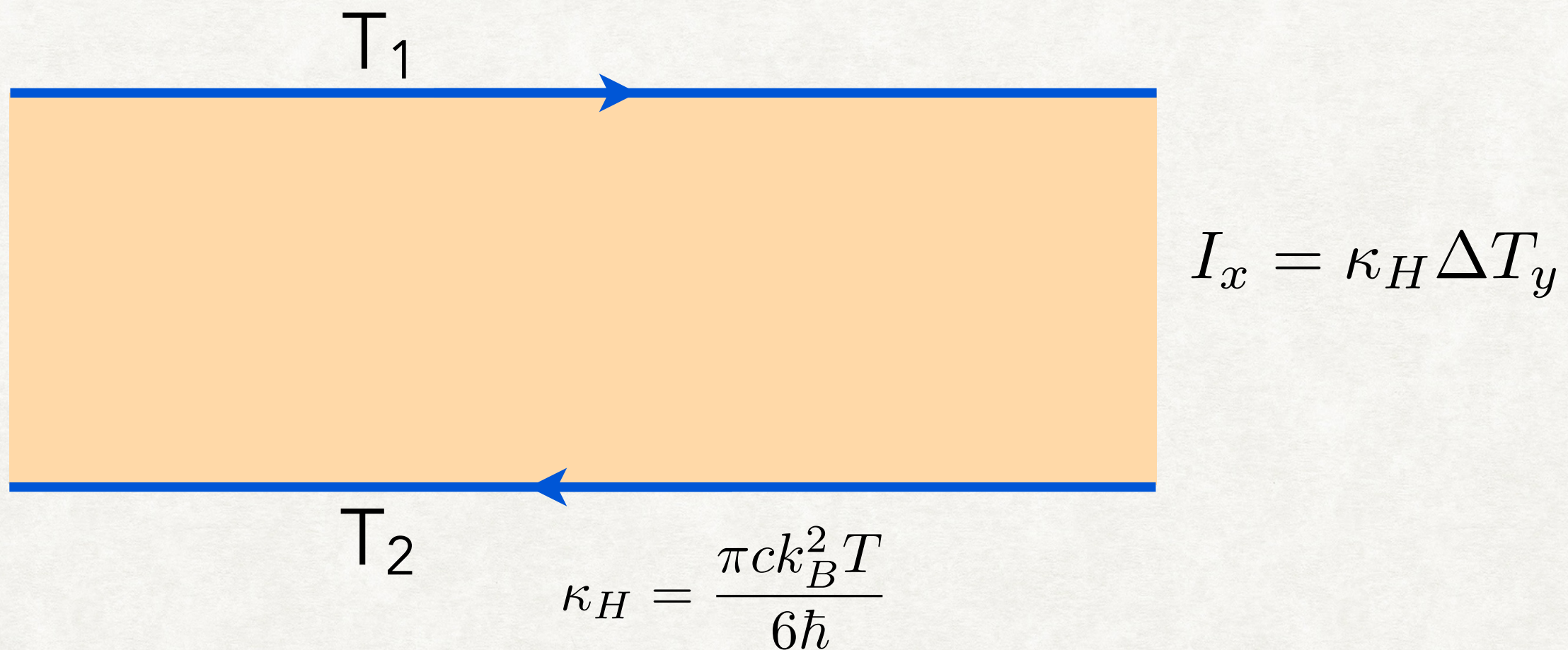


$$H_e = -\frac{iv}{4} \int dx \eta \partial_x \eta$$

Like p+ip edge state except
*the fermions are not
electrons*

THERMAL QUANTUM HALL EFFECT

- Edge state picture



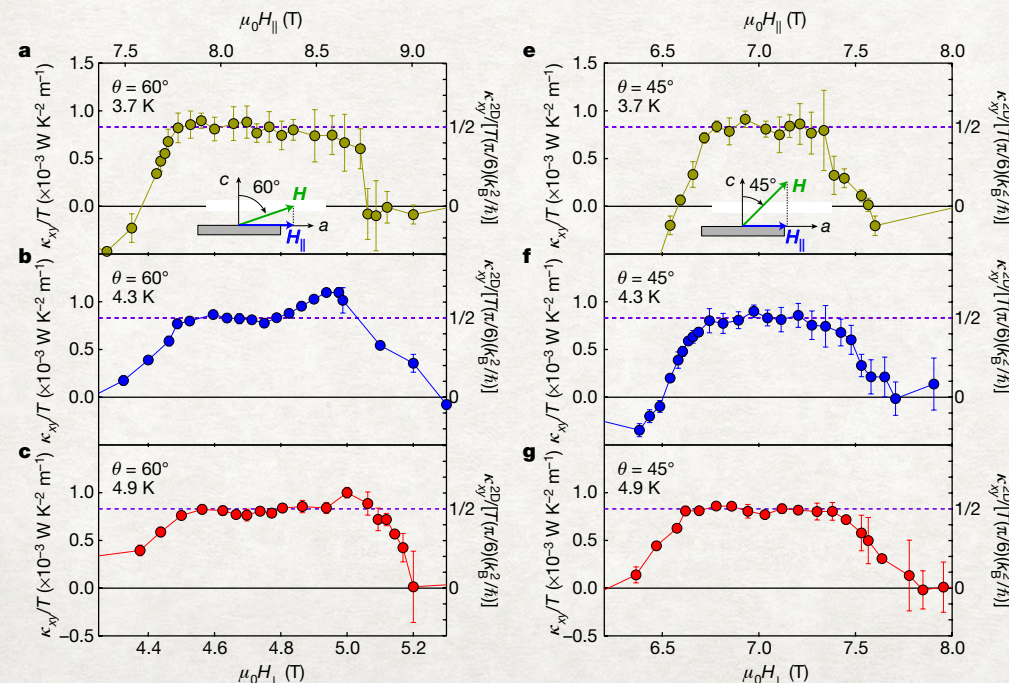
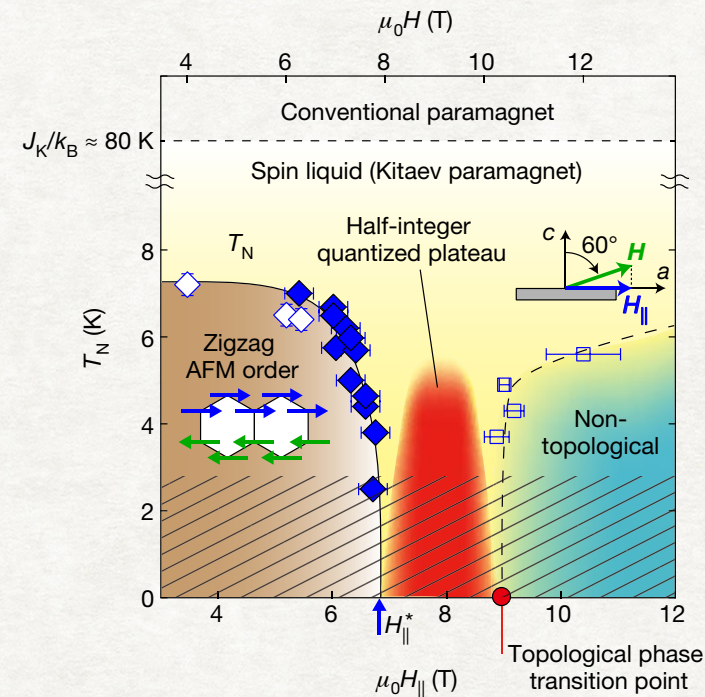
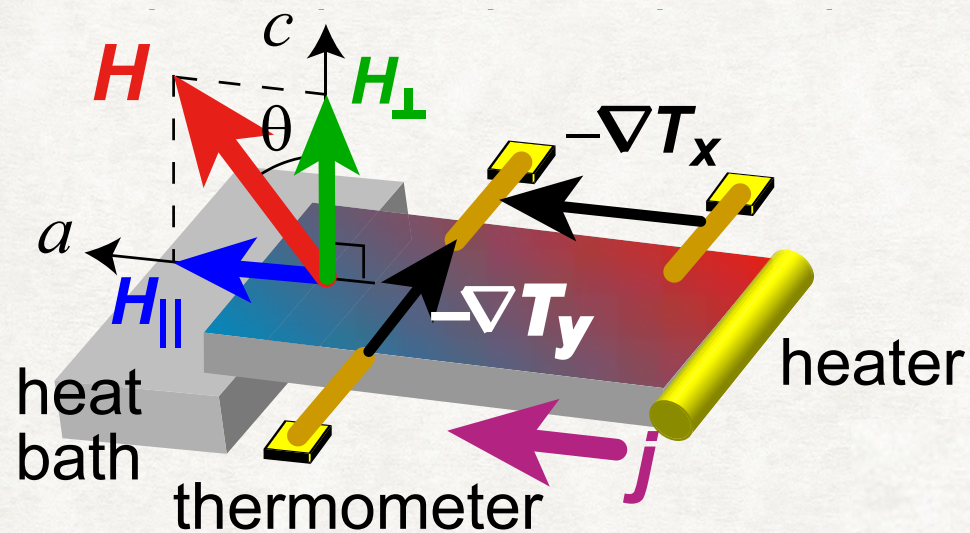
$$c=1/2$$

a universal prediction for chiral "Ising
anyon" phase: *agnostic to
microscopic spin interactions*

KITAEV SPIN LIQUID

MATSUDA: QUANTIZED THERMAL HALL EFFECT?

- Kasahara *et al*, 2018. α -RuCl₃



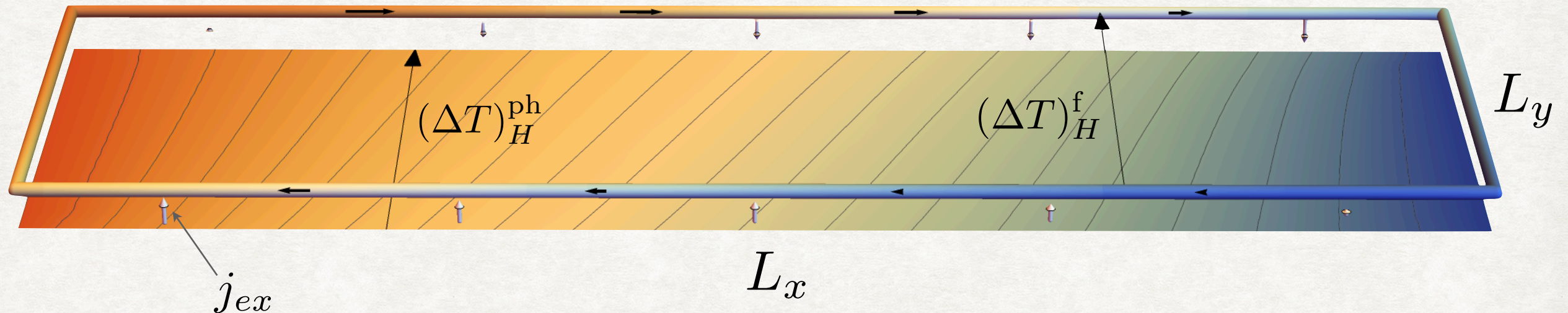
Evidence for an *emergent* chiral Majorana fermion edge mode?

Questions:

- Tiny Hall angle? **Savary**
- Reproducibility?
- Why should the nonabelian QSL be stabilized?

KITAEV SPIN LIQUID

- **Savary:** How about that small Hall angle?
- Difference from electrical transport: phonons+spins both carry heat. May there be a phonon miracle??

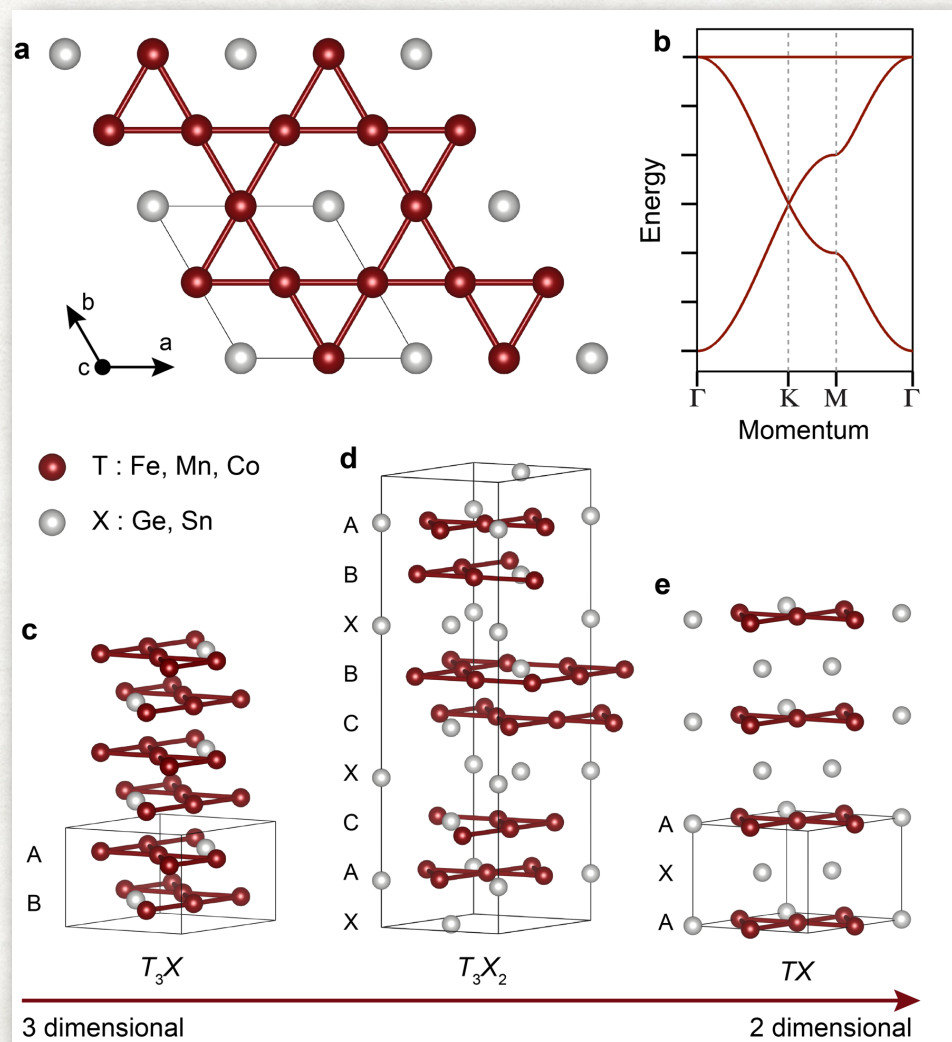


COUPLE SPINS TO ELECTRONS

- Go to war with the fermions you have, not the fermions you might want or wish to have at a later time (Donald Rumsfeld)
- Magnetic Weyls: Pyrochlore iridates, Mn_3Sn , Heuslers, RAIGe ,...
- Topological Kondo insulators: SmB_6 , YbB_{12} , ...
- Magnetically doped topological insulators: $\text{Cr-Bi}_2\text{Se}_3$, MnBi_2Te_4 ,...
- Magnetic 2d Dirac fermions? *Checkelsky*

COUPLE SPINS TO ELECTRONS

- **Checkelsky**: Fe_xSn_y : Dirac fermions plus spins on a kagome lattice

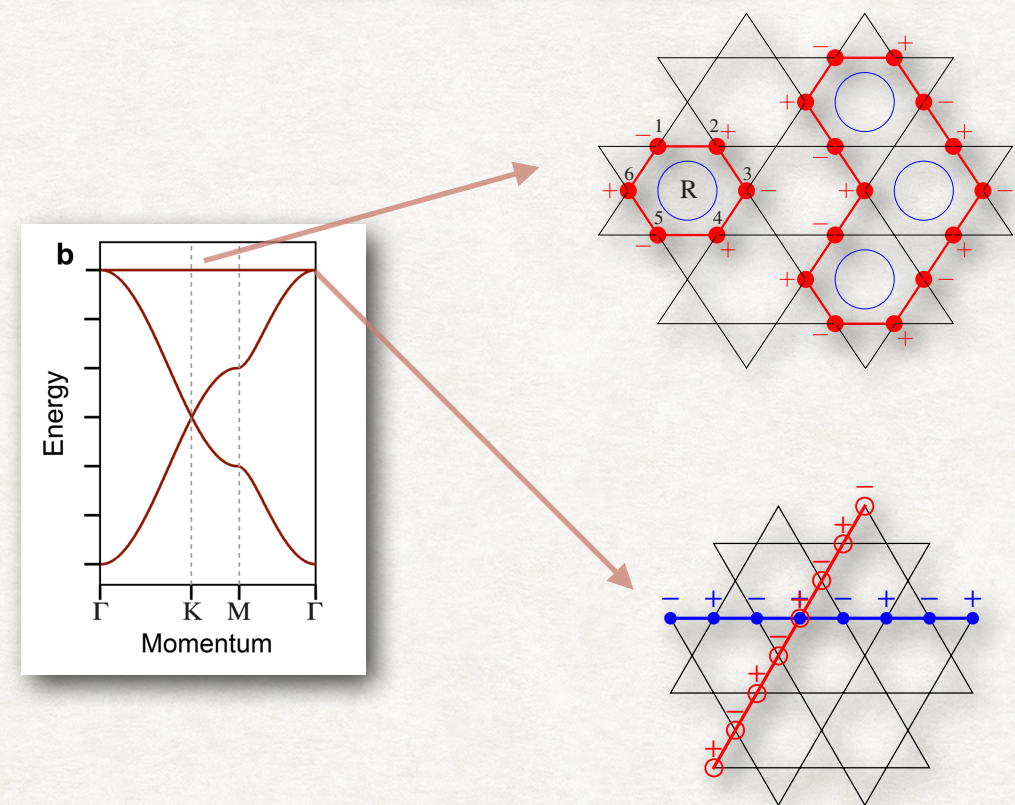


Old times

PHYSICAL REVIEW B **78**, 125104 (2008)

Band touching from real-space topology in frustrated hopping models

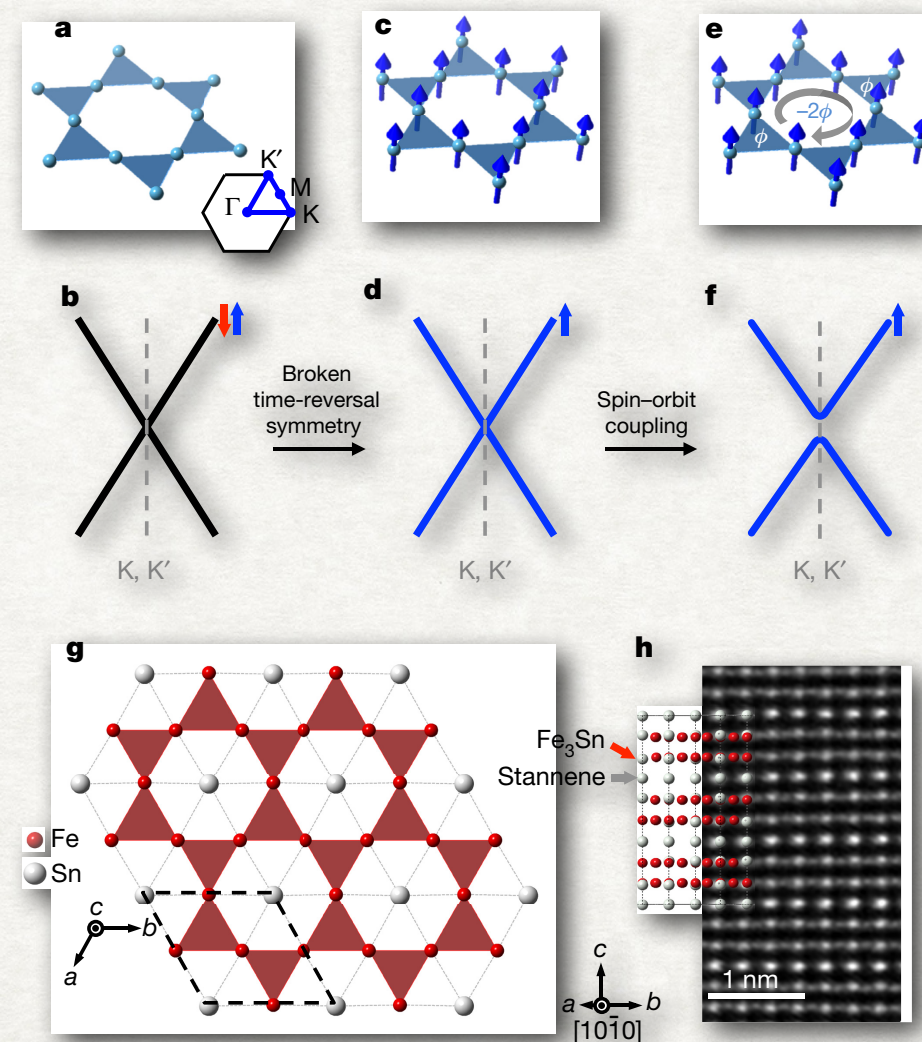
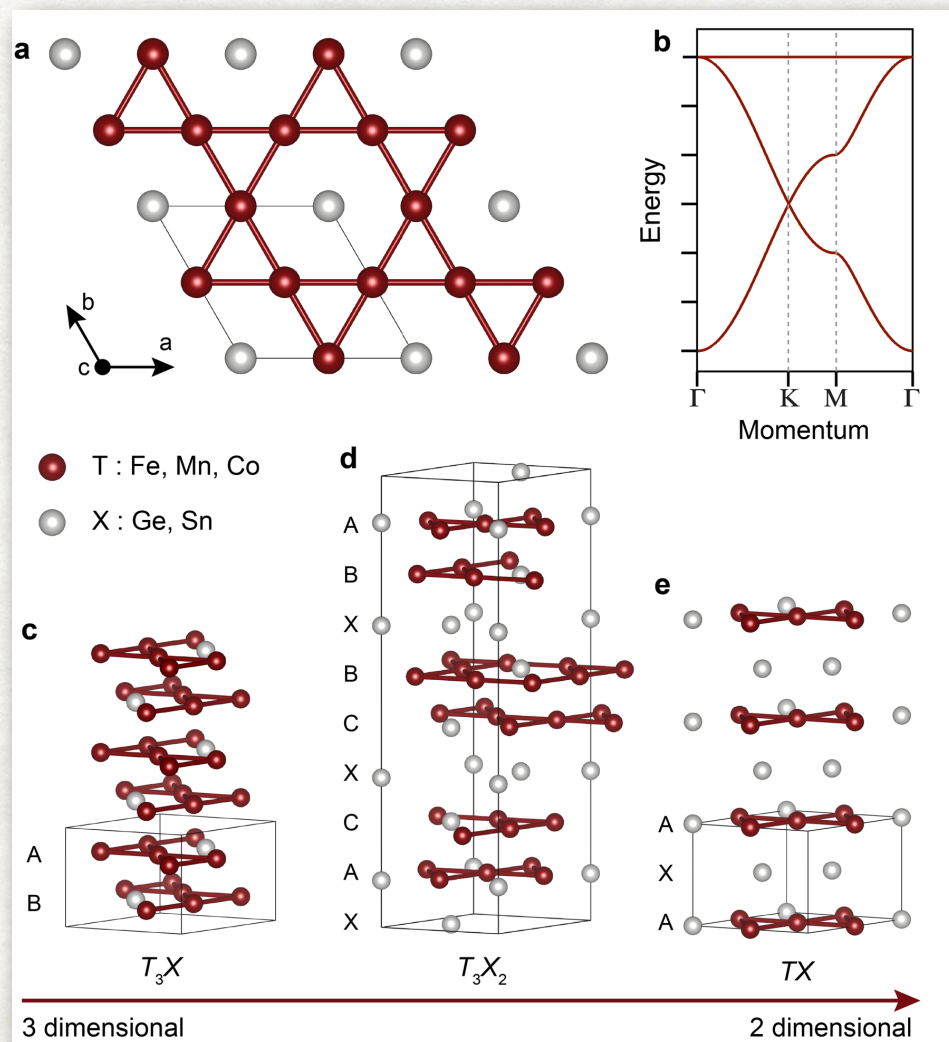
Doron L. Bergman,¹ Congjun Wu,² and Leon Balents³



COUPLE SPINS TO ELECTRONS

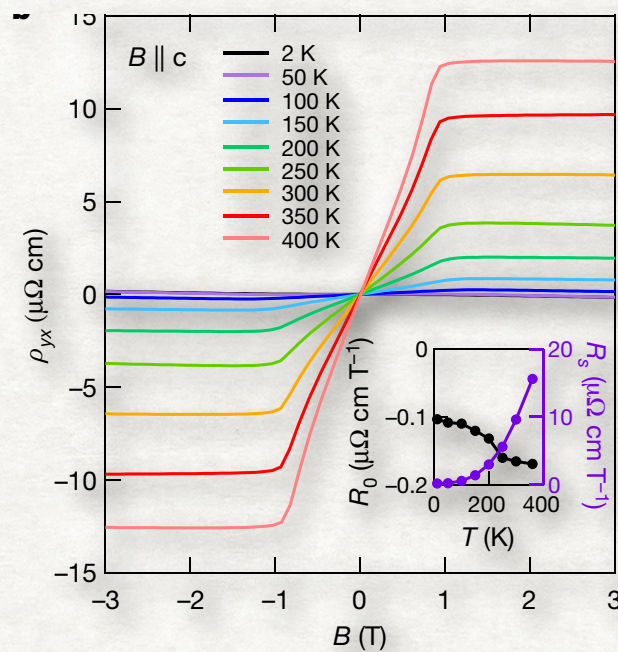
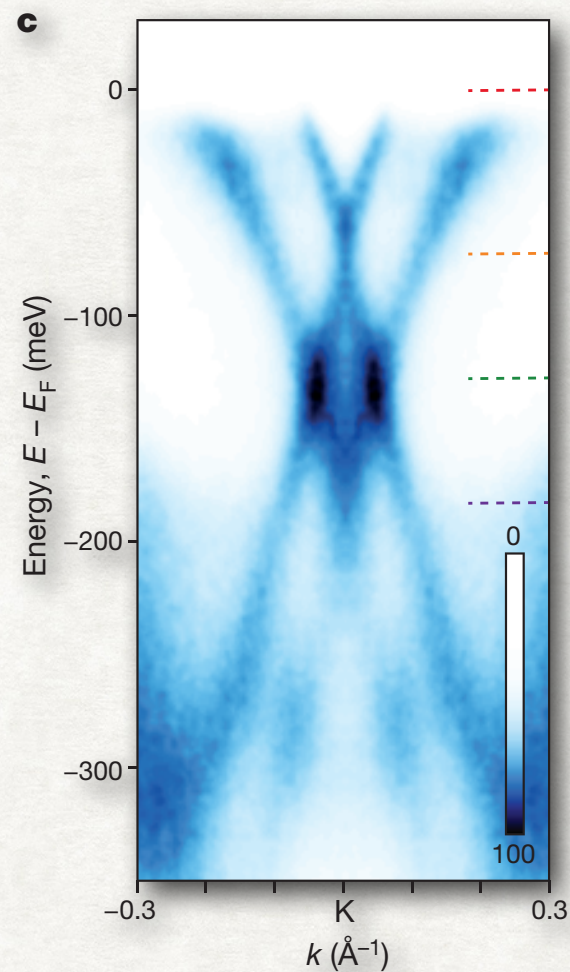
- **Checkelsky**: Fe_xSn_y : Dirac fermions plus spins on a kagome lattice

Q: What orbitals? Why is "s"-orbital TB model relevant?



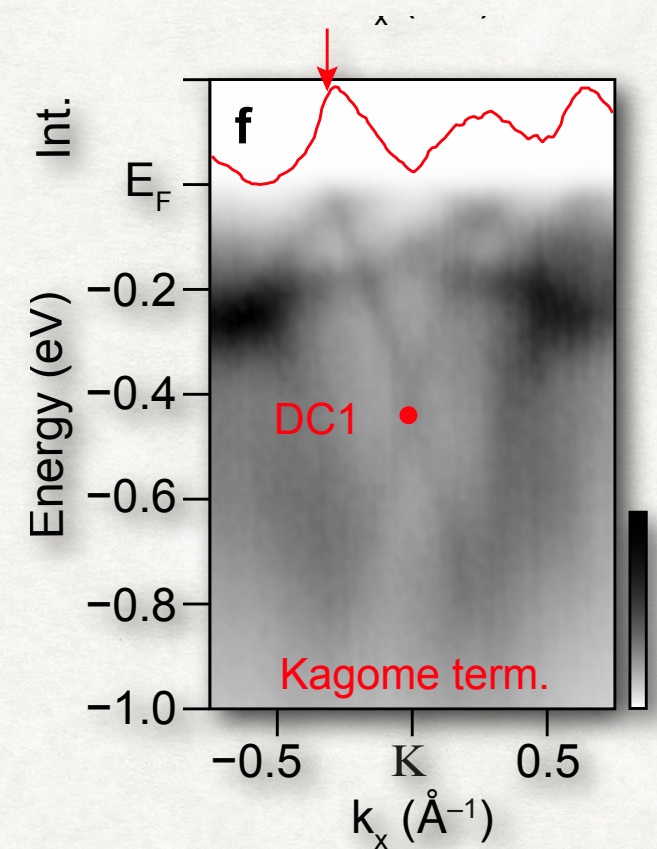
KAGOME DIRAC FERMIONS?

- Fe_3Sn_2 (bilayer)



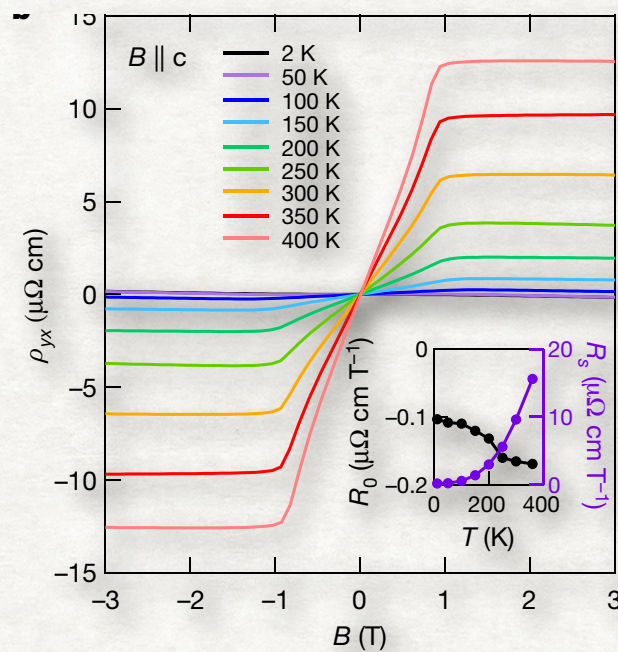
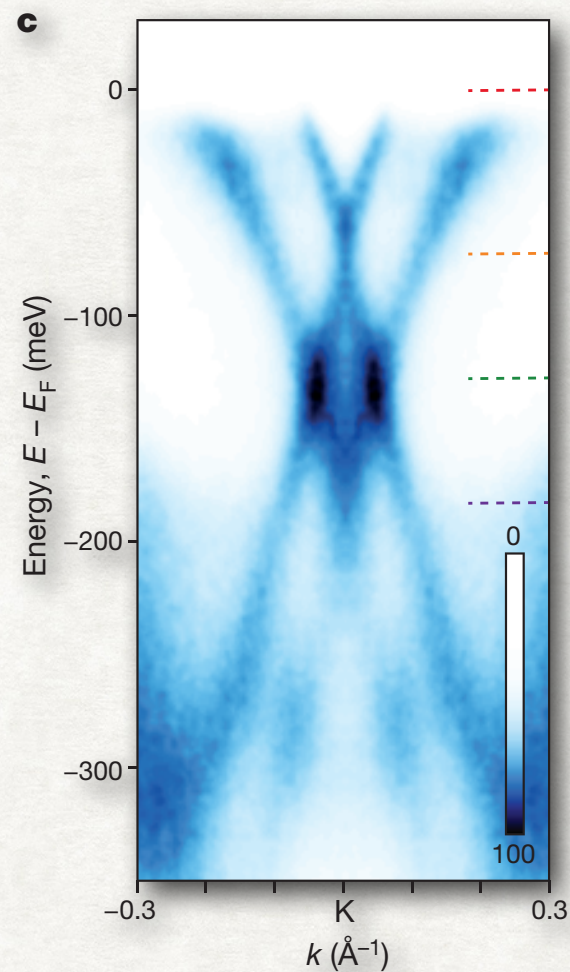
Q: AHE strongly decreases with lower temperature?

- FeSn (single layer)



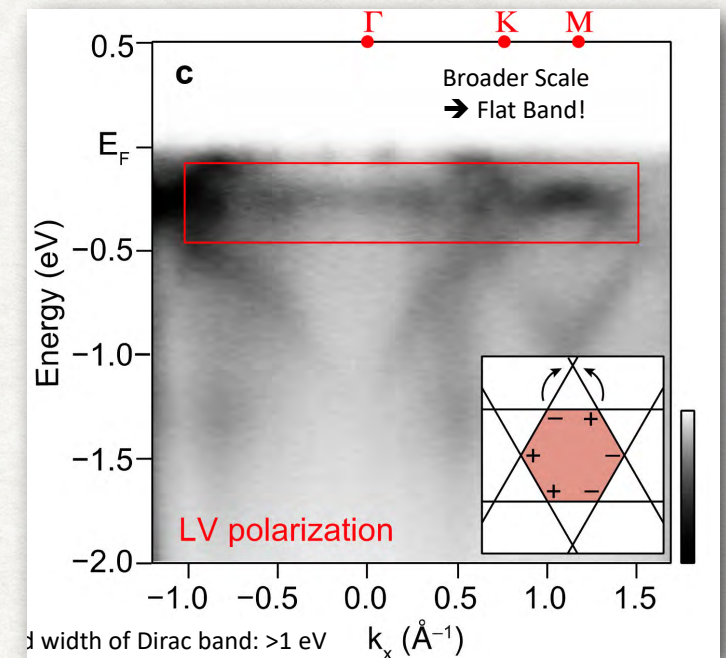
KAGOME DIRAC FERMIONS?

- Fe₃Sn₂ (bilayer)



Q: AHE strongly decreases with lower temperature?

- FeSn (single layer)

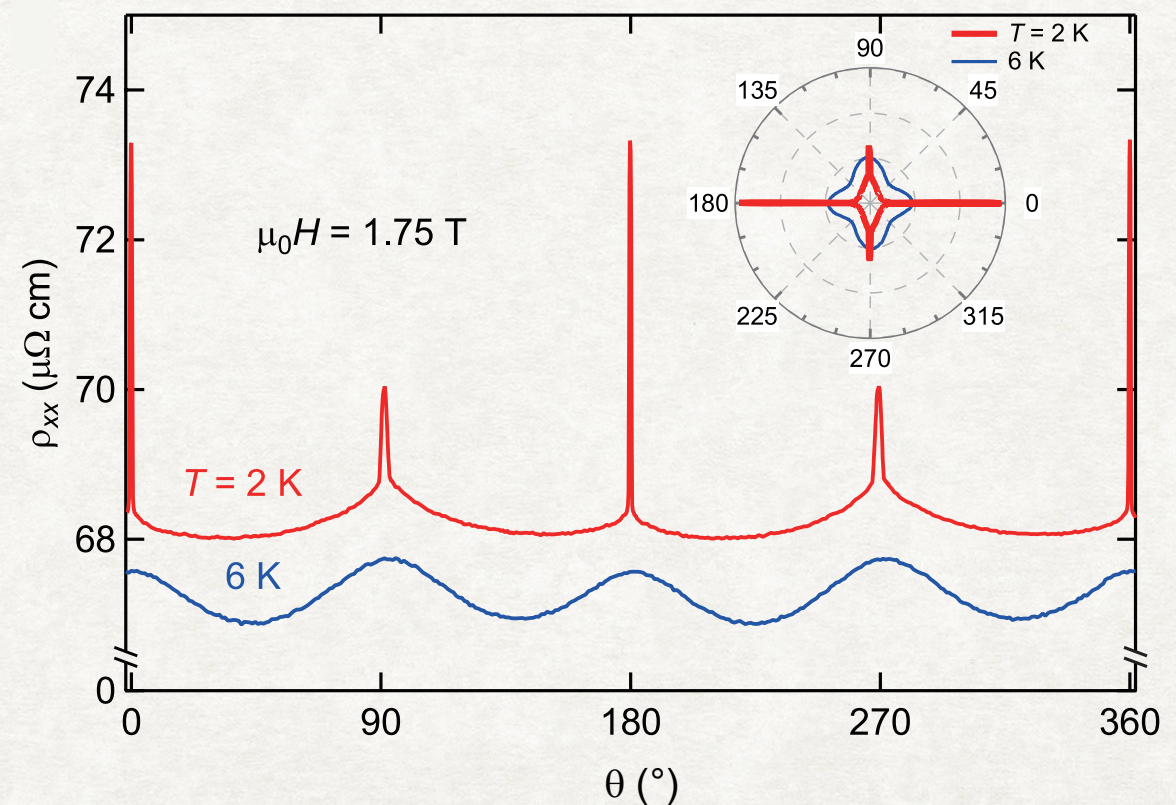
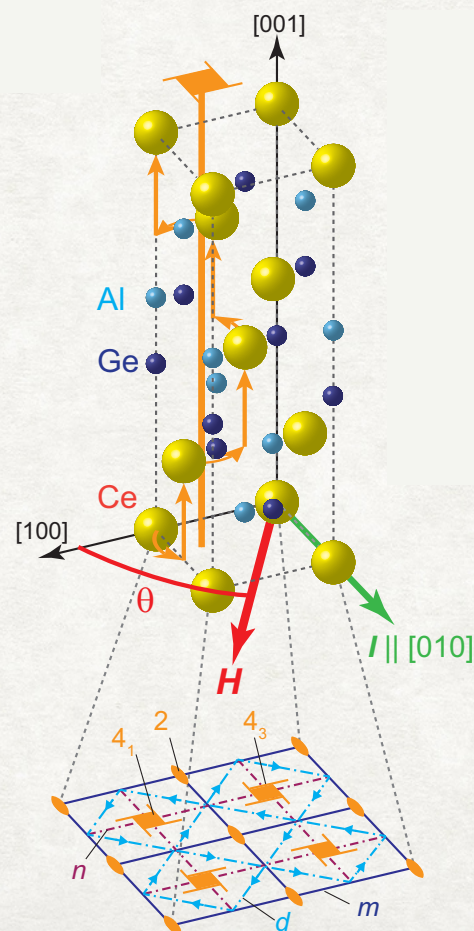


Flat band??!??!

Q: Correlation effects?

SINGULAR ANGULAR MAGNETORESISTANCE

- **Savary**: surprising transport phenomena in CeAlGe - an antiferromagnetic topological semimetal
- Let me spoil the surprise



Lucile will explain this!

LET'S GO!!

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